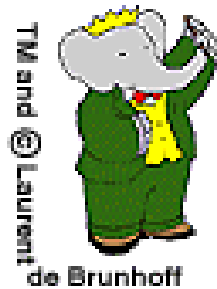


# BaBar Measurements of CP Violation, Mixing and Lifetimes of B Mesons

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Spåtind, Norway

# Outline

- CP Violation, CKM Matrix and the Unitarity Triangle
- Observation of CP Violation in the interference of Decay and Mixing  $\Rightarrow \sin 2\beta$ 
  - The PEP-II B Factory & The BaBar Detector
  - The three linked steps towards the  $\sin 2\beta$  measurement
    - B Lifetime
    - B Mixing ( $\Rightarrow$  digression on dileptons...)
    - CP Asymmetry
- The way forward : Summary and Outlook

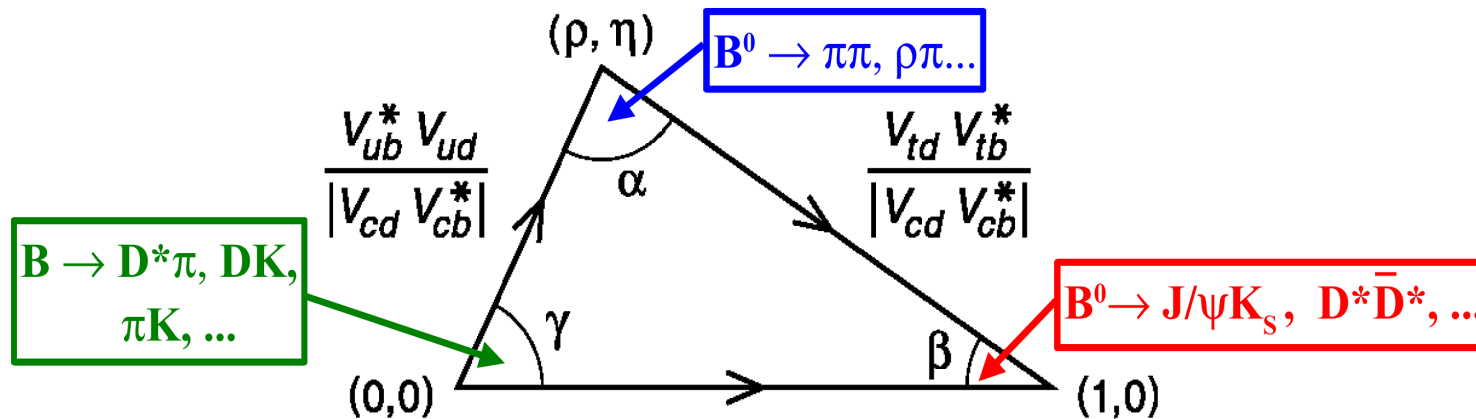
# CP violation in the Standard Model

CP violation arises from **single phase in CKM matrix**

$$V = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} = \begin{pmatrix} 1 - \frac{1}{2}\lambda^2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \frac{1}{2}\lambda^2 & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix} + \mathcal{O}(\lambda^4)$$

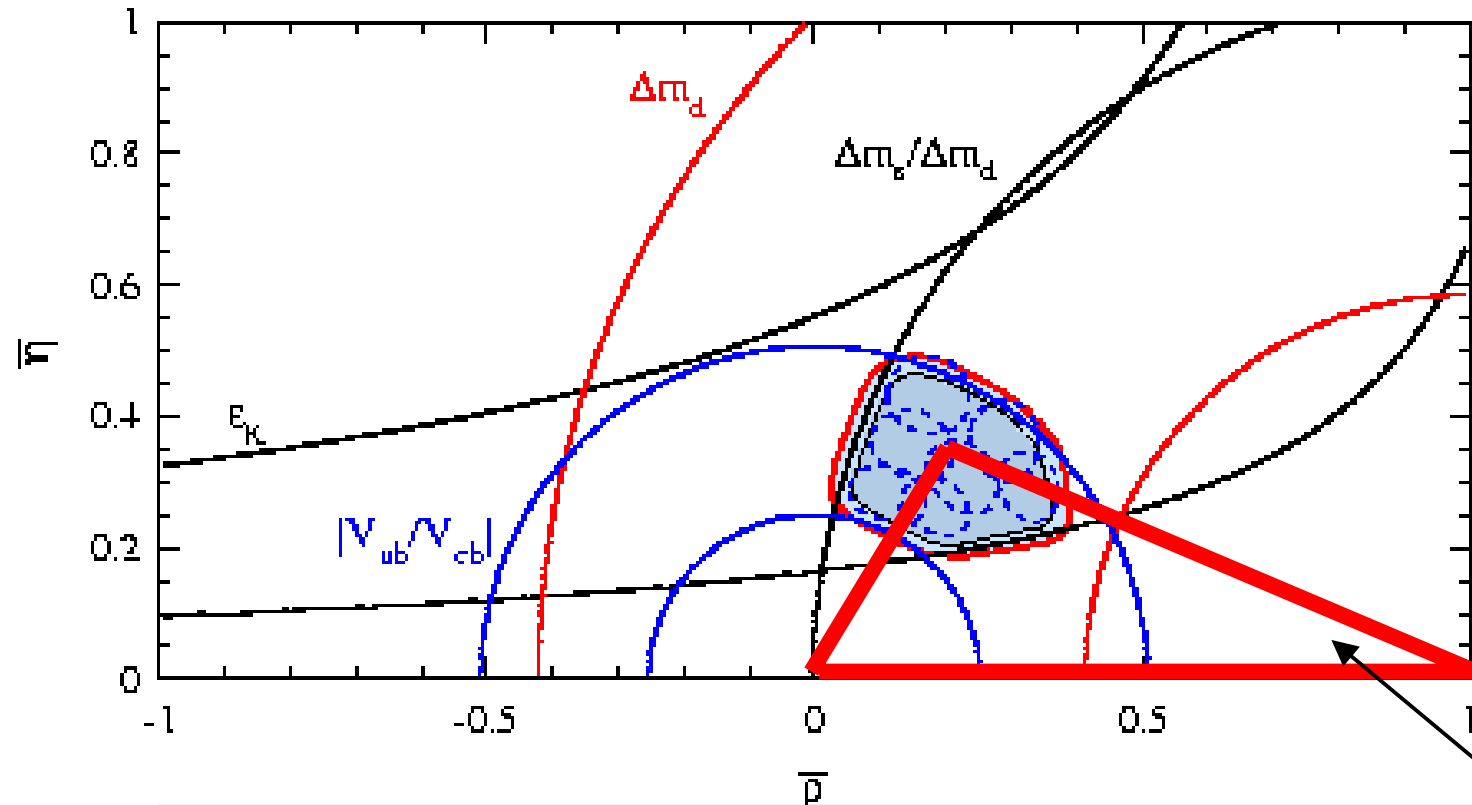
Unitarity of  $V$  implies eg.  $V_{ud}V_{ub}^* + V_{cd}V_{cb}^* + V_{td}V_{tb}^* = 0$

→ represented as **'unitary triangle'** in complex plane



**CP asymmetries in  $B^0$  decays give information on angles  $\alpha$ ,  $\beta$ ,  $\gamma$ !**

# The Unitarity Triangle without CP Violation Measurements



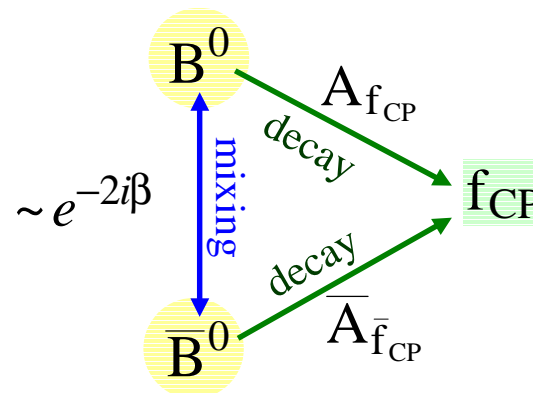
Method described in  
Höcker et al,  
hep-ex/0104062

➤ Test SM by over-constraining Unitarity Triangle with measurements of sides **and** angles

$\beta$

# CP from Interference of Mixing and Decay

CP violation results from interference between decays with and without mixing



$$\lambda_{f_{CP}} = \frac{q}{P} \frac{\bar{A}_{f_{CP}}}{A_{f_{CP}}}$$

$$= |\lambda_{f_{CP}}| e^{-2i\varphi_{CP}}$$

$$\lambda_{f_{CP}} \neq \pm 1 \Rightarrow \text{Prob}(\bar{B}_{\text{phys}}^0(t) \rightarrow f_{CP}) \neq \text{Prob}(B_{\text{phys}}^0(t) \rightarrow f_{CP})$$

## Time-dependent CP asymmetry:

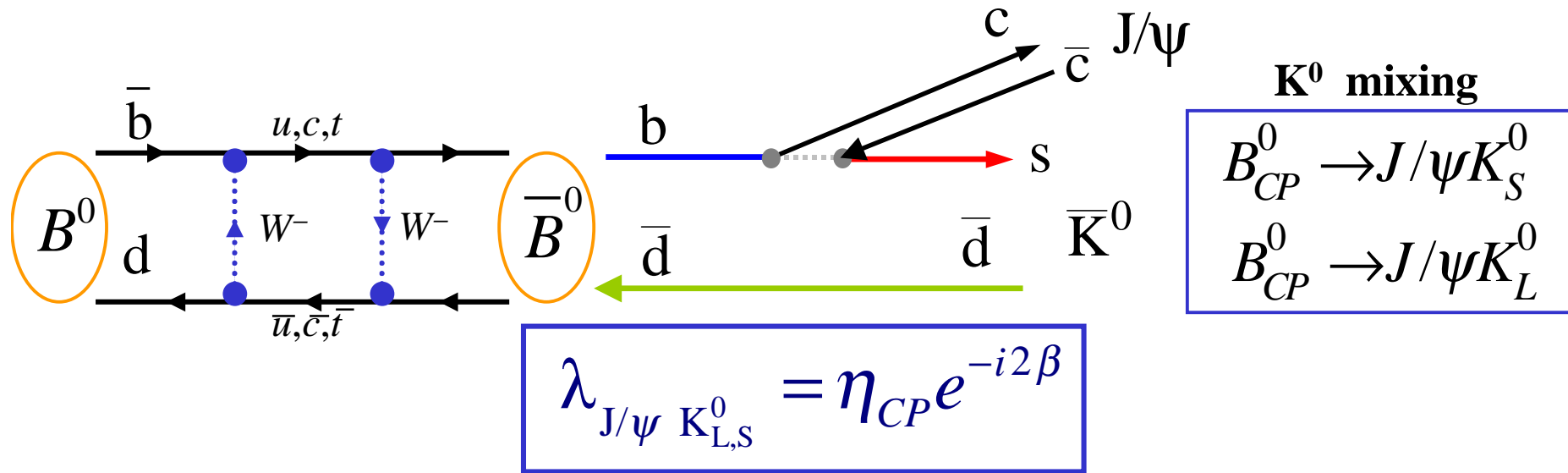
$$A_{f_{CP}}(t) = \frac{\Gamma(\bar{B}_{\text{phys}}^0(t) \rightarrow f_{CP}) - \Gamma(B_{\text{phys}}^0(t) \rightarrow f_{CP})}{\Gamma(\bar{B}_{\text{phys}}^0(t) \rightarrow f_{CP}) + \Gamma(B_{\text{phys}}^0(t) \rightarrow f_{CP})}$$

$$= C_{f_{CP}} \cos(\Delta m_d t) + S_{f_{CP}} \sin(\Delta m_d t)$$

$$C_{f_{CP}} = \frac{1 - |\lambda_{f_{CP}}|^2}{1 + |\lambda_{f_{CP}}|^2}$$

$$S_{f_{CP}} = \frac{-2 \text{Im} \lambda_{f_{CP}}}{1 + |\lambda_{f_{CP}}|^2}$$

# The “Golden” Decay Mode: $B^0 \rightarrow J/\psi K^0_S$



- Theoretically clean mode to measure  $\sin 2\beta$
- Clean experimental signature
- “Large” branching fraction compared to other CP eigenstates

Time-dependent CP asymmetry

$$A_{CP}(t) = -\eta_{CP} \sin 2\beta \sin(\Delta m t)$$

“Golden Modes”

- $\eta_{CP} = -1$ 
  - ✓  $B^0 \rightarrow J/\psi K_S^0$
  - ✓  $B^0 \rightarrow \psi(2s) K_S^0$

➤  $\eta_{CP} = +1$

✓  $B^0 \rightarrow J/\psi K_L^0$

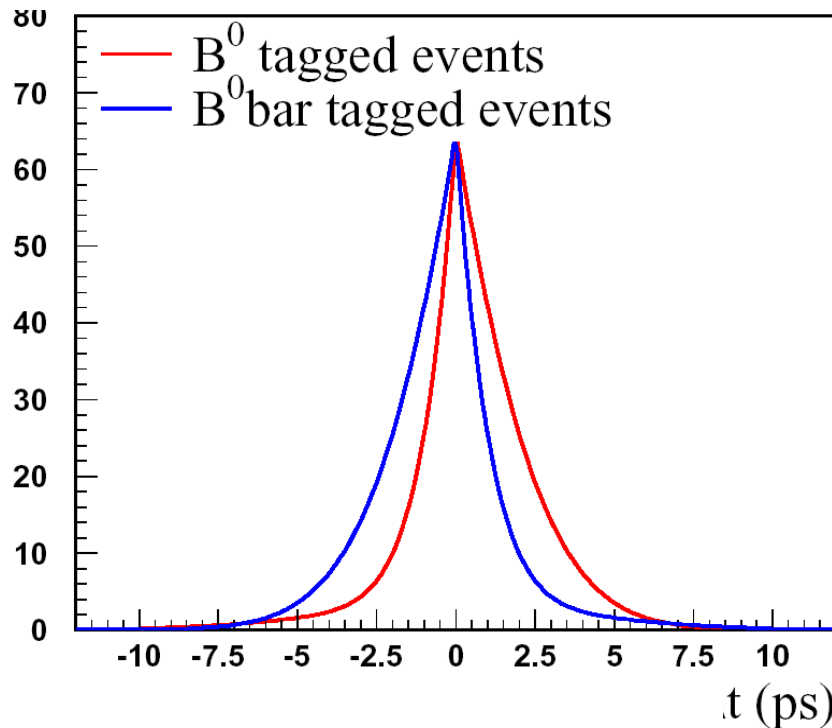
# Decay Time Distribution in $B \rightarrow f_{CP}$

$$f_+ : \bar{B}_{phys}^0 \rightarrow f_{CP}$$

$$f_- : B_{phys}^0 \rightarrow f_{CP}$$

$$f_{\pm}(B \rightarrow f_{CP}, t) = \frac{\Gamma}{4} e^{-\Gamma |\Delta t|} [1 \pm C_{f_{CP}} \cos(\Delta m_d t) \mp S_{f_{CP}} \sin(\Delta m_d t)]$$

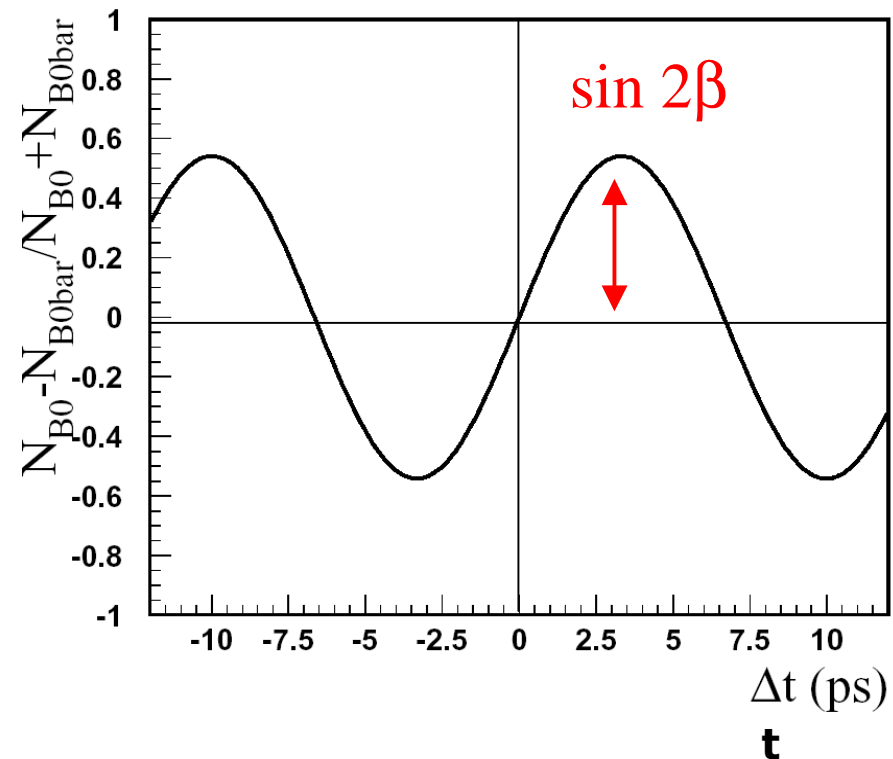
# Decay Time Evolution & $A_{CP}$ for $B^0 \rightarrow J/\psi K_S^0$



$$A_{CP}(t) = -\eta_f \sin 2\beta \sin(\Delta m_d t)$$

- In this ideal case, the amplitude of the oscillation is the CP Asymmetry
- time-integrated asymmetry is 0

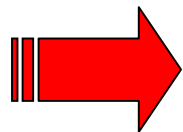
- $t$  spectrum and the observed asymmetry for a perfect detector (assuming  $\sin 2\beta = 0.6$ )
- Visible difference between  $B^0$  and  $\bar{B}^0$  decay rates





# Exptal Requirements For CPV Measurement

- BR ( $B \rightarrow f_{CP}$ )  $\sim 10^{-4} \Rightarrow$  Need to record and **reconstruct** a large # of B Mesons
- Determine the **flavor** of the initial B meson to separate  $B^0$  from  $\bar{B}^0$  ( B Flavor Tagging)
- Define and measure a **'time'** in order to study the time-dependent asymmetry
  - B Mesons must travel a measurable distance before decaying
  - Vertex Reconstruction: A high precision tracking system to measure the distance between the B decay points



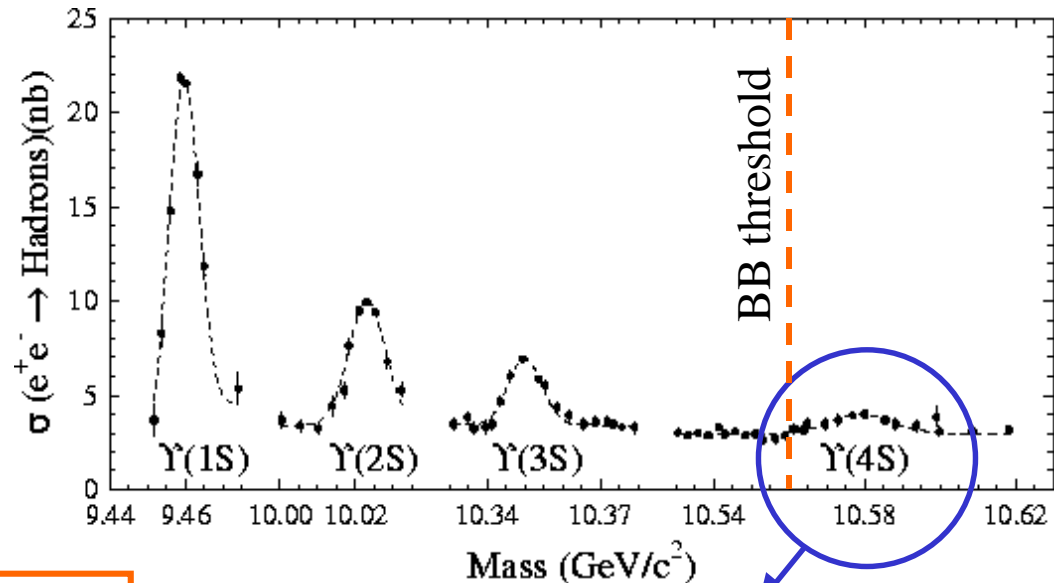
BaBar Detector @ PEP-II B Factory as example

# The Asymmetric Energy Collider@Y(4S):PEPII

Cleanest source of B<sup>0</sup> mesons:  $e^+e^- \rightarrow Y(4S) \rightarrow B\bar{B}$  at  $\sqrt{s} = 10.58 \text{ GeV}$

$\sigma_{Y(4S)} \approx 1.05 \text{ nb}$   
(24% of  $\sigma_{\text{had}}$ )

The Y(4S) B<sup>0</sup>B<sup>0</sup> system evolves coherently until one of the B<sup>0</sup> mesons decays, so:

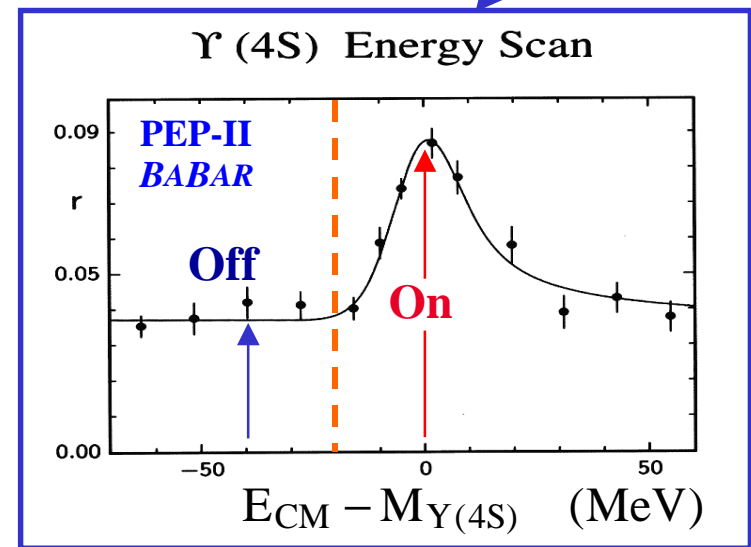


$$A_{CP}(t) \rightarrow A_{CP}(\Delta t) \propto \sin(\Delta m_{B_d} \Delta t)$$

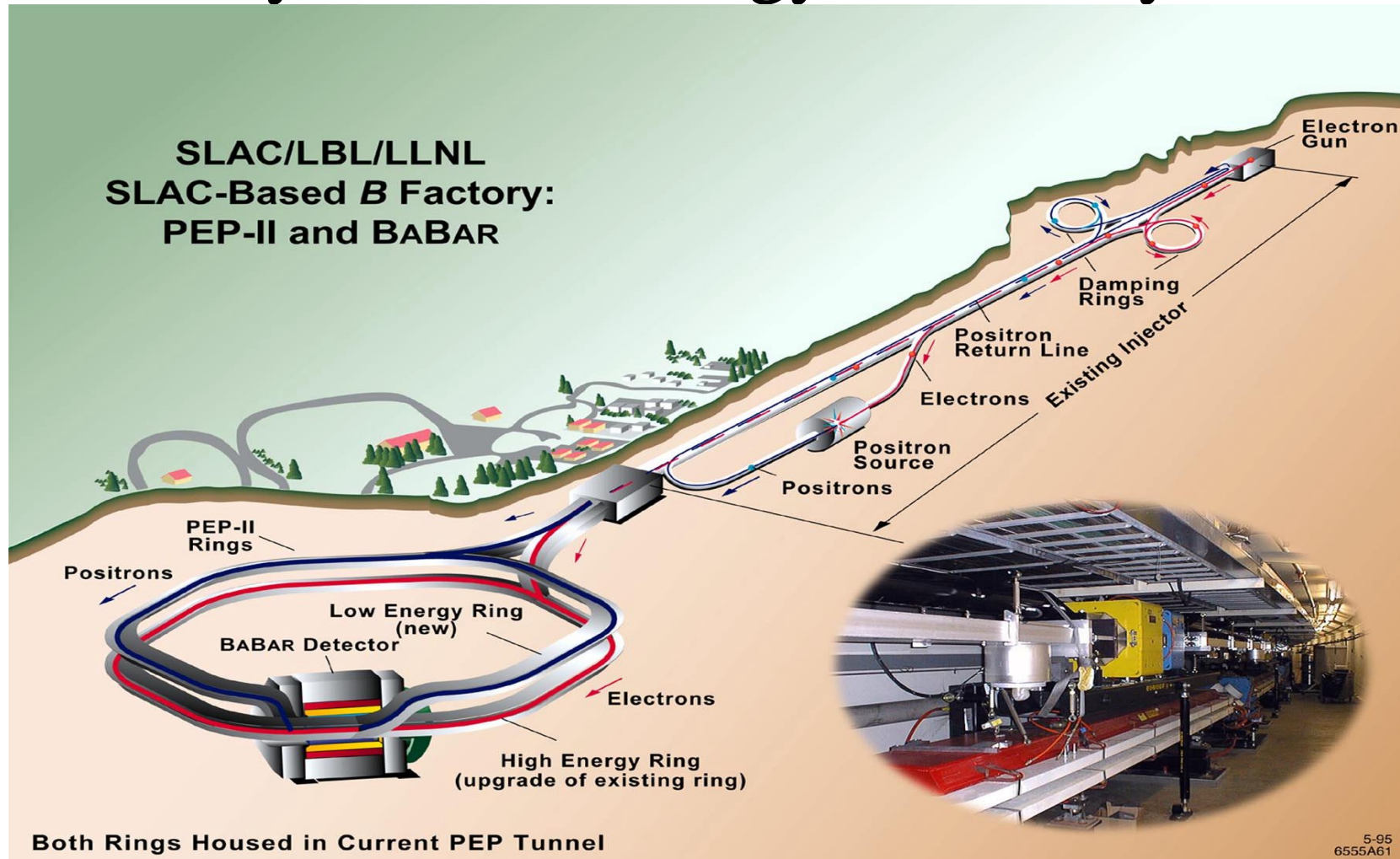
$\Delta t$  : proper time difference between the two B decays

$A_{CP}(\Delta t)$  integrates to zero over all  $\Delta t$

Study of CPV  $\Rightarrow$  measure of  $\Delta t$



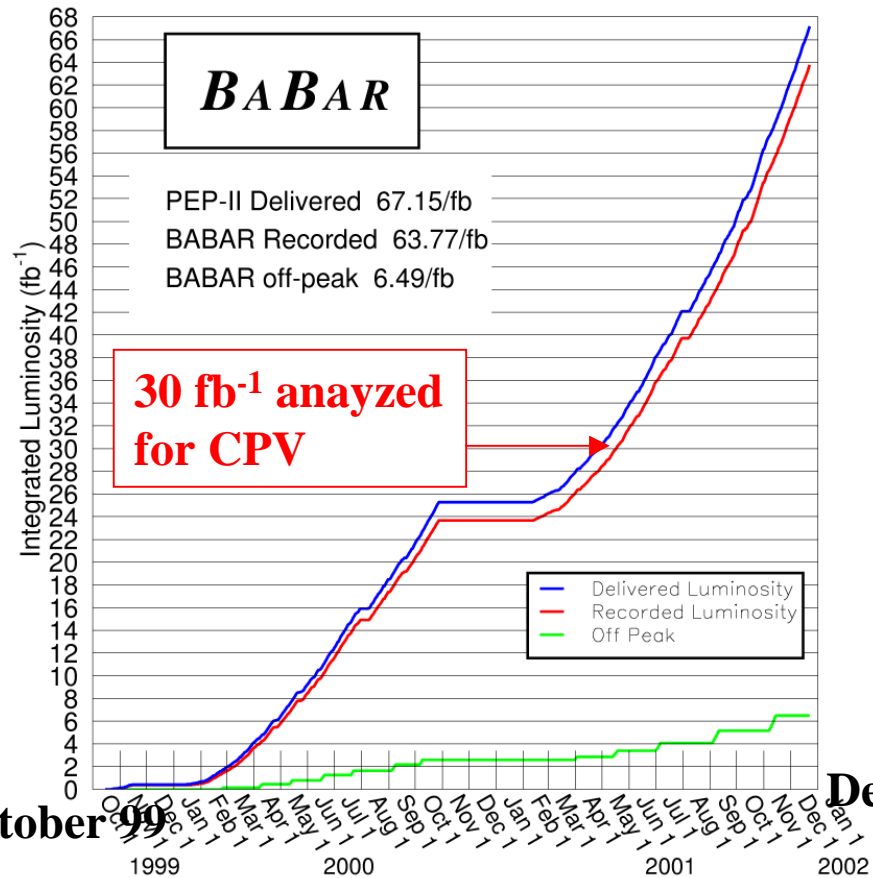
# PEP-II Asymmetric Energy B-Factory at SLAC



Collides 9 GeV  $e^-$  on 3.1 GeV  $e^+$

$Y(4S)$  boost in lab frame :  $\beta\gamma = 0.56$

# PEP-II Performance Has Been Spectacular !



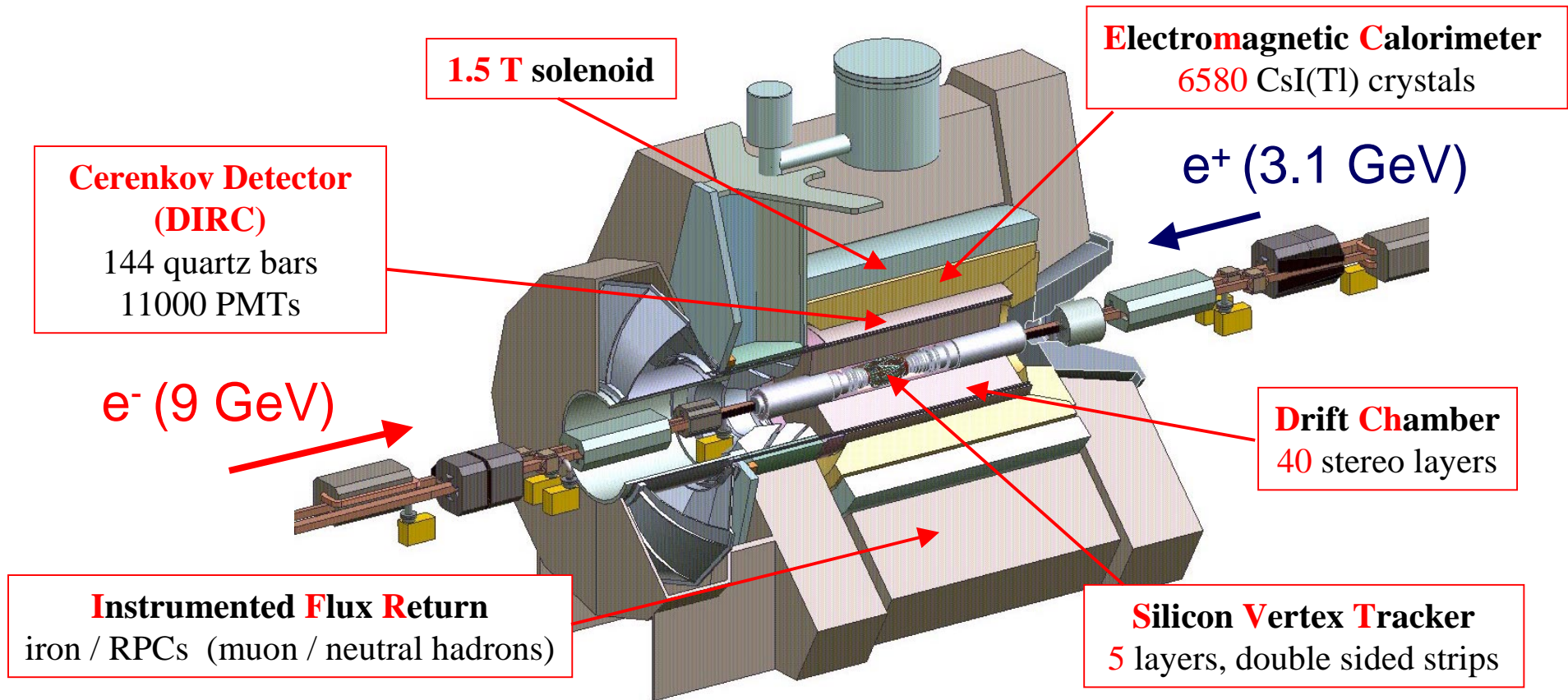
- PEP-II top luminosity:  
 $4.513 \times 10^{33} \text{ cm}^{-2}\text{s}^{-1}$   
 (design:  $3.0 \times 10^{33}$ )
- Top recorded Lumi/month:  $6.35 \text{ fb}^{-1}$
- Top recorded Lumi/week:  $1.76 \text{ fb}^{-1}$
- Top recorded Lumi/24hr:  $303 \text{ pb}^{-1}$
- Top recorded Lumi/8hr:  $105 \text{ pb}^{-1}$
- BaBar logging efficiency:  $>96\%$

PEP-II delivered: 67.15 fb-1

BaBar recorded: 63.77 fb-1 (including 5.49 fb-1 off-peak)

120 million B's recorded, being analysed!

# The BaBar Detector



**SVT:** 97% efficiency, 15  $\mu\text{m}$  z hit resolution (inner layers, perp. tracks)

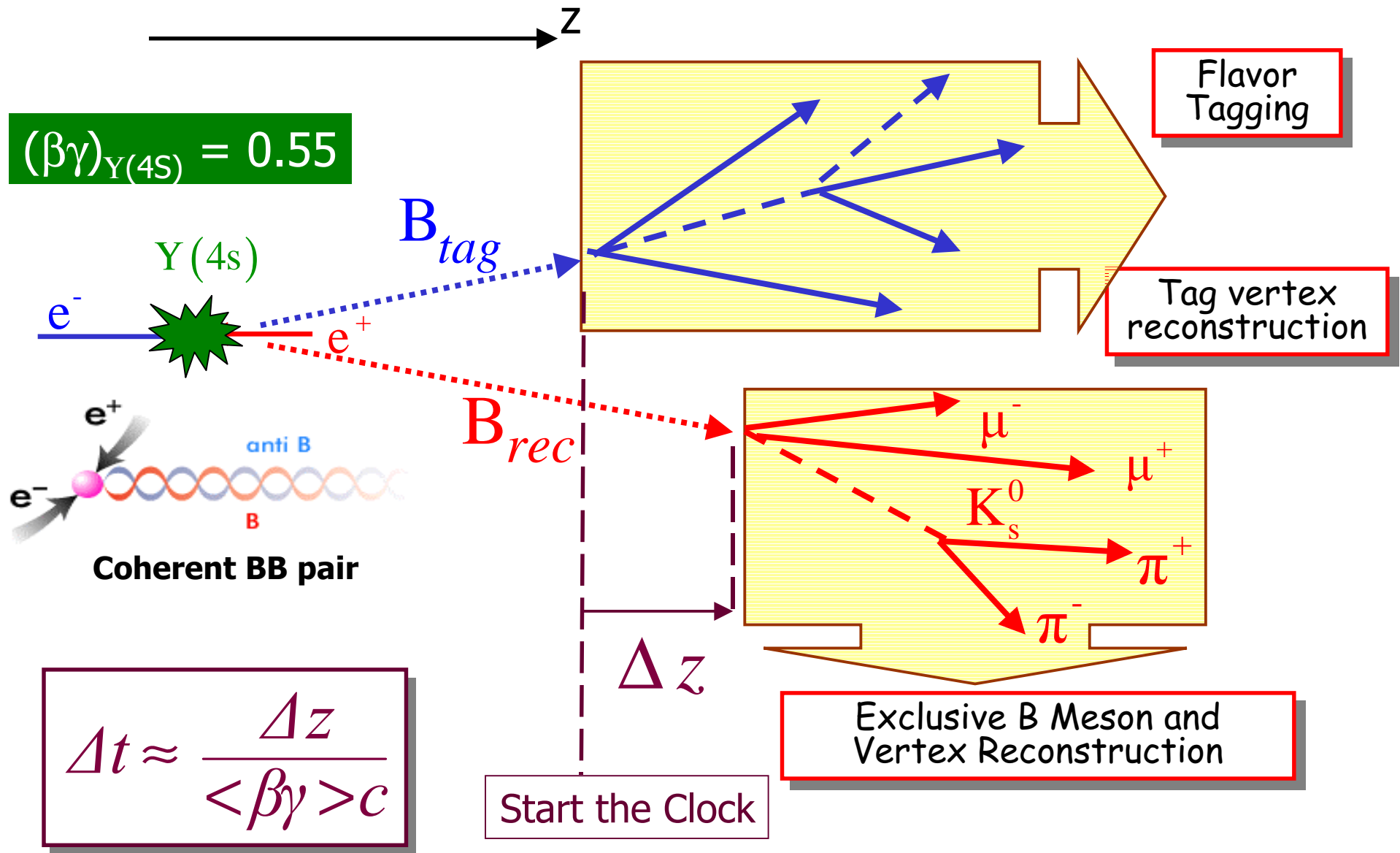
**SVT+DCH:**  $\sigma(p_T)/p_T = 0.13 \% \times p_T + 0.45 \%$

**DIRC:** K- $\pi$  separation 4.2  $\sigma$  @ 3.0 GeV/c  $\rightarrow$  2.5  $\sigma$  @ 4.0 GeV/c

**EMC:**  $\sigma_E/E = 2.3 \% \cdot E^{-1/4} \oplus 1.9 \%$

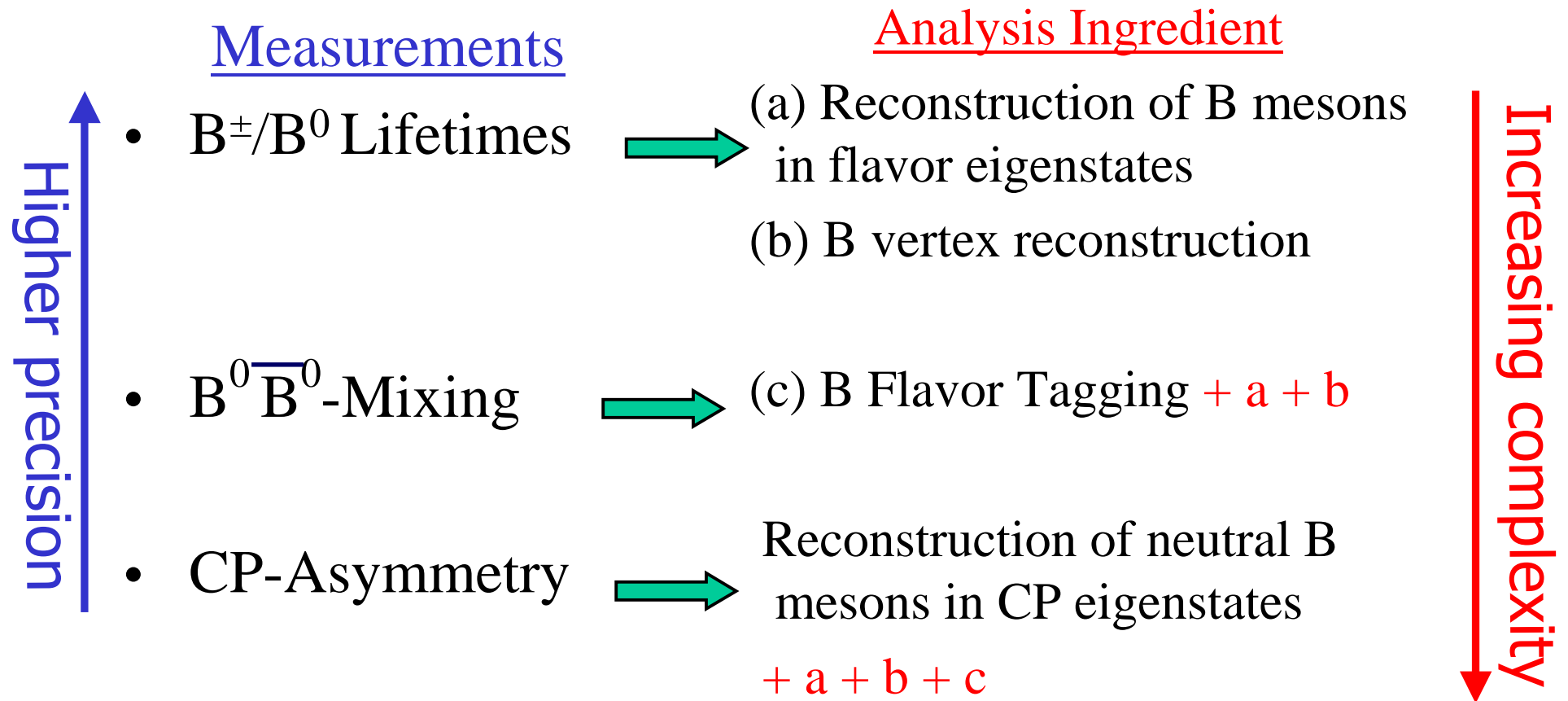


# B Event Topology at the Boosted $\Upsilon(4S)$

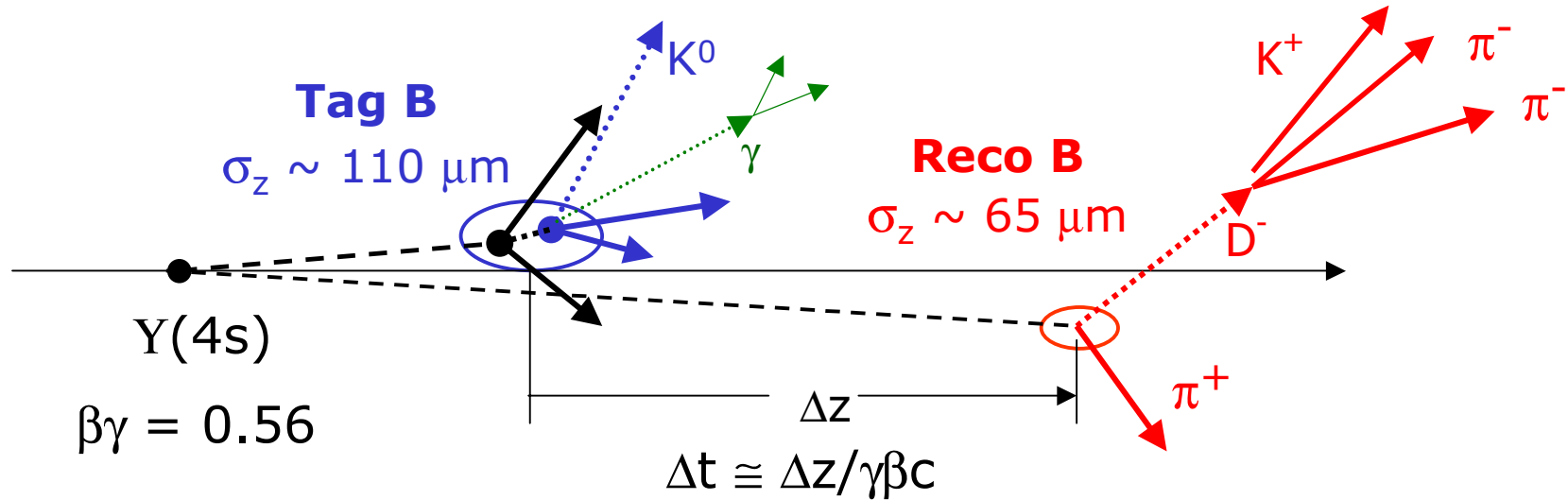


# Sin2 $\beta$ Analysis Strategy

Factorize the time-dependent analysis in 3 building blocks  
Obtain All analysis ingredients from DATA (not MC)



# Measurement of the $B^0$ and $B^+$ Lifetime



**3. Reconstruct Inclusively the vertex of the "other" B meson ( $B_{\text{TAG}}$ )**

**1. Fully reconstruct one B meson in self tagging ( $B_{\text{REC}}$ )**  
**2. Reconstruct the decay vertex**

**4. compute the proper time difference  $\Delta t$**   
**5. Fit the  $\Delta t$  spectra**

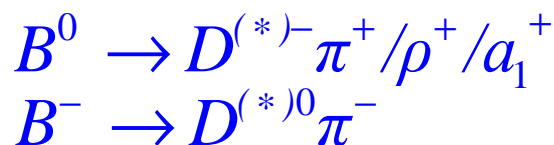
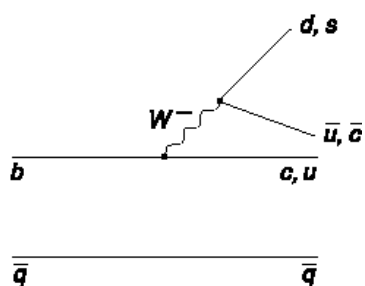


# Fully-Reconstructed Hadronic B Decay sample

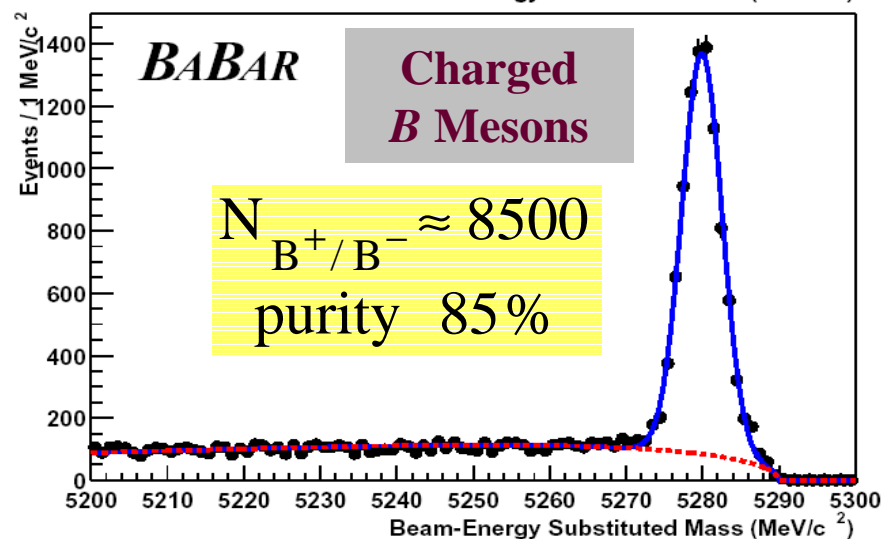
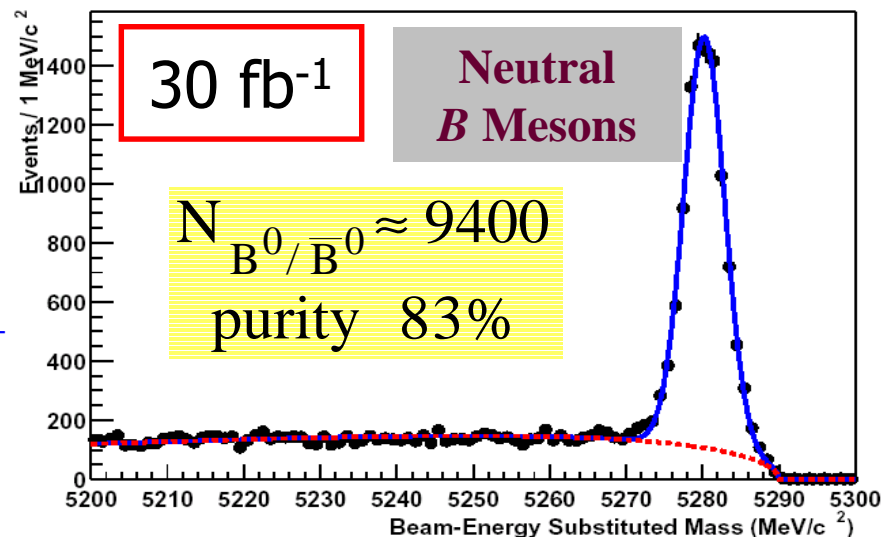
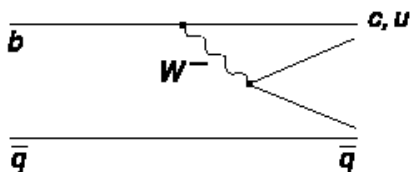
**Flavor Eigenstates  $B_{\text{flav}}$**  : for lifetime and mixing measurements

Self-tagging hadronic decays

$b \rightarrow c \bar{u} d$  "Open Charm" decays



Hadronic decays into final states with Charmonium  $b \rightarrow (c \bar{c}) s$



$$m_{\text{ES}} = \sqrt{(E_{\text{beam}}^{\text{cm}})^2 - (\mathbf{p}_B^{\text{cm}})^2} \text{ [GeV]}$$

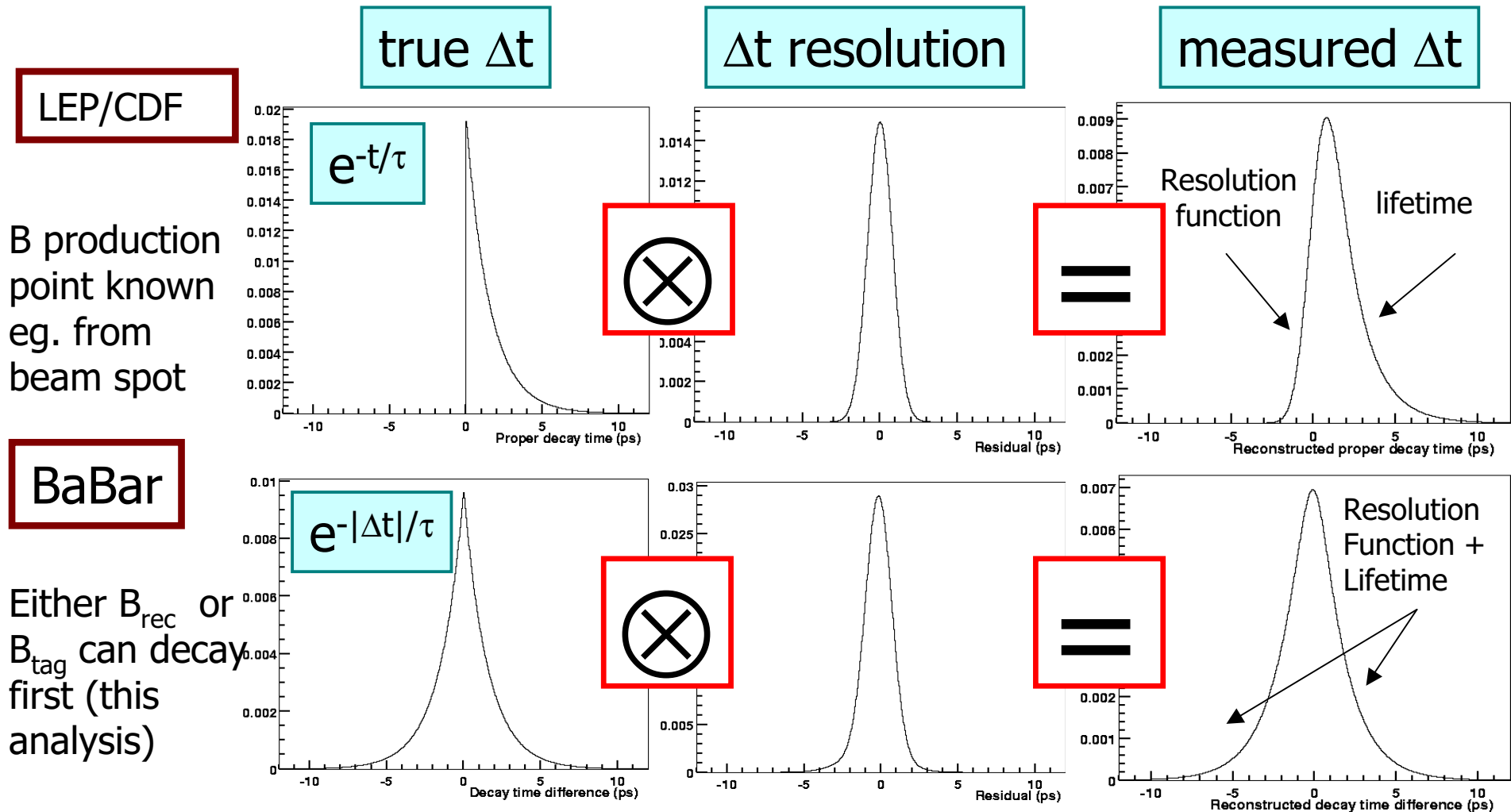
# Recoil (Tag) side Vertex and $\Delta z$ Reconstruction

- Reconstruct  $B_{\text{rec}}$  vertex from
  - charged  $B_{\text{rec}}$  daughters
- Determine  $B_{\text{Tag}}$  vertex from
  - charged tracks not belonging to  $B_{\text{rec}}$
  - $B_{\text{rec}}$  vertex and momentum
  - beam spot and  $Y(4S)$  momentum



- High efficiency (97%)
- Average  $\Delta z$  resolution is  $180 \mu\text{m}$  ( $\langle |\Delta z| \rangle \sim \beta\gamma c\tau = 260 \mu\text{m}$ )
- $\Delta t$  resolution function characterized from data

# $\tau_B$ Measurement at Boosted $\Upsilon(4S)$ : Unique



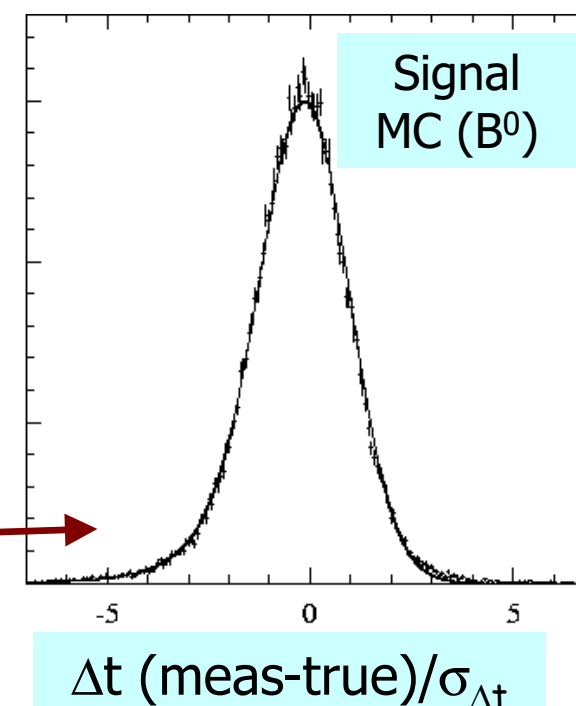
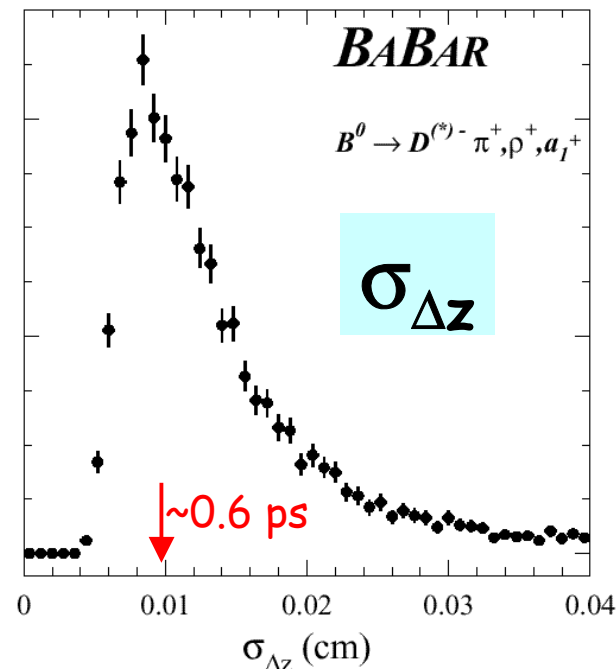
Need to disentangle resolution function from physics

# $\Delta t$ Resolution Function

- event-by-event  $\sigma(\Delta t)$  from vertex errors
- Charm Lifetime induced bias leads to
  - Small correlation between the lifetime and the Resolution Function parameters

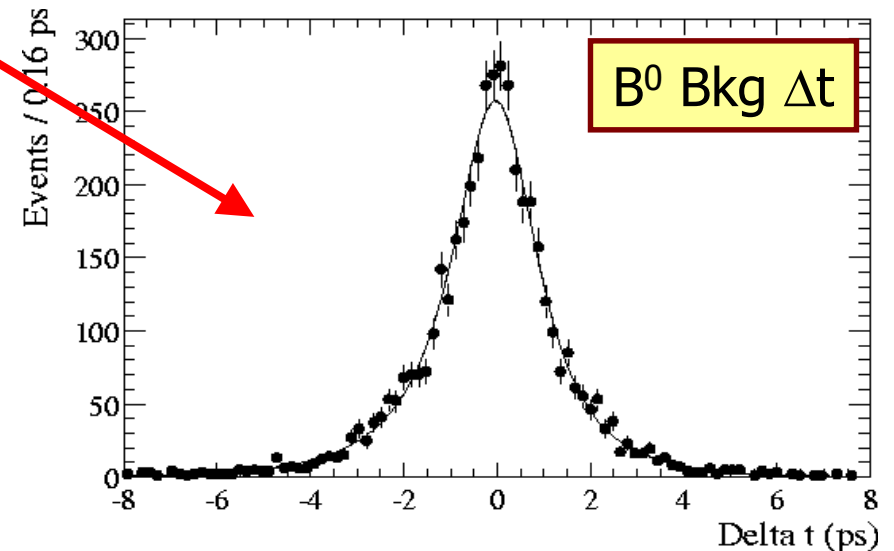
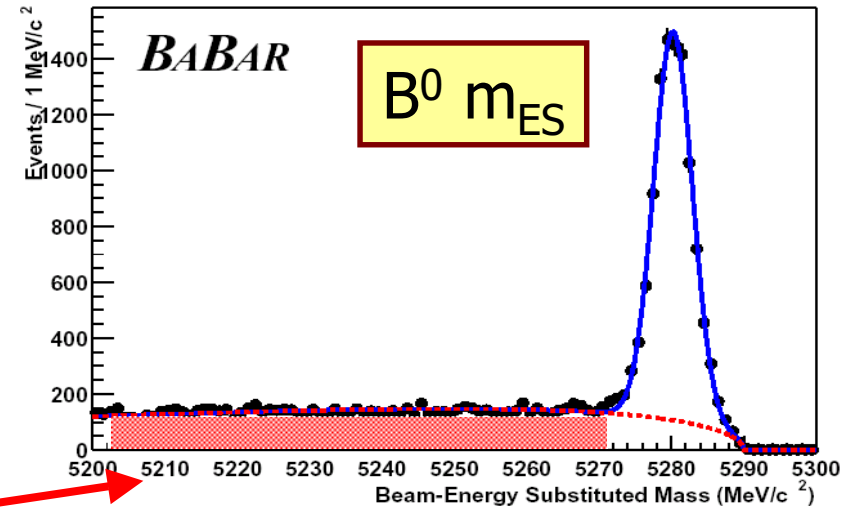
$$R = (1 - f_{tail} - f_{outlier})G(S\sigma_{\Delta t}, \mu_{core} = 0) + f_{tail}G(S\sigma_{\Delta t}, \mu = 0) \otimes \exp(-\Delta t / \sigma_{\Delta t} \tau_{bias}) + f_{outlier}G(\sigma_{outlier}, \mu_{outlier})$$

tracks from long-lived D's  
in tag vertex  
**asymmetric Resolution Function**

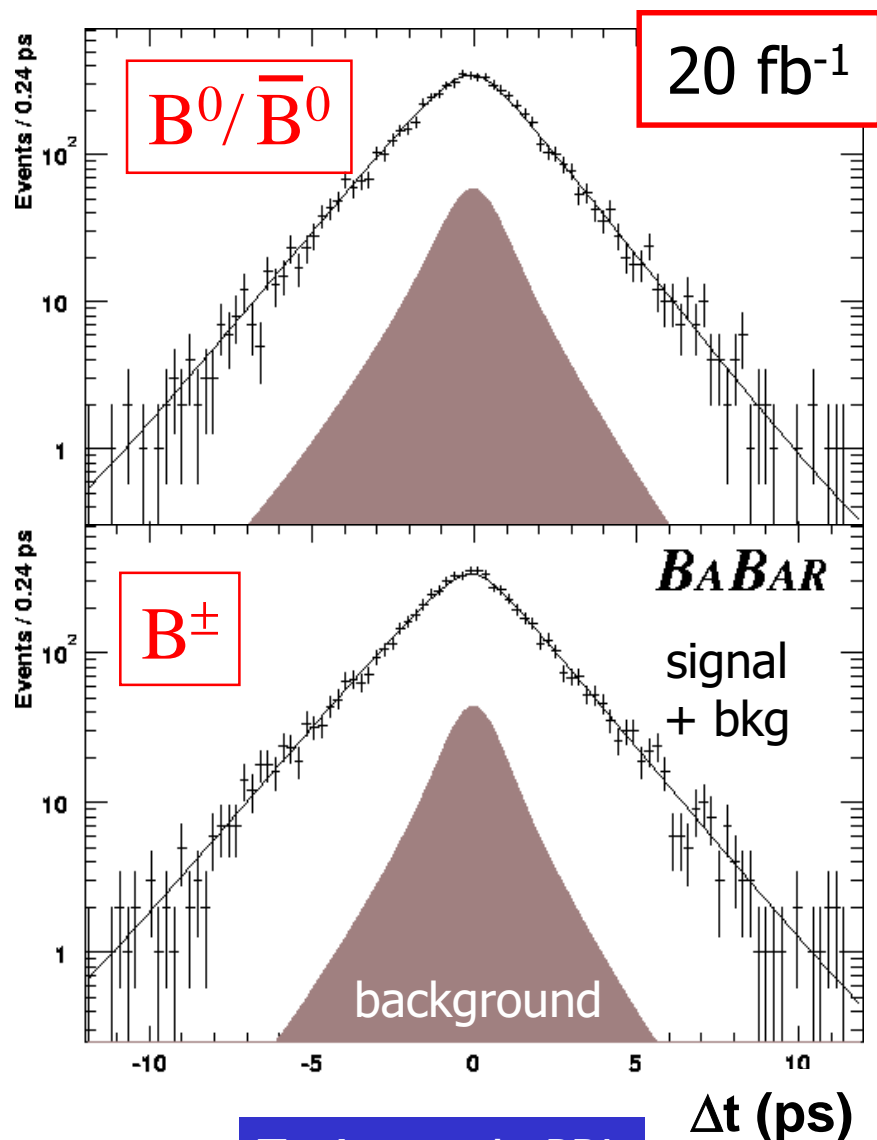


# B Lifetime Likelihood Fit

- Simultaneous unbinned maximum likelihood fit to  $B^0/B^+$  samples
- Use data to extract the properties of background events
  - Mass distribution provides the signal probability
  - Use the events in the **sideband** ( $m_{ES} < 5.27$ ) to determine the  $\Delta t$  structure of the background events under the signal peak
- 19 free parameters
  - $\tau(B^+)$  and  $\tau(B^0)$  2
  - $\Delta t$  signal resolution 5
  - empirical background description 12



# B Lifetime Results: Calibrating The BaBar Clock

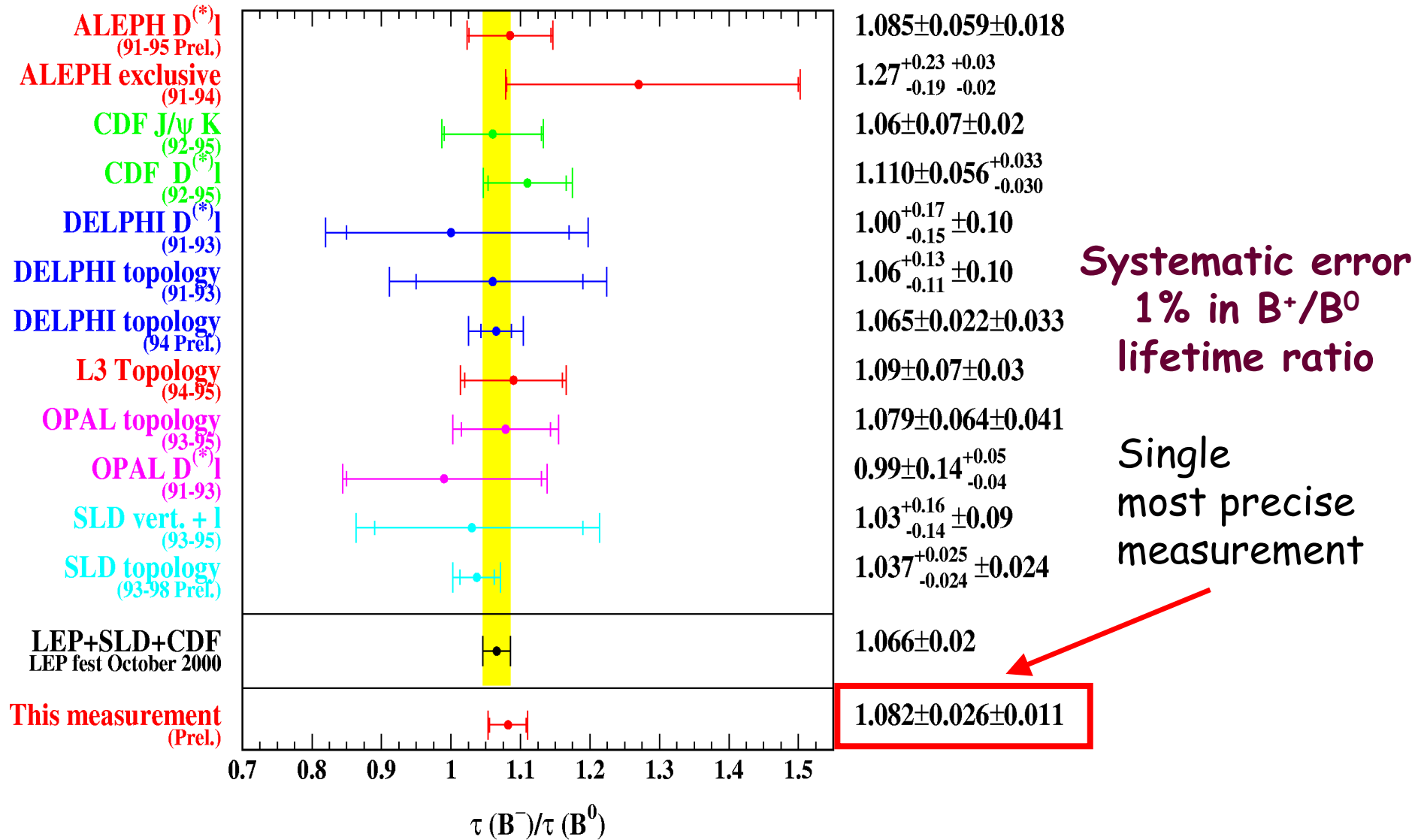


To Appear in PRL

$\tau_0 = 1.546 \pm 0.032 \pm 0.022 \text{ ps}$   
 PDG:  $1.548 \pm 0.032 \text{ ps}$   
 $\tau_{\pm} = 1.673 \pm 0.032 \pm 0.022 \text{ ps}$   
 PDG:  $1.653 \pm 0.028 \text{ ps}$   
 $\tau_{\pm}/\tau_0 = 1.082 \pm 0.026 \pm 0.011$   
 PDG:  $1.062 \pm 0.029$

- Precision measurement !
  - 2 % statistical error
  - 1.5% systematic error
- Main source of systematic error
  - Parameterization of the  $\Delta t$  resolution function
  - Description of events with large measured  $\Delta t$  (outliers)

# Comparison of Lifetime Ratio Measurements



# Sin2 $\beta$ Analysis Strategy (Part II)

## Measurements

## Analysis Ingredient

=  $B^+/B^0$  Lifetimes

(a) Reconstruction of  $B$  mesons in flavor eigenstates



(b)  $B$  vertex reconstruction

•  $B^0\overline{B^0}$ -Mixing

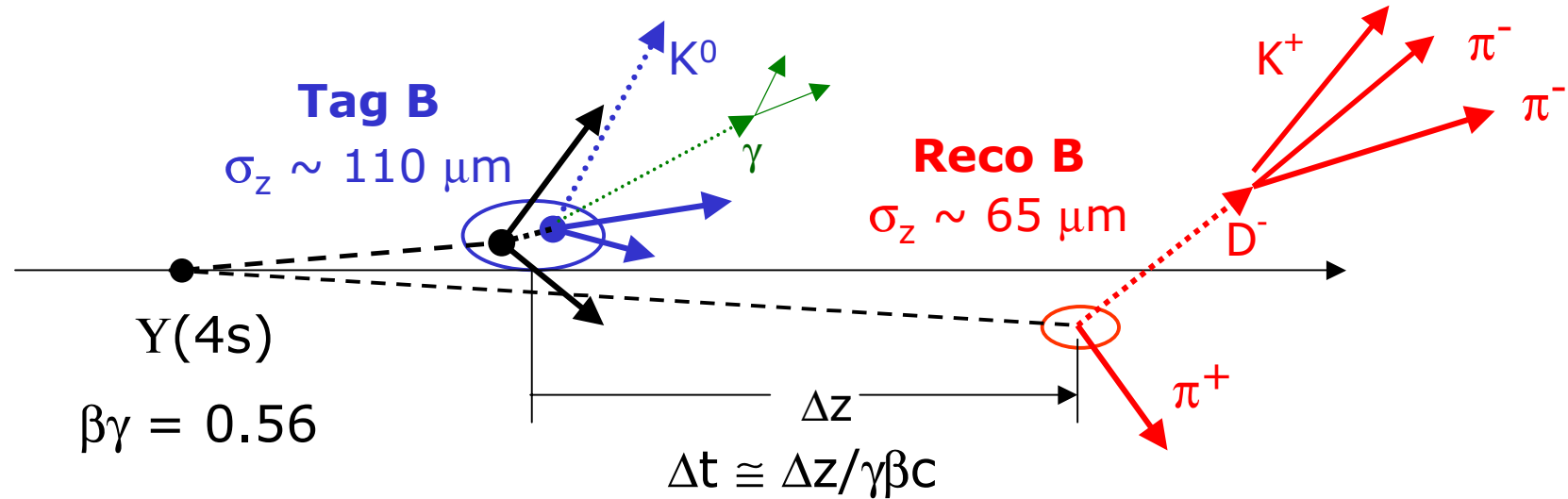
(c)  $B$  Flavor Tagging (+ a + b)

= CP-Asymmetries

= Reconstruction of neutral  $B$  mesons in CP eigenstates (+ a + b + c)



# $B^0\bar{B}^0$ Mixing with Fully Reconstructed B Mesons



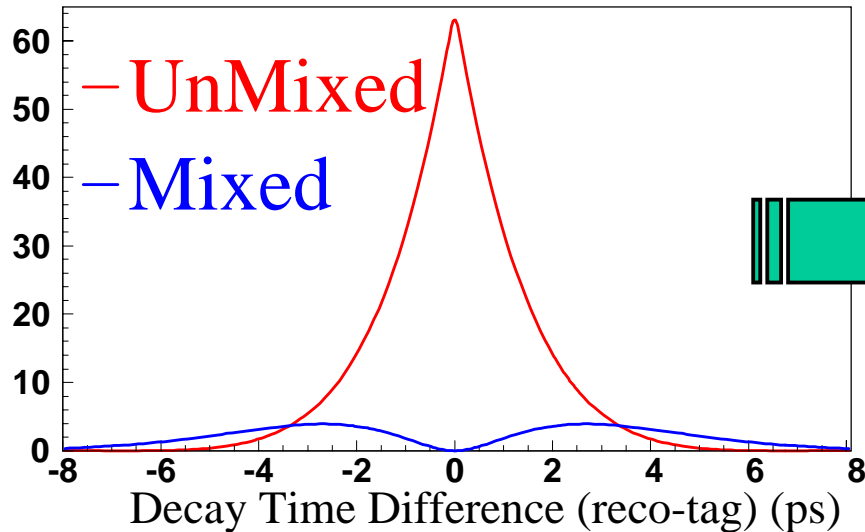
- 3. Reconstruct Inclusively the vertex of the "other" B meson ( $B_{\text{TAG}}$ ) ✓
- 4. Determine the flavor of  $B_{\text{TAG}}$  to separate Mixed and Unmixed events

- 1. Fully reconstruct one B meson in flavor eigenstate ( $B_{\text{REC}}$ ) ✓
- 2. Reconstruct the decay vertex ✓

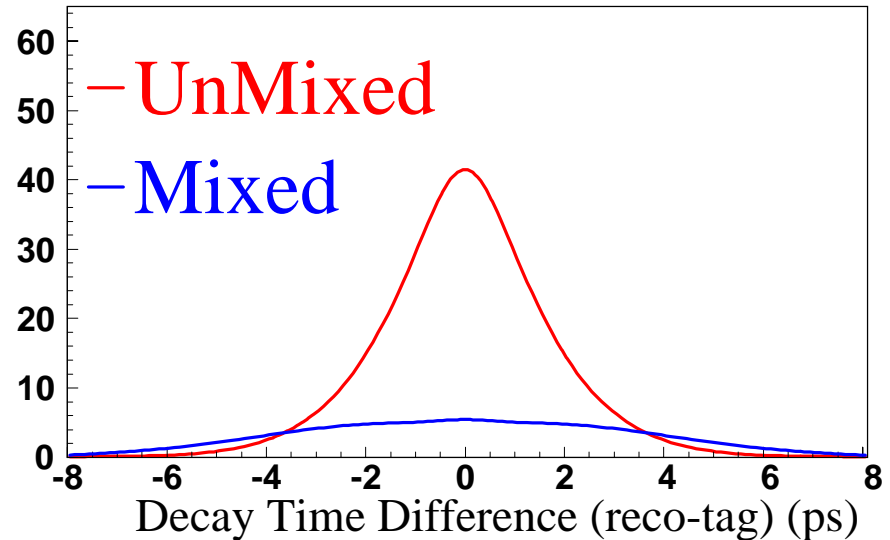
- 5. compute the proper time difference  $\Delta t$  ✓
- 6. Fit the  $\Delta t$  spectra of mixed and unmixed events

# $\Delta t$ Spectrum of Mixed and Unmixed B Events

**perfect**  
flavor tagging & time resolution



**realistic**  
mis-tagging & finite time resolution



$$f_{\text{Unmix}}^{\text{Mix}}(\Delta t) = \left\{ \frac{e^{-|\Delta t|/\tau_{B_d}}}{4\tau_{B_d}} \times \left( 1 \pm (1-2w) \cos(\Delta m_d \Delta t) \right) \right\} \otimes \text{ResolutionFunction}$$

w: the fraction of wrongly tagged events

$\Delta m_d$ : oscillation frequency

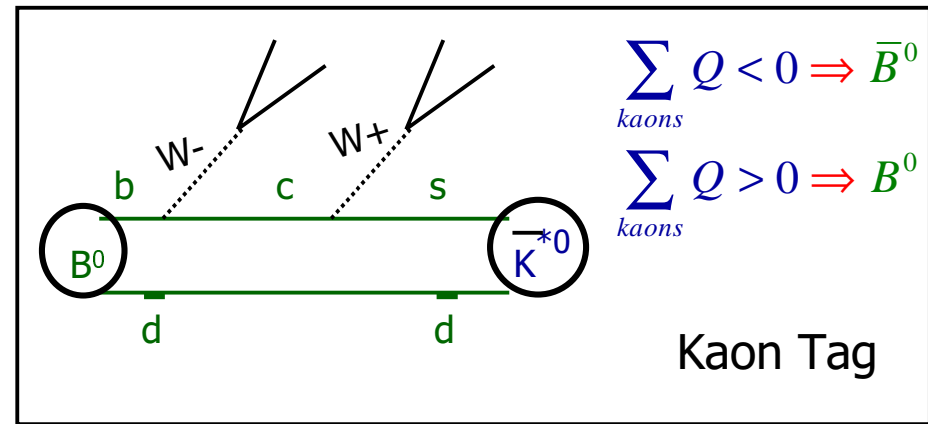
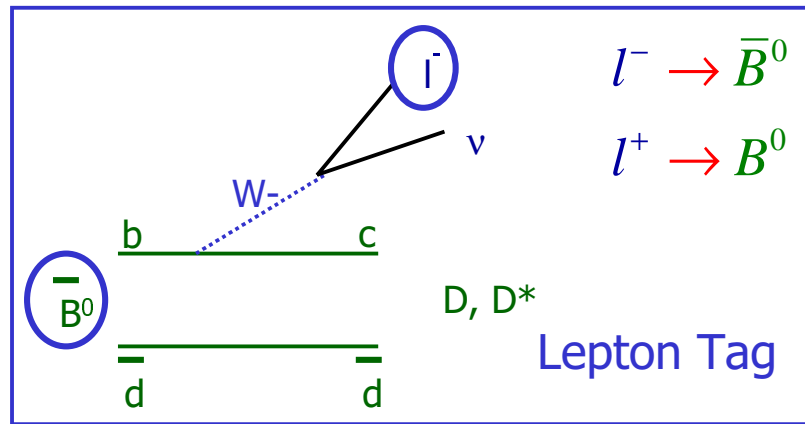
Unmixed:  $B_{flav}^0 \bar{B}_{tag}^0$  or  $\bar{B}_{flav}^0 B_{tag}^0$

Mixed:  $B_{flav}^0 B_{tag}^0$  or  $\bar{B}_{flav}^0 \bar{B}_{tag}^0$

# B Flavor Tagging Methods

## Hierarchical Tagging Categories

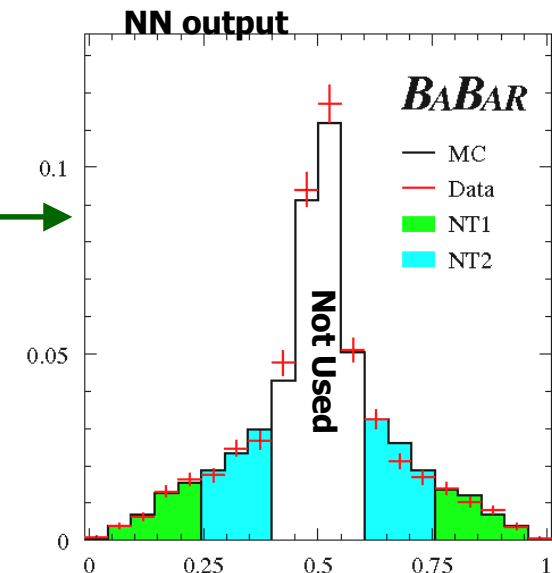
For electrons, muons and Kaons use the charge correlation



Multivariate analysis exploiting the other kinematic information of the event, e.g.,

- Momentum spectrum of the charged particles
  - Information from non-identified leptons and kaons
  - Soft  $\pi$  from  $D^*$  decay
- Neural Network

Each category is characterized by the probability of giving the wrong answer (mistag fraction  $w$ )



# B Flavor Tagging Performance Using B Mixing

The large sample of fully reconstructed hadronic B decays provides the precise determination of the tagging parameters required in the CP fit

Tagging category	Fraction of tagged events $\varepsilon$ (%)	Wrong tag fraction $w$ (%)	$Q = \varepsilon (1-2w)^2$ (%)
Lepton	$10.9 \pm 0.3$	<b><math>8.9 \pm 1.3</math></b>	$7.4 \pm 0.5$
Kaon	<b><math>35.8 \pm 0.5</math></b>	$17.6 \pm 1.0$	$15.0 \pm 0.9$
NT1	$7.8 \pm 0.3$	$22.0 \pm 2.1$	$2.5 \pm 0.4$
NT2	$13.8 \pm 0.3$	$35.1 \pm 1.9$	$1.2 \pm 0.3$
ALL	<b><math>68.4 \pm 0.7</math></b>		<b><math>26.1 \pm 1.2</math></b>

Highest "efficiency"

The error on  $\sin 2\beta$  the quality factor  $Q$

$$\sigma(\sin 2\beta) \propto \frac{1}{\sqrt{Q}}$$

Smallest mistag fraction

# $\Delta t$ Resolution Function

$$R(\delta\Delta t) = (1 - f_{tail} - f_{outl}) \cdot G_{core}(\delta\Delta t, S_{core}, \delta_{core,i}) \quad \leftarrow \text{Core}$$

$$+ f_{tail} \cdot G_{tail}(\delta\Delta t, S_{tail}, \delta_{tail}) \quad \leftarrow \text{Tail}$$

$$+ f_{outl} \cdot G_{outl}(\delta\Delta t, \sigma_{outl} = 8 \text{ ps}, \delta_{outl} = 0) \quad \leftarrow \text{Outlier}$$

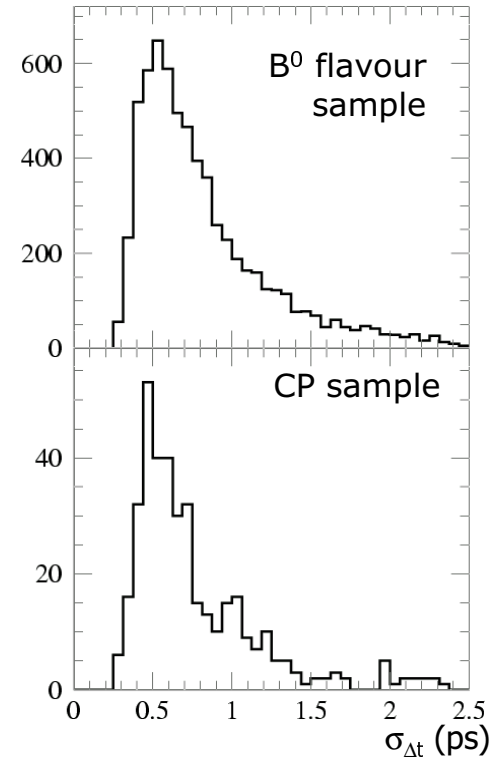
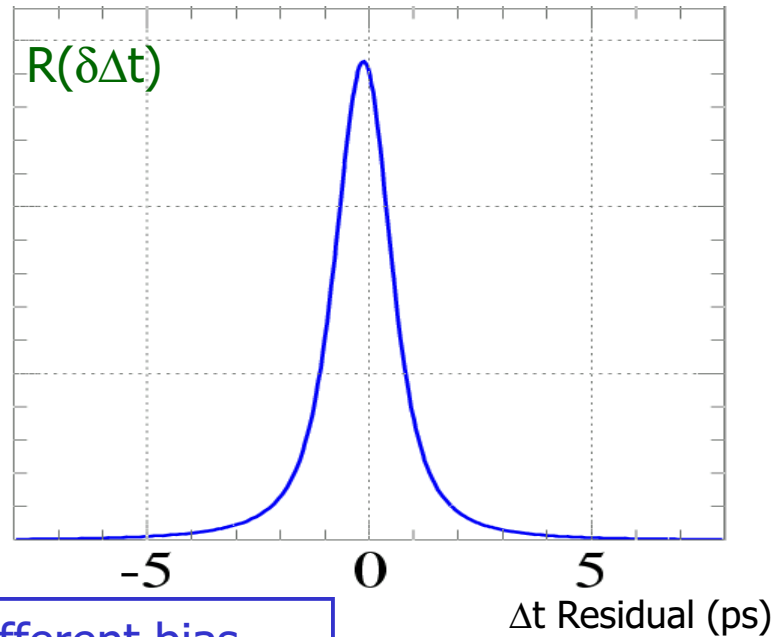
$$\sigma_{core} = S_{core} \cdot \sigma_{\Delta t}^{evt}$$

$$\sigma_{tail} = S_{tail} \cdot \sigma_{\Delta t}^{evt}$$

**Use the event-by-event uncertainty on  $\Delta t$**

Parameter
$S_{Core}$
$S_{Tail}$
$f_{Tail}$ (%)
$f_{Outlier}$ (%)
$\delta_{Core,Lepton}$ (ps)
$\delta_{Core,Kaon}$ (ps)
$\delta_{Core,NT1}$ (ps)
$\delta_{Core,NT2}$ (ps)
$\delta_{Tail}$ (ps)

Different bias  
For each tagging  
category



# Mixing Likelihood Fit

Unbinned maximum likelihood fit to flavor-tagged neutral B sample

$$f_{\text{Unmix}}^{\text{Mix}}(\Delta t) = \left\{ \frac{e^{-|\Delta t|/\tau_{B_d}}}{4\tau_{B_d}} \times \left( 1 \pm (1-2w) \cos(\Delta m_d \Delta t) \right) \right\} \otimes R$$

## Fit Parameters

$\Delta m_d$

Mistag fractions for  $B^0$  and  $\bar{B}^0$  tags

Signal resolution function(scale factor,bias,fractions)

Empirical description of background  $\Delta t$

B lifetime fixed to the PDG value

1

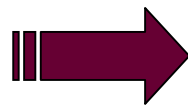
8

9

16

$\tau_B = 1.548$  ps

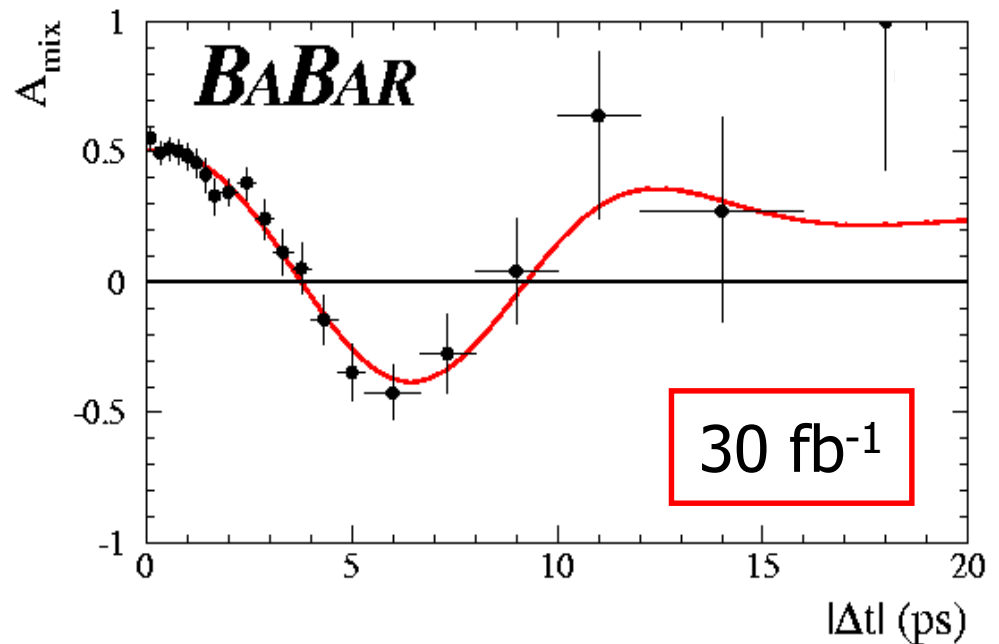
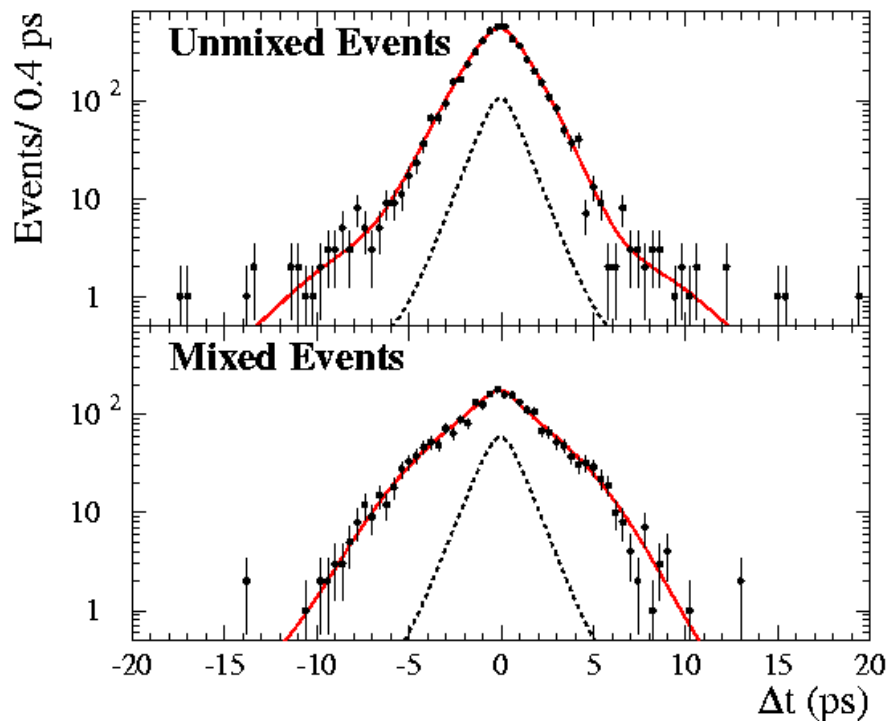
34 total free parameters



All  $\Delta t$  parameters extracted from data

# $B^0\bar{B}^0$ Mixing Fit Result

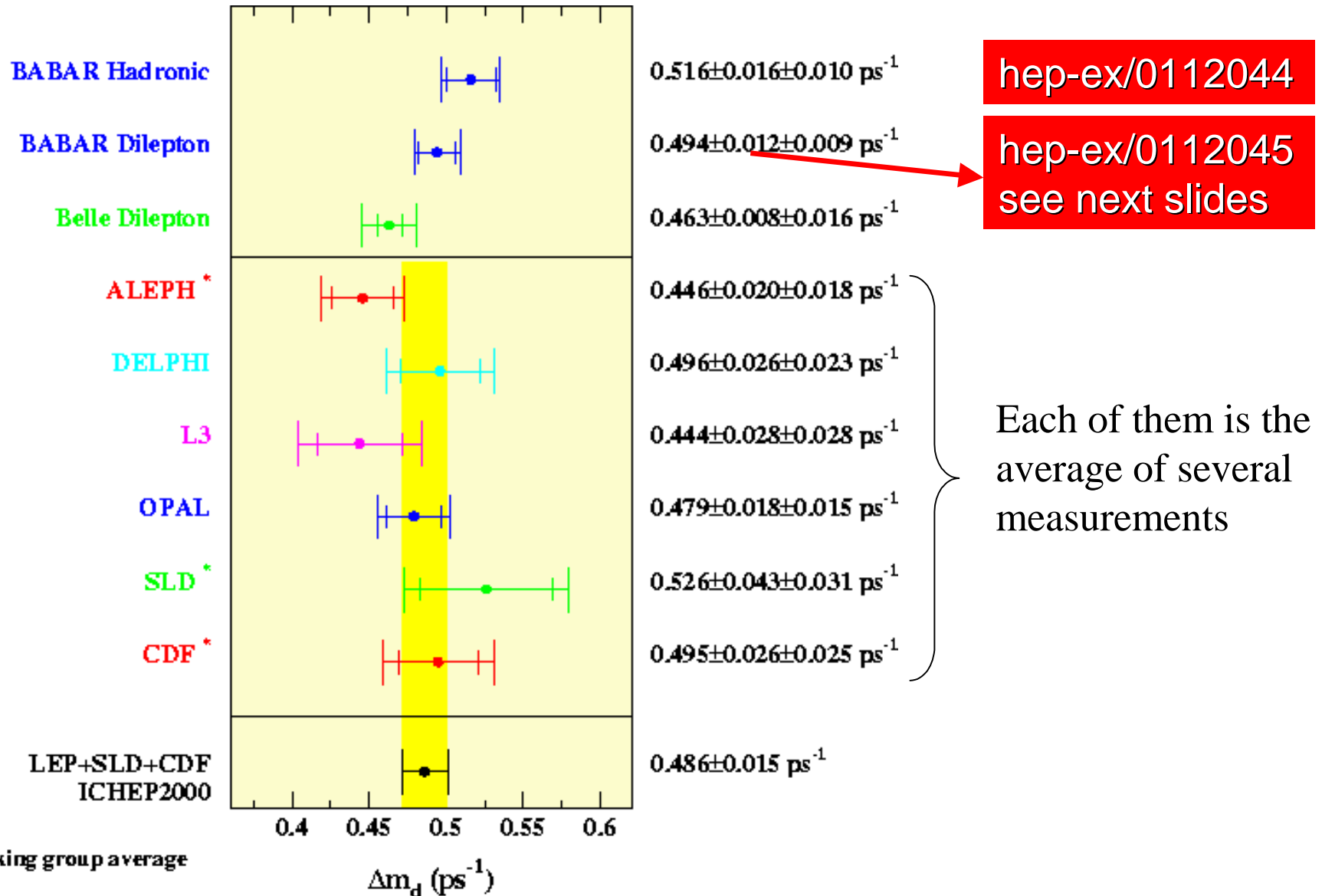
$$\text{Asymmetry}(\Delta t) = \frac{N(\text{unmixed}) - N(\text{mixed})}{N(\text{unmixed}) + N(\text{mixed})} \approx (1 - 2w) \times \cos(\Delta m_d \Delta t)$$



$$\Delta m_d = 0.516 \pm 0.016 (\text{stat}) \pm 0.010 (\text{syst}) \text{ ns}^{-1}$$

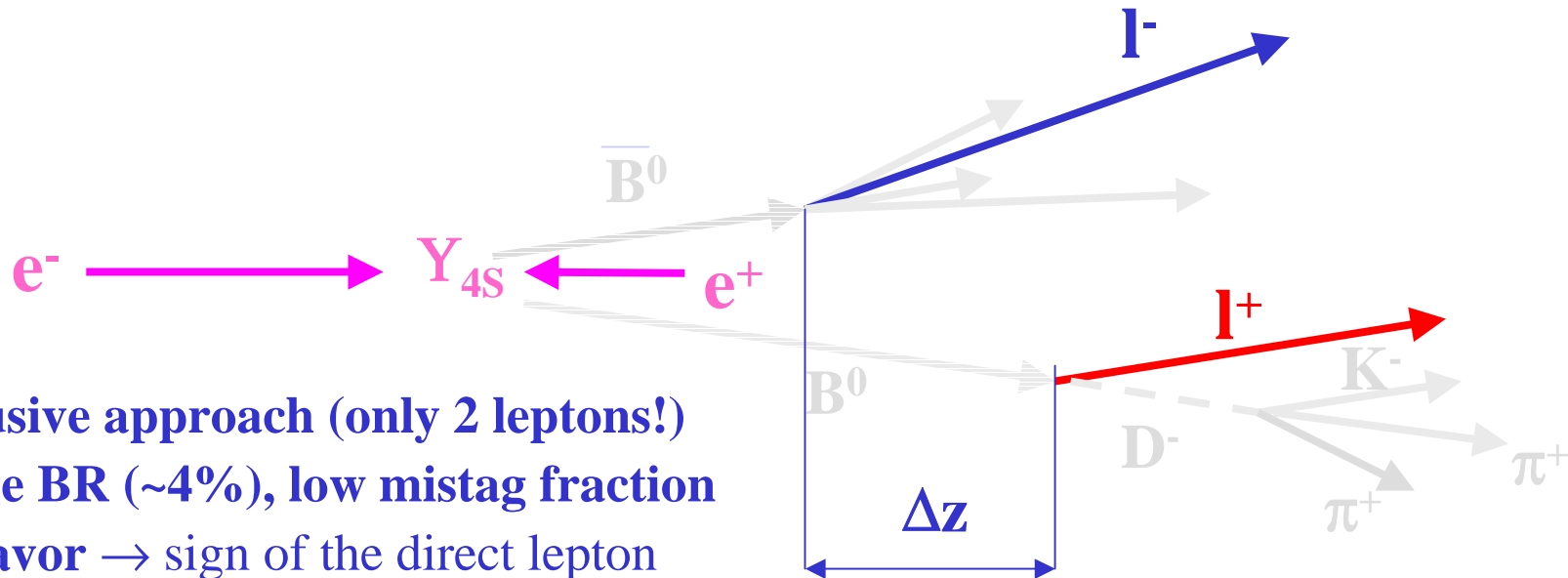
hep-ex/0112044

# $\Delta m_d$ Measurements in Comparison





# The Dilepton Way to mixing and CPV

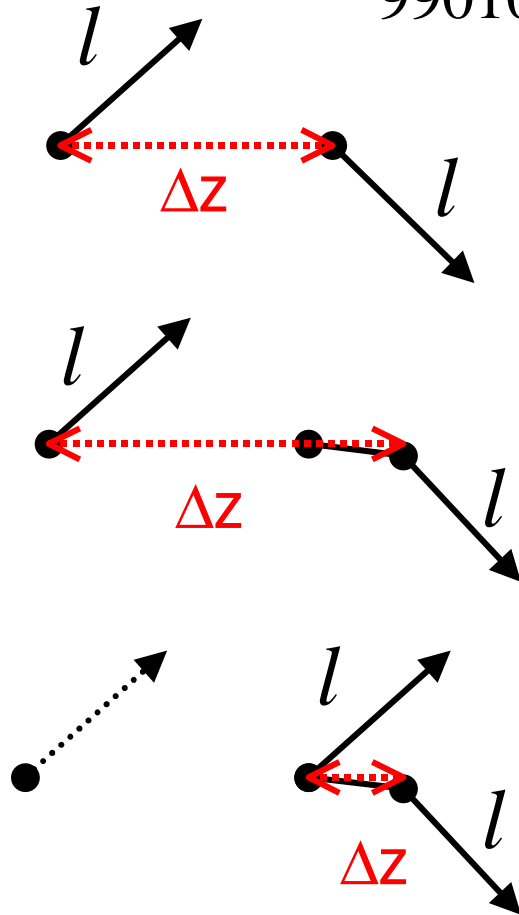


- Inclusive approach (only 2 leptons!)
- Large BR ( $\sim 4\%$ ), low mistag fraction
- B Flavor  $\rightarrow$  sign of the direct lepton
- $B^0$  and  $B^\pm$  admixture
- Efficient Neural Network event selection
- Very accurate description of the residual background
- $\Delta z \rightarrow$  points of closest approach of the leptons to the beam spot in transverse plane
- Extraction of  $\Delta m$  from time evolution:  $e^{-\Gamma|\Delta t|} [1 \pm \cos(\Delta m \Delta t)]$
- Study of CPV in mixing from charge asymmetry of same sign leptons:

$$A_T = (N_{l^+l^+} - N_{l^-l^-}) / (N_{l^+l^+} + N_{l^-l^-}) \sim 4\text{Re}(\epsilon) / (1 + |\epsilon|^2)$$

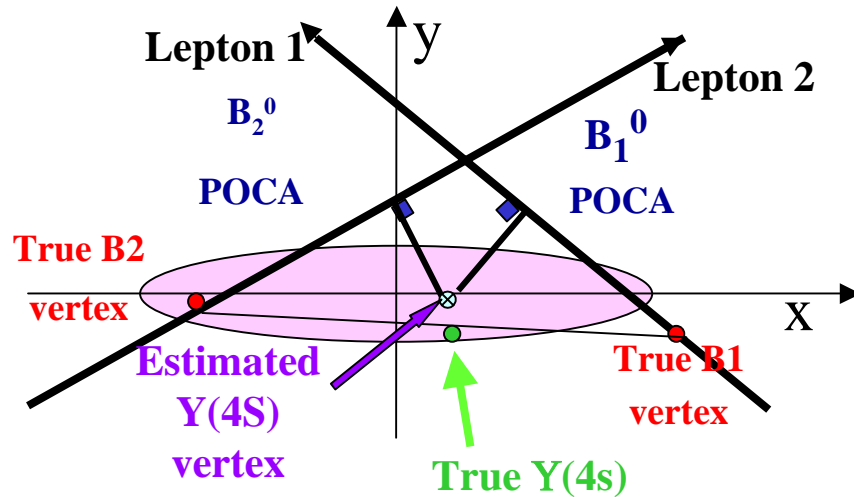
# Dileptons: sample composition

99010 events selected in  $20.7 \text{ fb}^{-1}$



- Direct leptons ( $\sim 78\%$ )
  - sensitive to mixing (!)
  - B-lifetime component
- Opposite-B cascade (OBC) leptons ( $\sim 7\%$ )
  - sensitive to mixing, but
  - source of mistag ( $\sim 100\%$ )
  - extra-lifetime due to charm decay (B-lifetime + effective lifetime from charm)
- Same-B cascade (SBC) leptons ( $\sim 5\%$ )
  - not sensitive to mixing
  - source of opposite-sign leptons only
  - effective lifetime from charm
- Misidentified leptons ( $\sim 5\%$ ):
  - same topologies (and resolution function) as above
  - extra mistag to be taken into account
- Continuum ( $\sim 5\%$ ): fit off-resonance data

# Dilepton Mixing: $\Delta t$ measurement

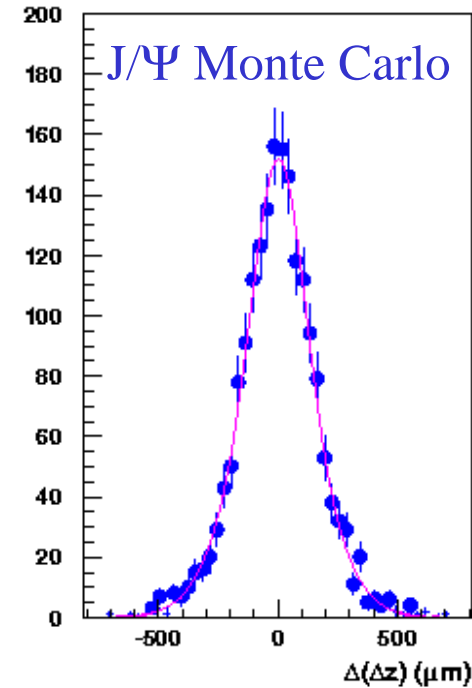
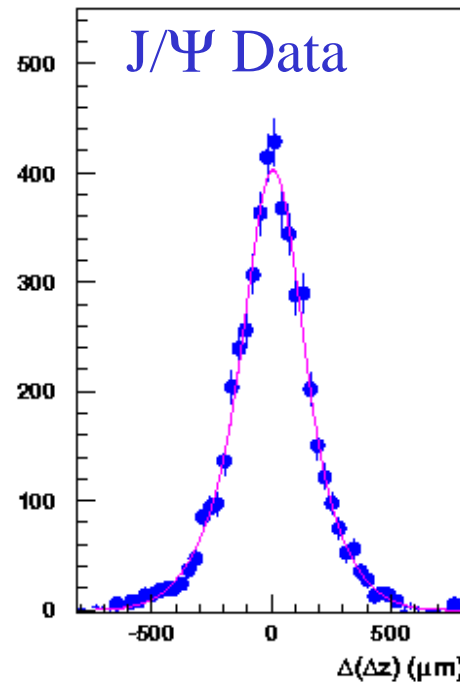


$\Delta z = z$  difference of the point of closest approach (POCA) of the tracks to a  $Y(4S)$  vertex, estimated with the 2 leptons and a beam spot constraint

Agreement within 10%

- $\Delta z$  resolution function determined with MC and cross-checked with  $J/\Psi$ .
- Resolution model: 3 gaussians
  - Narrow Gaussian :  $85\mu\text{m}$  (64.8%)
  - Wide Gaussian :  $160\mu\text{m}$  (35.5%)
  - Outlier Gaussian :  $630\mu\text{m}$  (0.7%)
- Boost approximation:

$$\Delta t = \Delta z / (c \langle \beta \gamma \rangle)$$



# Dilepton mixing results

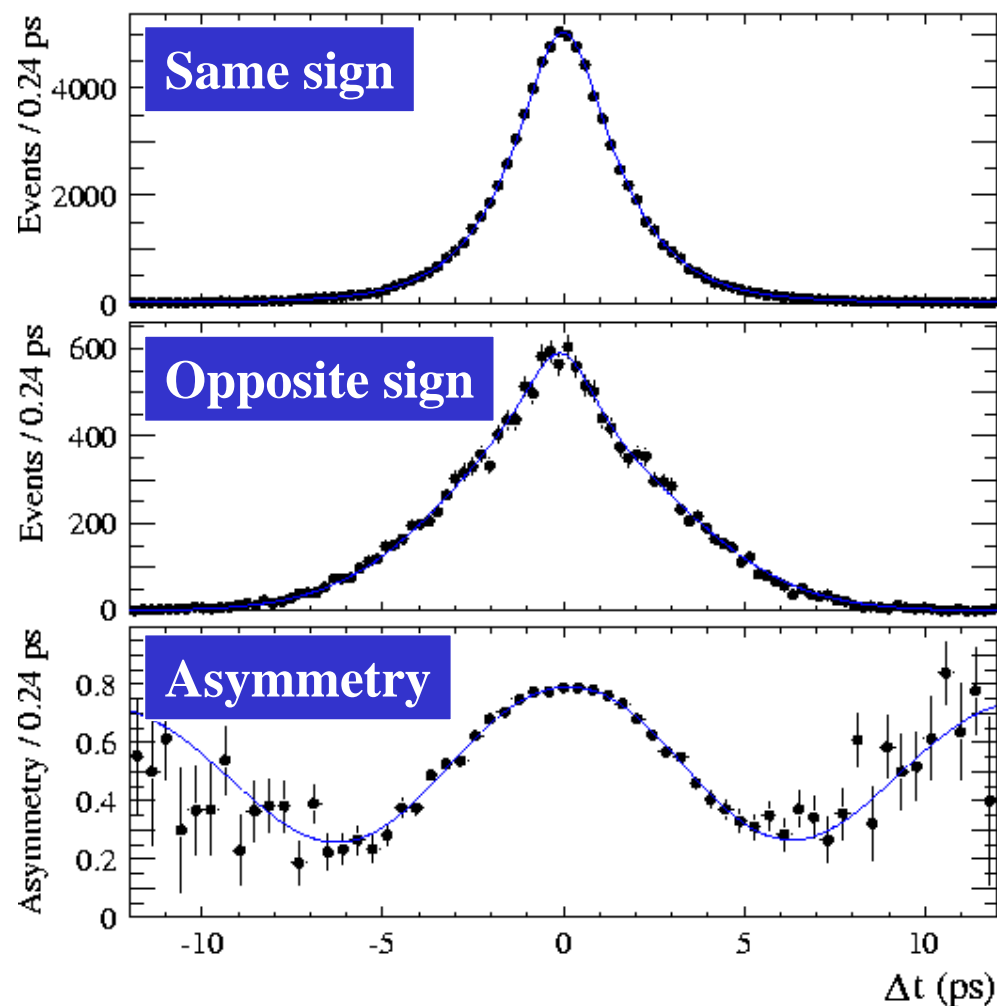
$$\Delta m_d = 0.493 \pm 0.012 \pm 0.009 \text{ ps}^{-1}$$

Most precise single measurement!

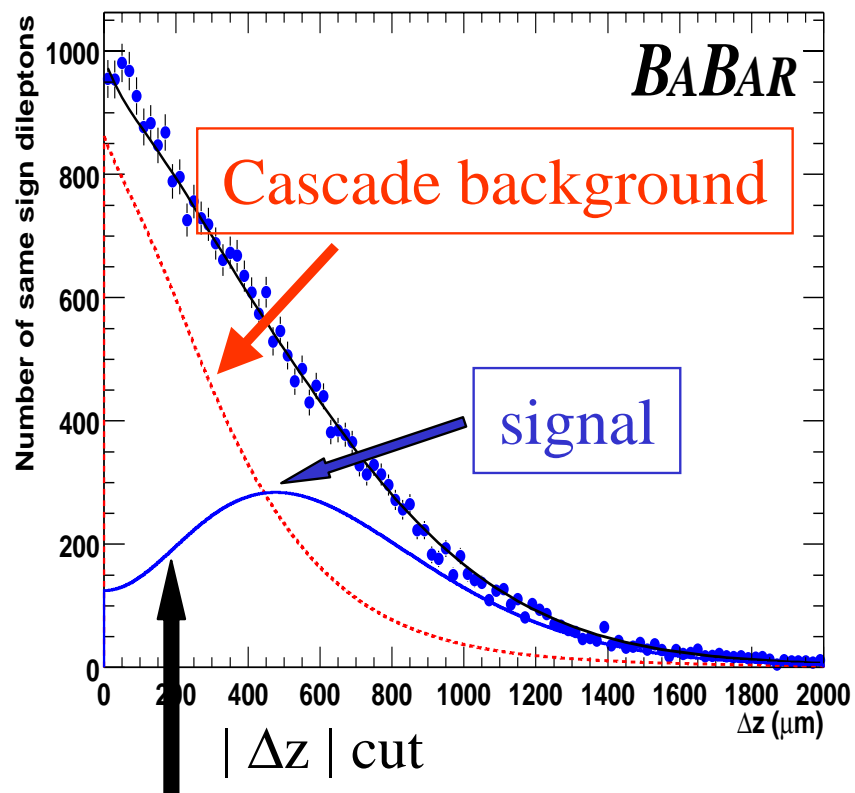
1% correction due to the time dependence of the resolution function

Systematics dominated by:

- B meson lifetimes (0.0064)
- time dependence of resolution function and cascade resolution + lifetimes (0.0050)



# CPV with dileptons: Background reduction



Almost all background comes from cascade leptons from  $B^+$  or unmixed  $B^0$

Cut at  $200 \mu\text{m}$

Correct for background dilution by weighting in bins of  $|\Delta z|$

$$A_T^{mes}(\Delta t) = A_T(\Delta t) \cdot \frac{S(\Delta t)}{S(\Delta t) + B(\Delta t)}$$

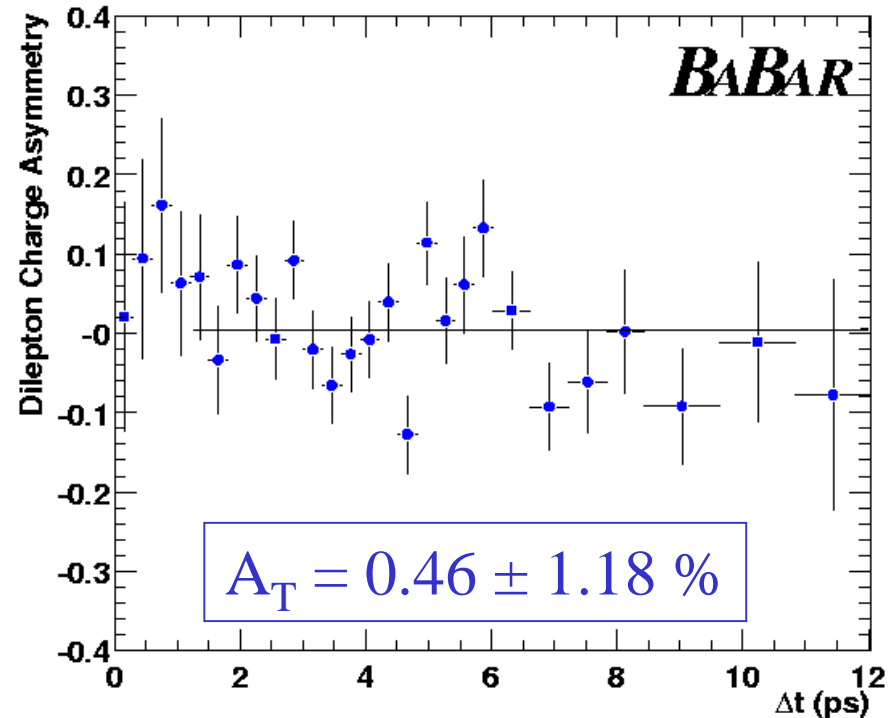
Neglect background asymmetry  $\Rightarrow$  small systematics

**20381 events in 20.7 fb<sup>-1</sup>**

# CPV with dileptons: results

Corrected for charge asymmetries in the detection (particle ID, tracking)

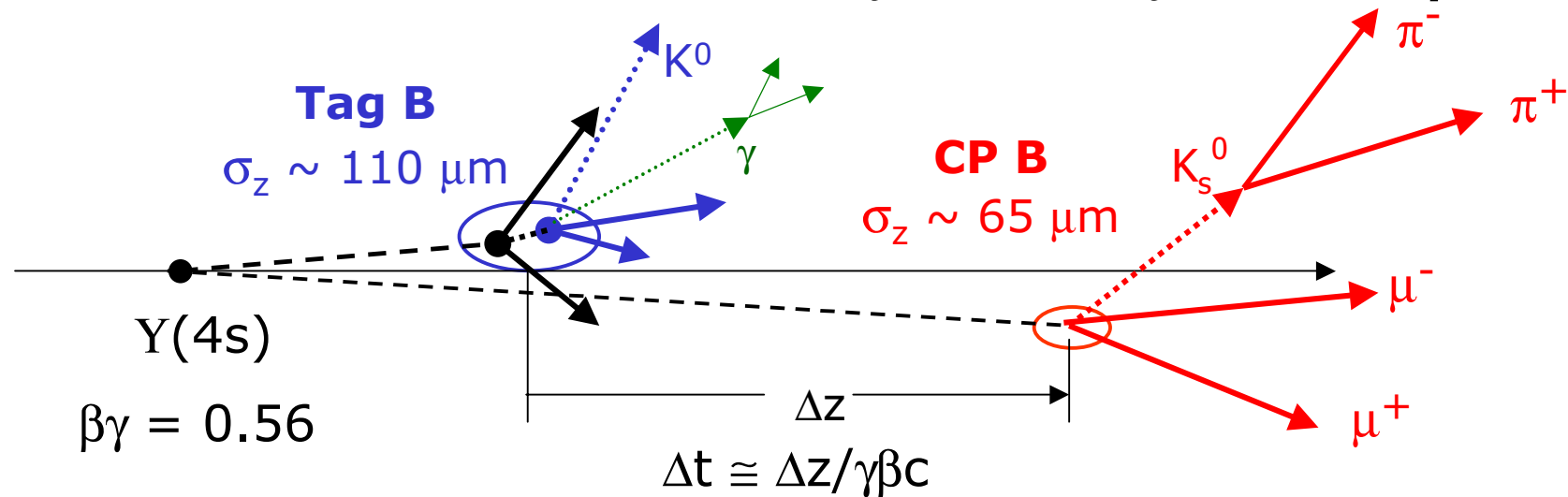
Most precise single measurement!



$$\frac{\text{Re}(\epsilon)}{1+|\epsilon|^2} = 0.11 \pm 0.29 \pm 0.36 \%, \text{ or}$$
$$|q/p| = 0.998 \pm 0.006 \pm 0.007$$

Systematics dominated by charge asymmetries in the detector

# Measurement of CP Asymmetry : $\text{Sin}2\beta$

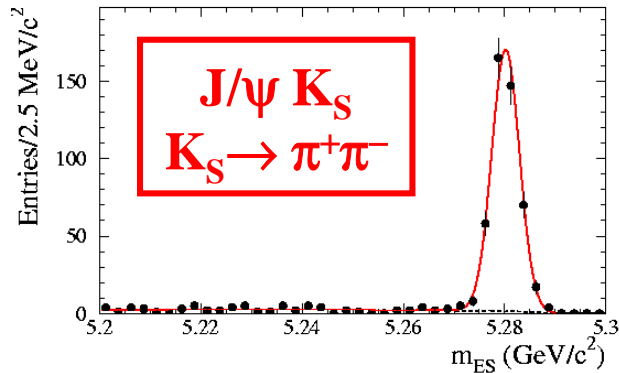


3. Reconstruct Inclusively the vertex of the "other" B meson ( $B_{\text{TAG}}$ ) ✓
4. Determine the flavor of  $B_{\text{TAG}}$  to separate Mixed and Unmixed events ✓

1. Fully reconstruct one B meson in CP eigenstate ( $B_{\text{CP}}$ )
2. Reconstruct the decay vertex ✓

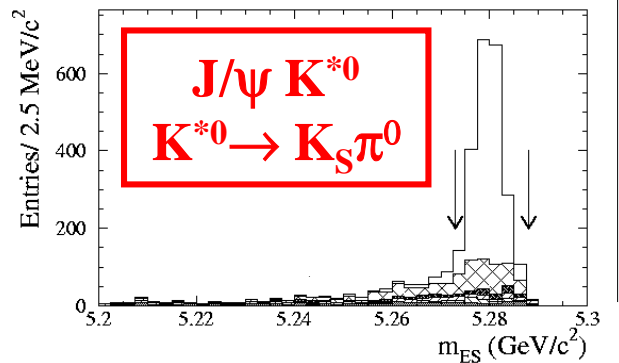
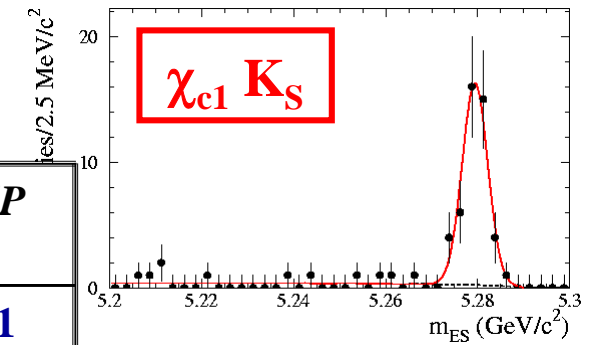
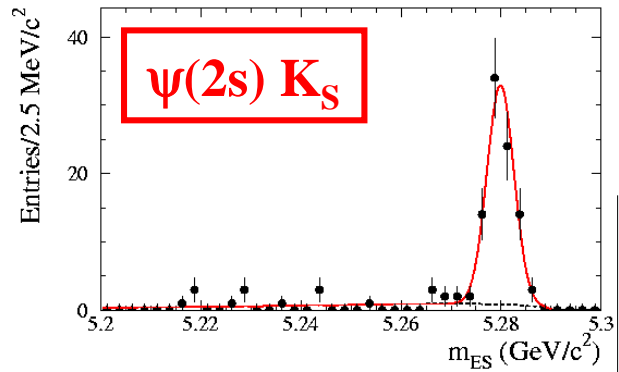
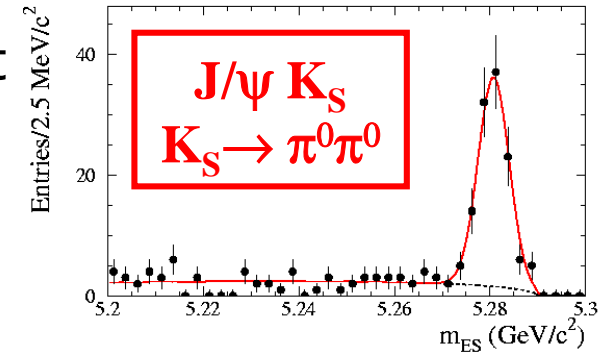
5. compute the proper time difference  $\Delta t$  ✓
6. Fit the  $\Delta t$  spectra of  $B^0$  and  $\bar{B}^0$  tagged events

# The fully Reconstructed CP Sample

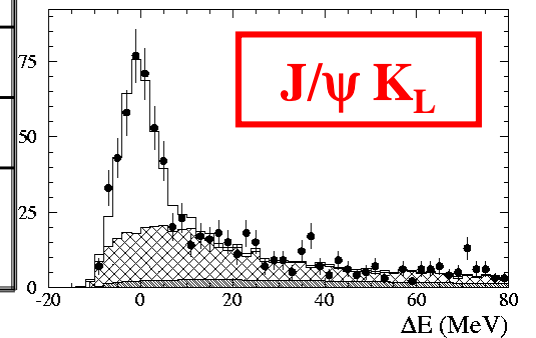


Before tagging requirement

**1999-2001 data**  
32 x 10<sup>6</sup> BB pairs  
29 fb<sup>-1</sup> on peak



Sample	tagged events	Purity	CP
[J/ψ, ψ(2S), χ <sub>c1</sub> ] K <sub>S</sub>	480	96%	-1
J/ψ K <sub>L</sub>	273	51%	+1
J/ψ K <sup>*0</sup> (K <sub>S</sub> π <sup>0</sup> )	50	74%	mixed
<b>Full CP sample</b>	<b>803</b>	<b>80%</b>	



After flavor tagging

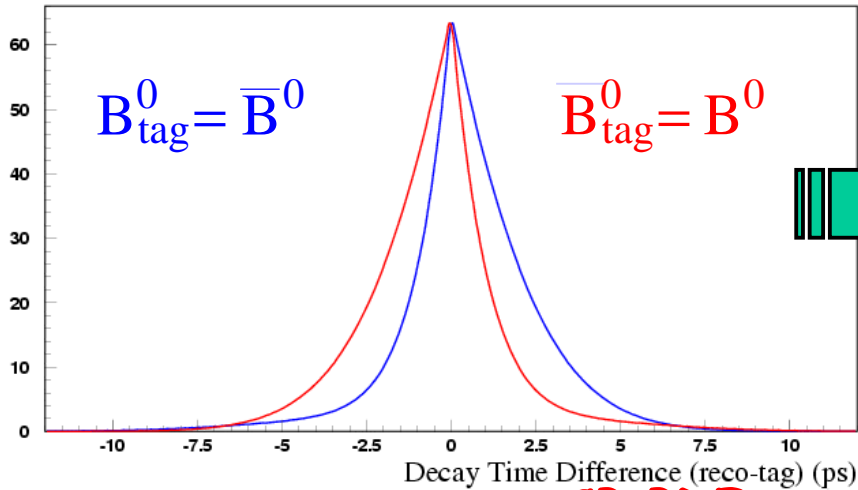
$$\Delta E = E_{J/\psi} + E_{K_L} - E_{beam}^{cm}$$

$$m_{ES} = \sqrt{(E_{beam}^{cm})^2 - (p_B^{cm})^2}$$

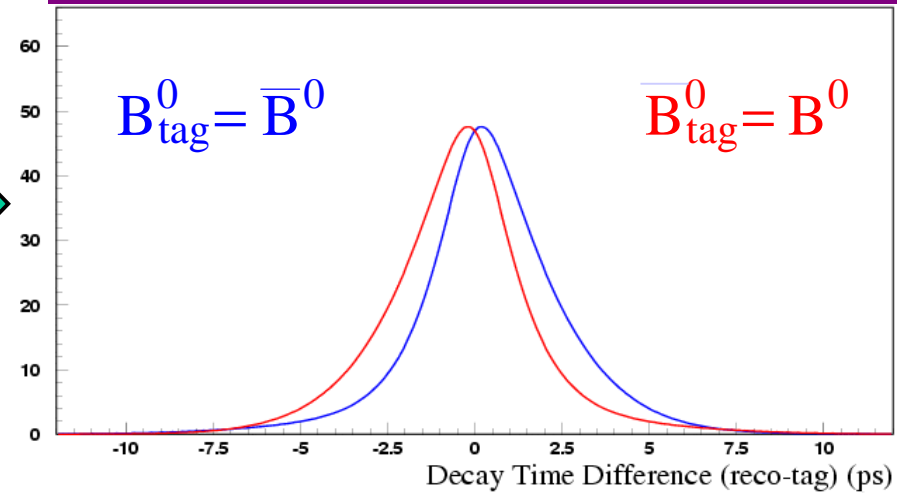


# $\Delta t$ Spectrum of CP Events

**perfect**  
flavor tagging & time resolution



**realistic**  
mis-tagging & finite time resolution



**CP PDF**

Mistag fractions  $w$   
And  
Resolution function  $R$

$$f_{CP,\pm}(\Delta t) = \left\{ \frac{e^{-|\Delta t|/\tau_{B_d}}}{4 \tau_{B_d}} \times \left( 1 \mp \eta_f \sin 2\beta (1 - 2w) \sin(\Delta m_d \Delta t) \right) \right\} \otimes R$$

determined from the  
flavor sample

**Mixing PDF**

$$f_{mixing,\pm}(\Delta t) = \left\{ \frac{e^{-|\Delta t|/\tau_{B_d}}}{4 \tau_{B_d}} \times \left( 1 \pm (1 - 2w) \cos(\Delta m_d \Delta t) \right) \right\} \otimes R$$

# Sin2 $\beta$ Likelihood Fit

Combined unbinned maximum likelihood fit to  $\Delta t$  spectra of flavor and CP sample

## Fit Parameters

Sin2 $\beta$

Mistag fractions for  $B^0$  and  $\bar{B}^0$  tags in each Cat.

Signal resolution function

Empirical description of background  $\Delta t$

B lifetime fixed to the PDG value

Mixing Frequency fixed to the PDG value

1 tagged CP samples

8 } tagged flavor sample

16

20

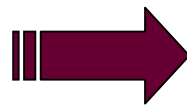
$\tau_B = 1.548$  ps

$\Delta m_d = 0.472$  ps<sup>-1</sup>

Global correlation coefficient for sin2 $\beta$ : 13%

Different  $\Delta t$  resolution function parameters for Run1 and Run2

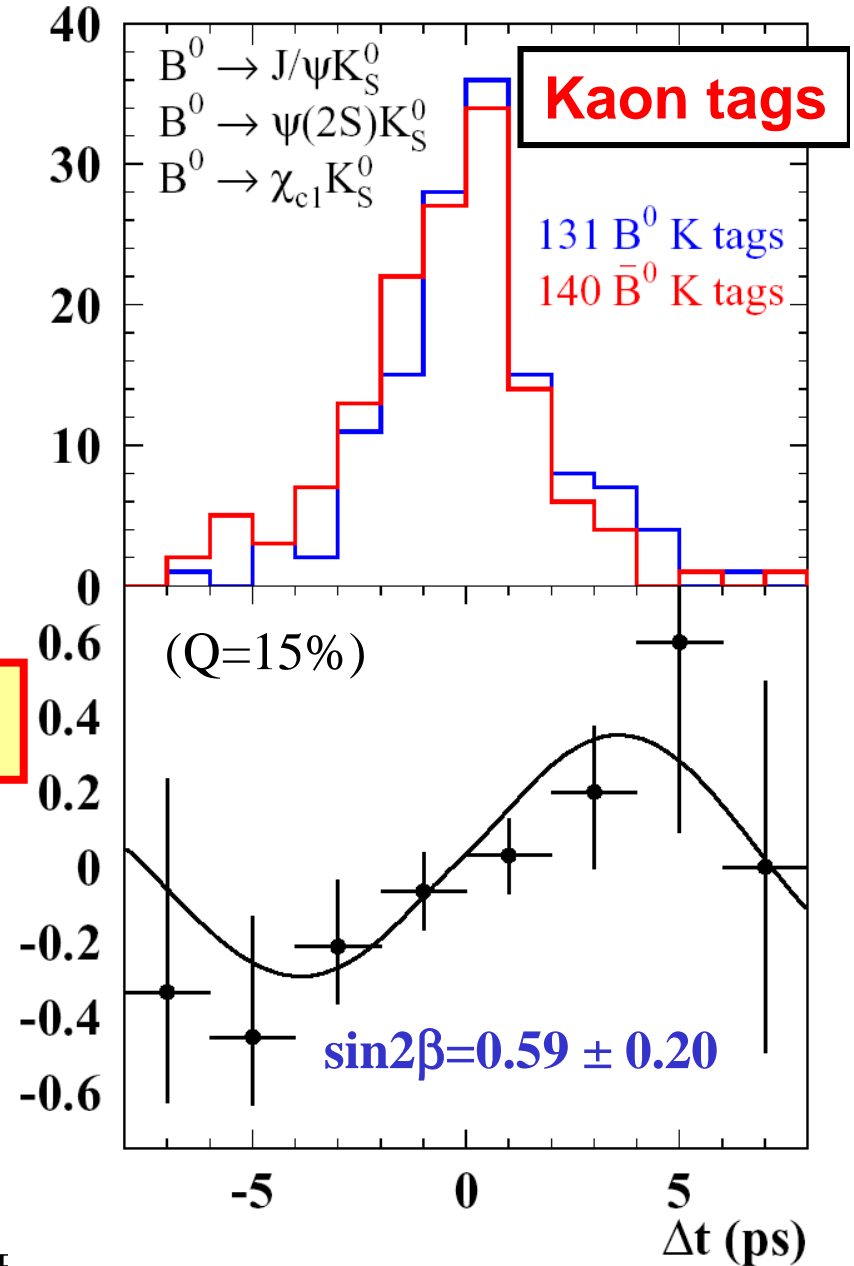
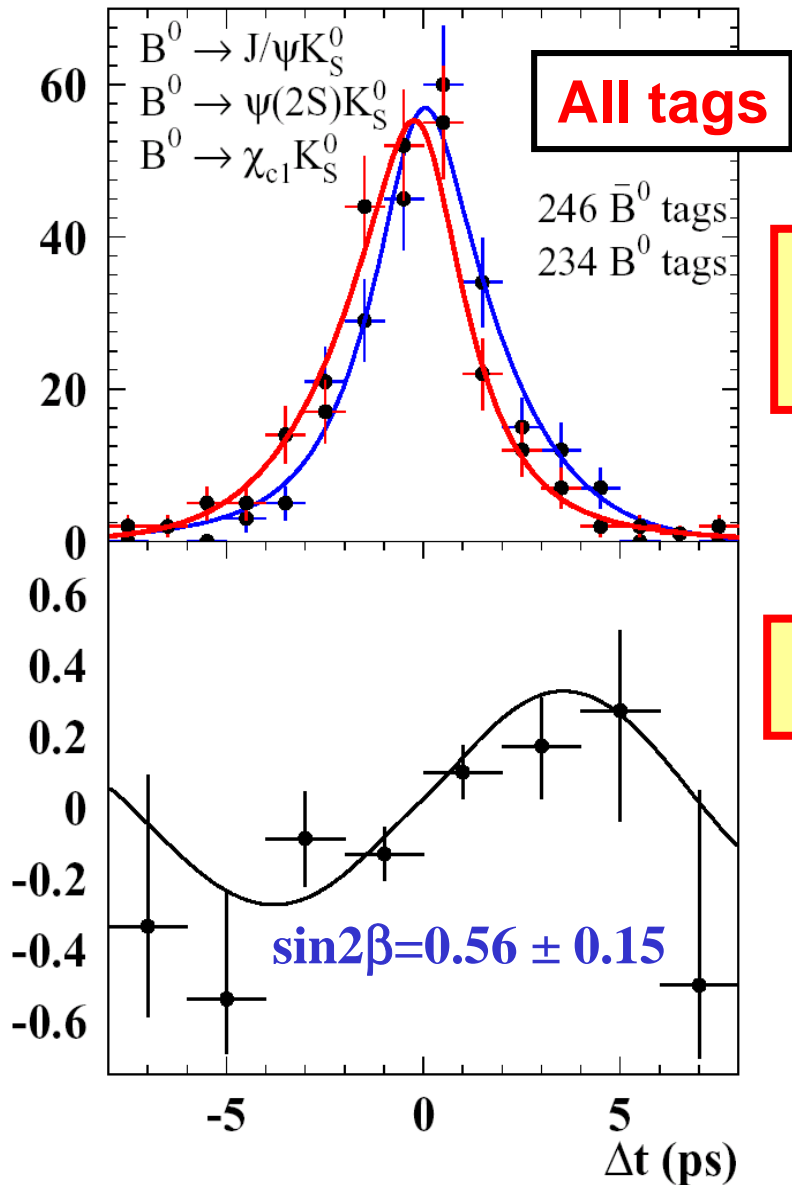
45 total free parameters



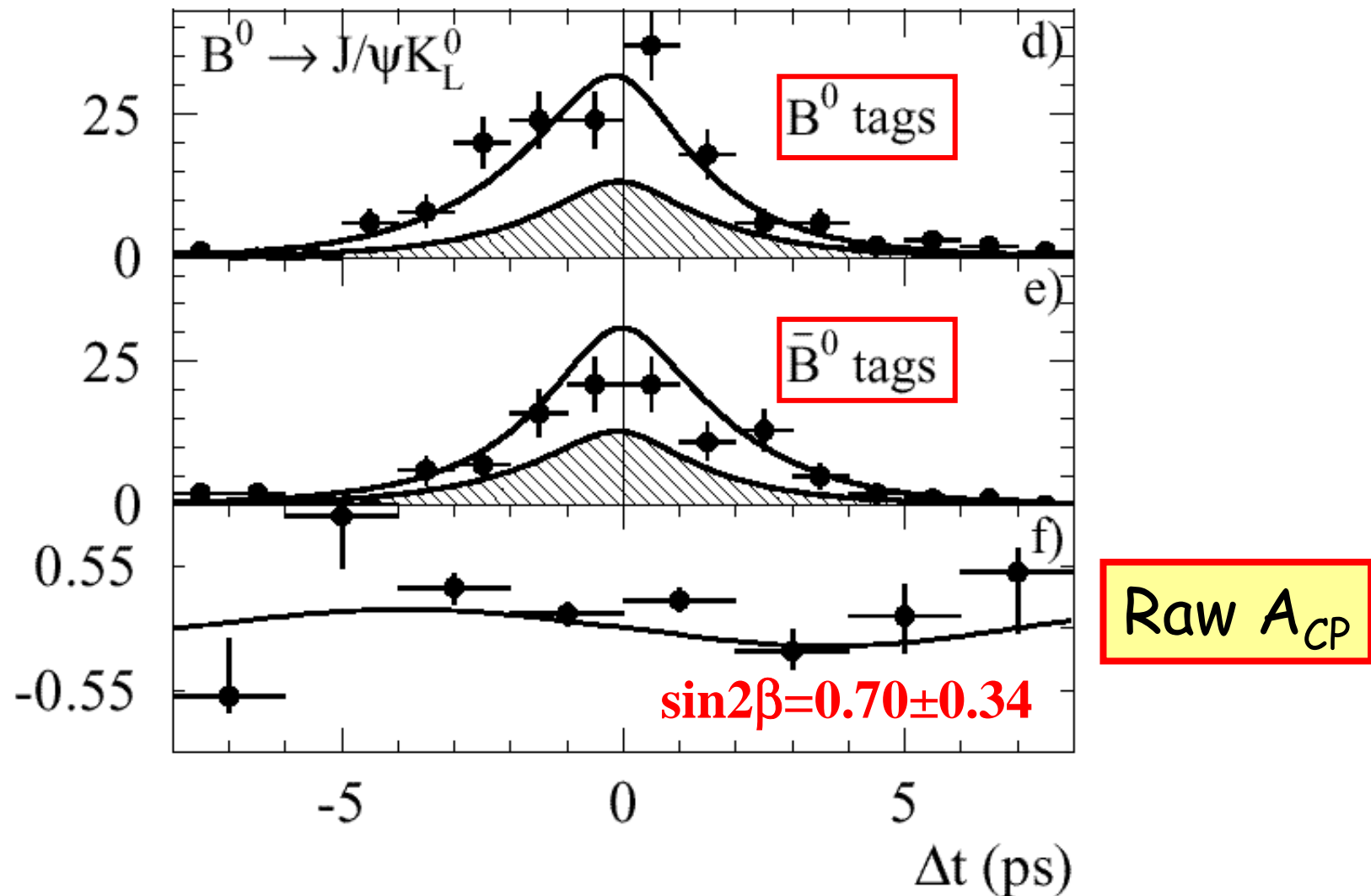
- ✓ All  $\Delta t$  parameters extracted from data
- ✓ Correct estimate of the error and correlations

# Raw Asymmetries

$$A_{CP}(\Delta t) \approx (1-2w) \times \sin(2\beta) \times \sin(\Delta m_d \Delta t)$$



# $J/\Psi K_L \Delta t$ Distributions



Fit projections are from global fit to all CP samples

# sin2β Fit Results

Phys. Rev. Lett. **87**  
091801 (2001)

Cross-checks:  
Null result in flavor samples

**B<sup>+</sup> reco**

0.03 ± 0.04

**B<sup>0</sup> reco**

0.02 ± 0.04

**J/ψKL**

0.70 ± 0.34

**J/ψK\*0**

0.82 ± 1.00

Consistency of CP  
channels  $P(\chi^2) = 8\%$

**χcKs**

2.59<sup>+0.55</sup>  
-0.67

**ψ(2S)Ks**

0.47 ± 0.42

**I/ψKs2π0**

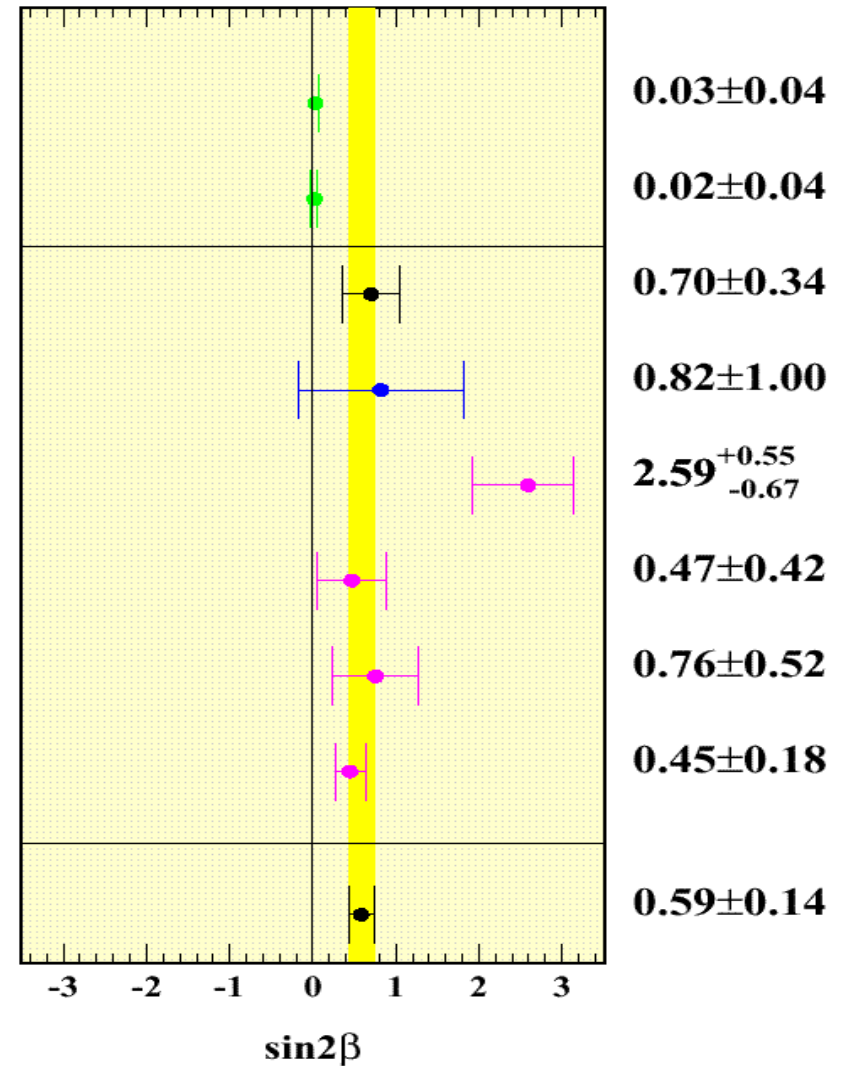
0.76 ± 0.52

**JψKs**

0.45 ± 0.18

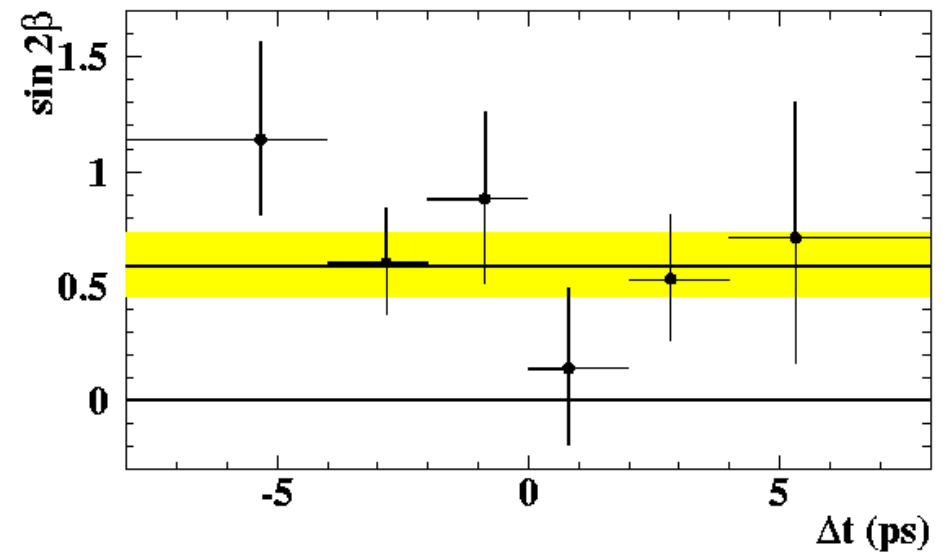
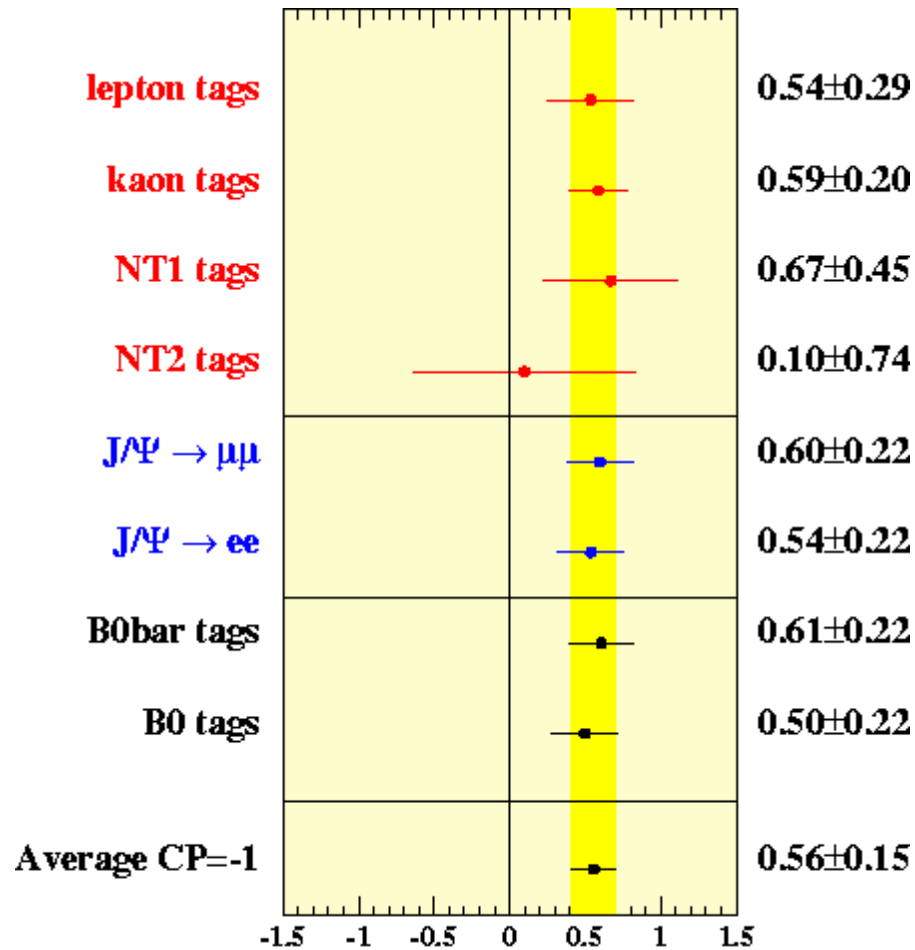
Goodness-of-fit:  
 $P(L_{\max} > L_{\text{obs}}) > 27\%$

All modes



$$\sin(2\beta) = 0.59 \pm 0.14$$

# Sin2b in various sub-samples



$\sin(2\beta)$  measured in several  $\Delta t$  bins

$\sin(2\beta)$  vs.  $J/\psi$  decay mode and tagging category and flavor for  $\eta = -1$  events

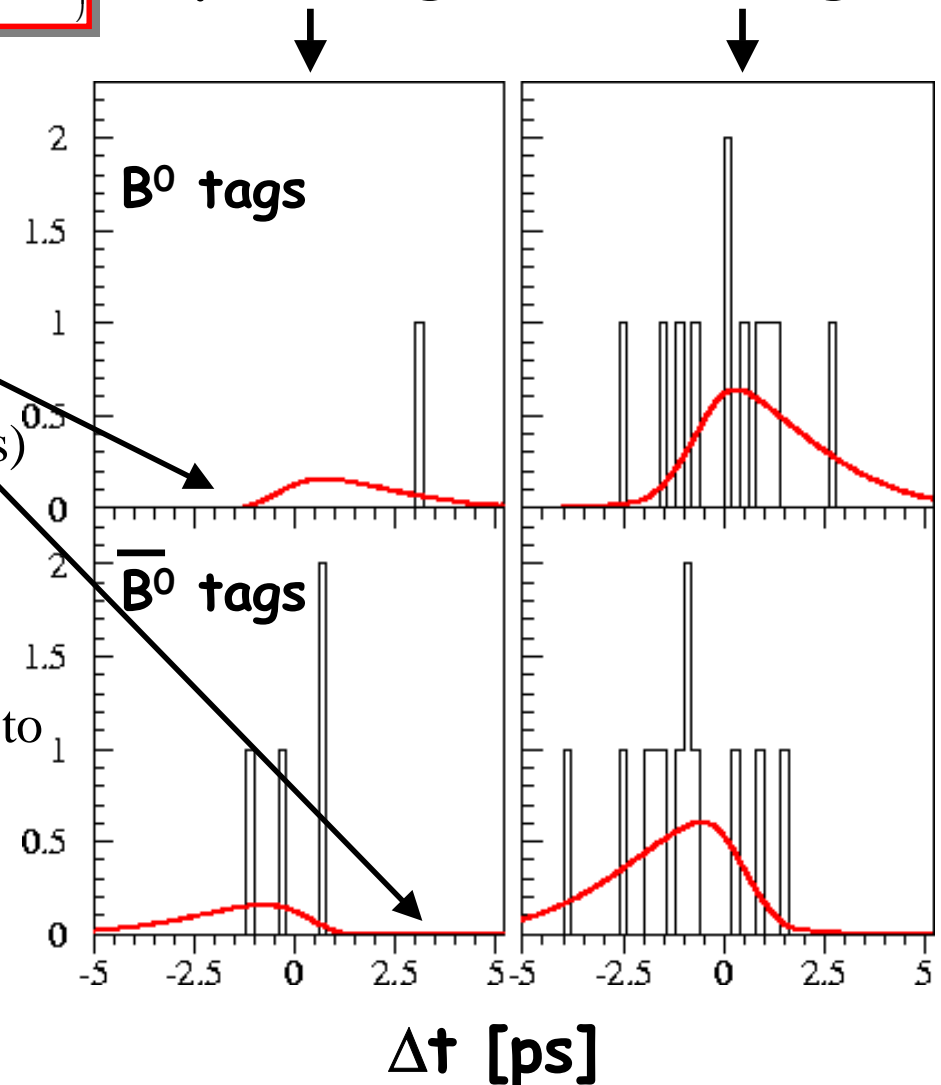
# Large $\sin 2\beta$ in $B^0 \rightarrow \chi_{C1} K_S$

$$f_{CP,\pm}(\Delta t) = \frac{e^{-|\Delta t|/\tau_B}}{4\tau_B} \times \left( 1 \pm \sin 2\beta \left[ 1 - 2\omega \right] \sin(\Delta m_d \Delta t) \right)$$

- fit for  $B^0/\bar{B}^0$   $\Delta t$  PDFs, not for  $A_{CP}$
- accommodate large asymmetry with **negative signal PDF** (at  $-(+)\pi/2\Delta m_d$  for  $B^0(\bar{B}^0)$  tagged events)
- Possible, because
  - No events at these  $\Delta t$  (eg. lepton tags)
  - Sum of signal + background PDFs **positive** (eg. Kaon tags)
- Note: a single lepton  $B^0$ -tag at  $\Delta t = -\pi/2\Delta m$  would bring  $\sin 2\beta$  from 2.6 to  $\sim 1/(1-2\omega_{lep}) \approx 1.1$
- Measure  $\sin 2\beta$  unbiased for low stat. samples and probability to obtain  $\sin 2\beta > 2.6$  when true value 0.7 is 1-2%

Lepton tags

Kaon tags

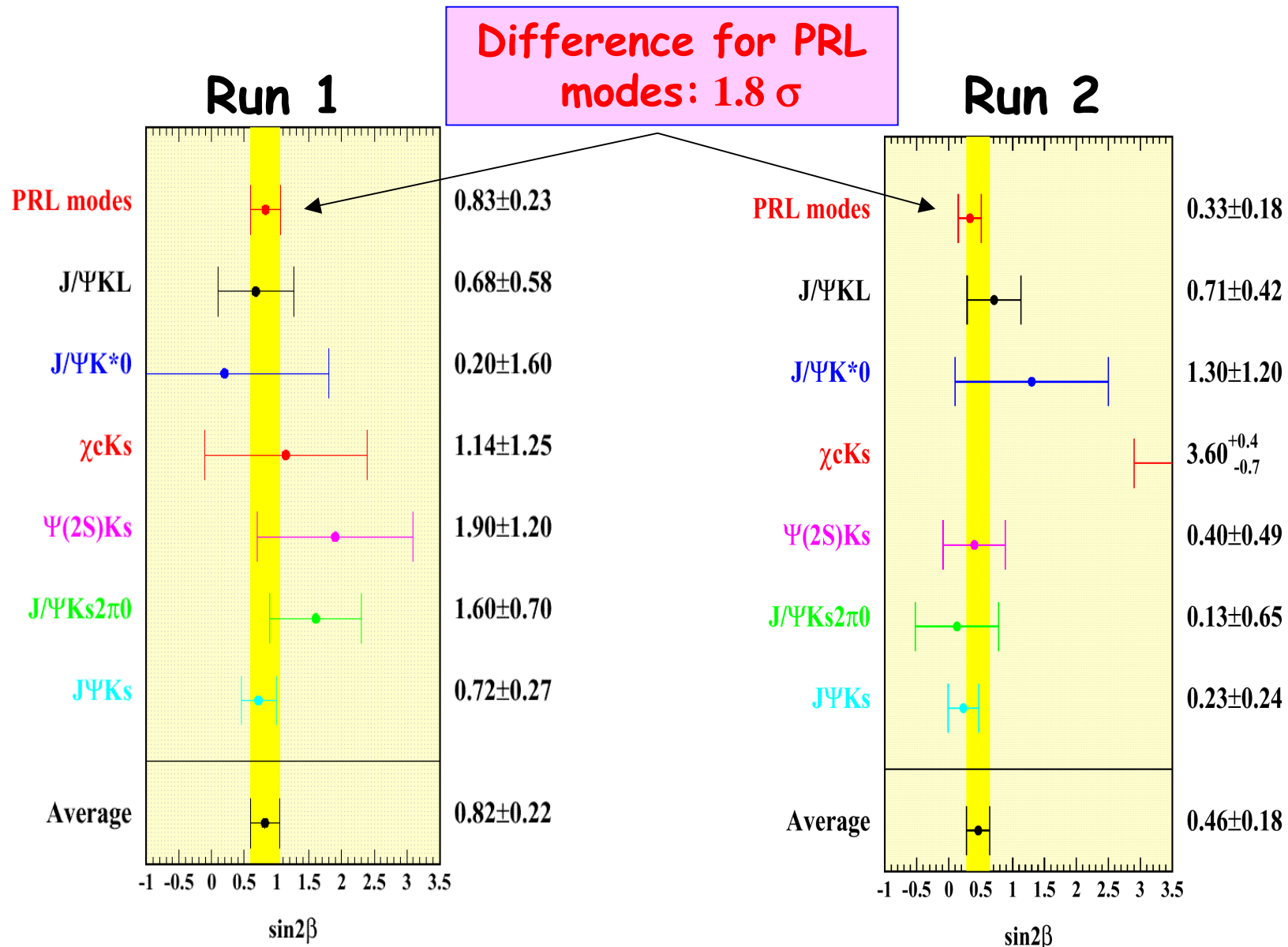


# Run1 $\rightarrow$ Run2 Changes/Results

- First publication in March 2001  
 $\sin(2\beta) = 0.34 \pm 0.20 \pm 0.05$  PRL 86 (2001) 2515
- Changes since then:
  - More data (run 2): **23  $\rightarrow$  32  $B\bar{B}$  pairs**
  - Improved reconstruction efficiency
  - Optimized selection criteria takes into account CP asymmetry of background in  $J/\psi K_L$
  - Additional decay modes  $\chi_{C1} K_S$  and  $J/\psi K^{*0}$
  - Improved vertex resolution for reconstructed and tag B



# Run 1 / Run 2 Results



# Major Sources of Systematic Error in $\text{Sin}2\beta$

*Measurement is Statistics Dominated*

Error/Sample	$K_S$	$K_L$	$K^{*0}$	Total
Statistical	0.15	0.34	1.01	0.14
Systematic	0.05	0.10	0.16	0.05

- Signal resolution and vertex reconstruction  $\longrightarrow$  0.03
  - Resolution model, outliers, residual misalignment of the Silicon Vertex Detector
- Flavor Tagging  $\longrightarrow$  0.03
  - possible differences between  $B_{CP}$  and  $B_{\text{flavor}}$  samples
- Background Characterization:  $\longrightarrow$  0.02 (overall)
  - Signal probability, fraction of  $B^+$  background in the signal region, CP content of background
  - Total 0.09 for  $J/\Psi K_L$  channel; 0.11 for  $J/\Psi K^{*0}$
- Total Systematic Uncertainty:  $\longrightarrow$  0.05 for total sample

# Search for Direct CP

If at least 2 amplitudes with a weak phase difference contribute

$|\lambda|$  might be different from 1

(tree amplitude and leading penguin amplitude for  $B \rightarrow J/\psi K_S$  have same weak phase in SM)

$$A_{CP} = C_{f_{CP}} \cos \Delta m_d \Delta t + S_{f_{CP}} \sin \Delta m_d \Delta t$$

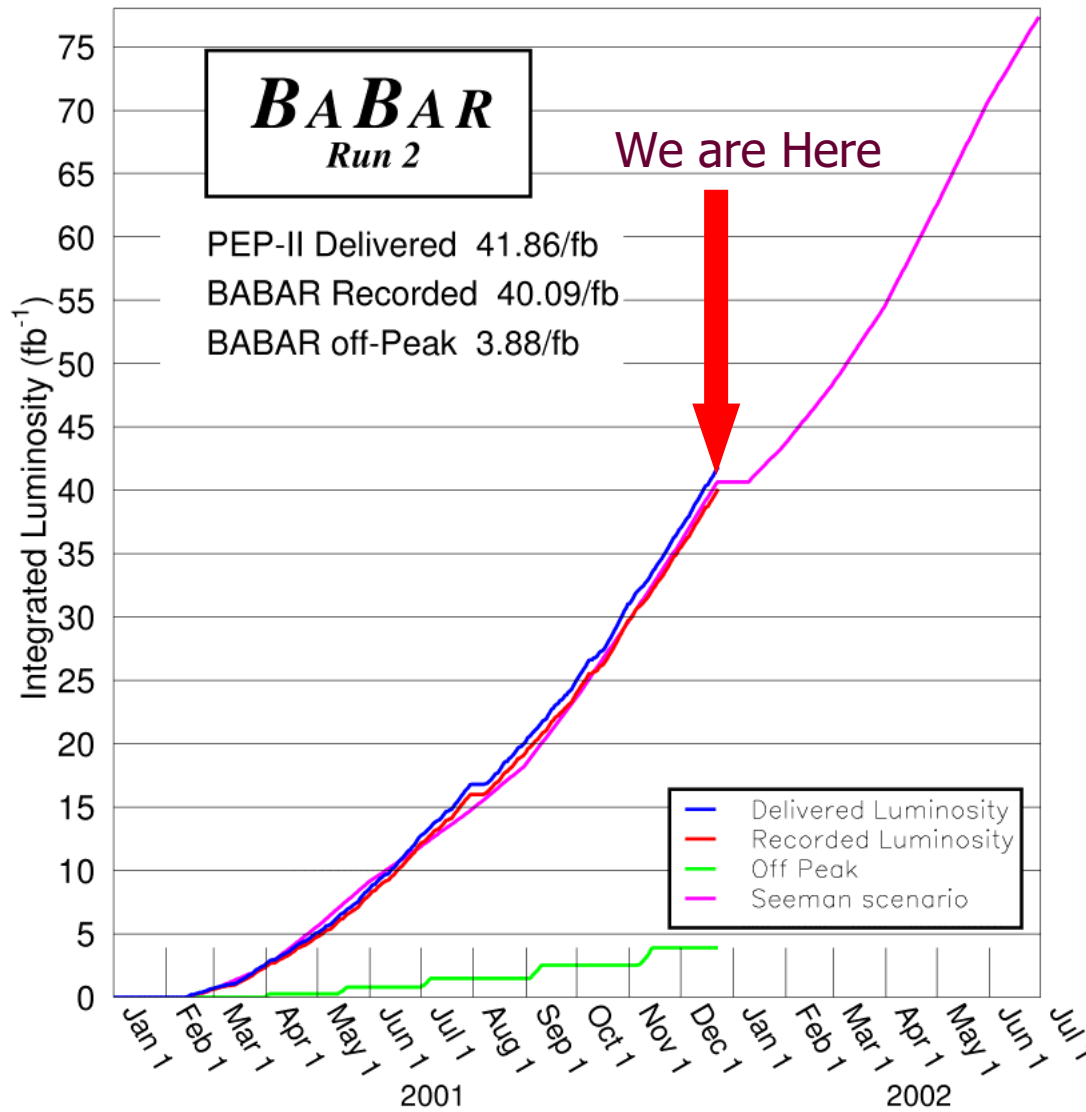
Probing new physics (only use  $\eta_{CP} = -1$  sample that contains no  $\overline{CP}$  background)

$$C_{f_{CP}} = \frac{1 - |\lambda_{f_{CP}}|^2}{1 + |\lambda_{f_{CP}}|^2}$$
$$S_{f_{CP}} = \frac{-2 \operatorname{Im} \lambda_{f_{CP}}}{1 + |\lambda_{f_{CP}}|^2}$$

$$|\lambda| = 0.93 \pm 0.09 \text{ (stat.)} \pm 0.03 \text{ (syst.)}$$

No evidence of direct CP violation due to decay amplitude interference (coefficient of the "sine" term unchanged)

# Luminosity Projection to Summer 2002

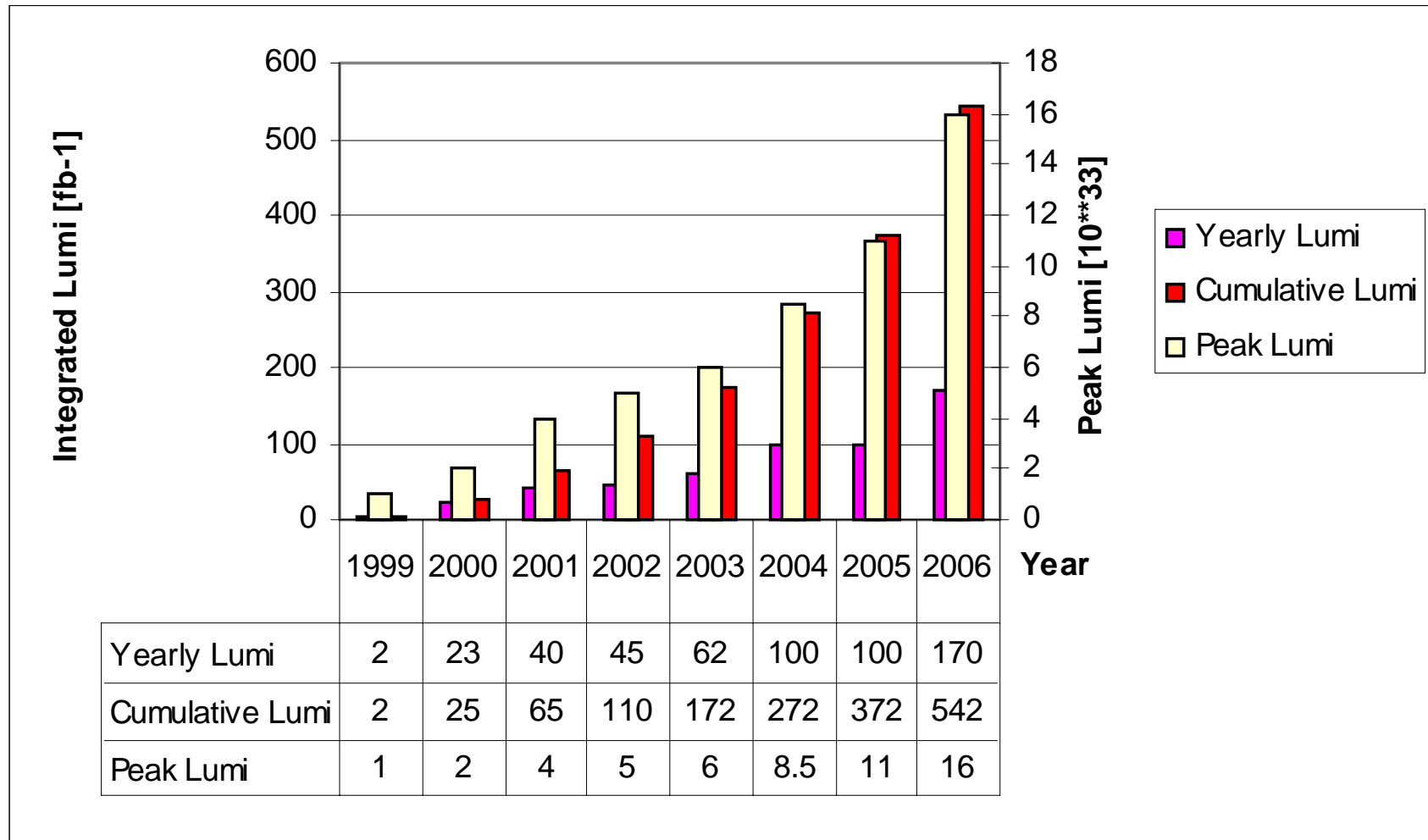


Project  $100 \text{ fb}^{-1}$  by Jun 2002

Hope to analyze Data very Quickly As demonstrated Already

# Luminosity Plans for BABAR & PEP II

Expect 550 fb<sup>-1</sup> By 2006



# Prognostications on Future $\sin 2\beta$ Precision

- In the Charmonium Modes

- Add more sub-modes “drops in the bucket” :

- Select  $\Psi \rightarrow$  hadrons, not just  $\Psi \rightarrow e^+ e^-$  or  $\mu^+ \mu^-$ ,
- smarter event selection (bremstrahlung recovery)
- Expect for charmonium modes:  $\Rightarrow$

$$\sigma_{\sin 2\beta} \leq 0.08 \text{ for } 100 \text{ fb}^{-1}$$

- Add new CP modes :

- $b \rightarrow ss\bar{s} \Rightarrow B \rightarrow \phi K_S$   $\Rightarrow$
- Compare with  $\sin 2\beta$  from  $b \rightarrow c \bar{c} s$

$$\sigma_{\sin 2\beta} \leq 0.25 \text{ for } 500 \text{ fb}^{-1}$$

- Cabibbo Suppressed  $B \rightarrow \Psi \pi^0$   $\Rightarrow$

$$\sigma_{\sin 2\beta} \leq 0.23 \text{ for } 500 \text{ fb}^{-1}$$

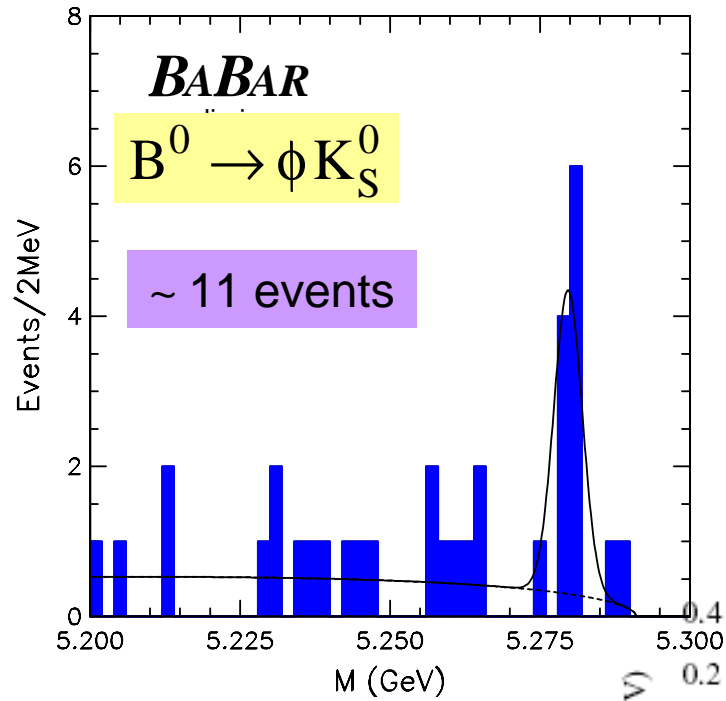
- Look for difference in  $\sin 2\beta$  measured from  $b \rightarrow c \bar{c} s$ 
  - » bound u-quark penguin pollution

- Cabibbo suppressed  $b \rightarrow c \bar{c} d \Rightarrow B \rightarrow D^{(*+)} D^{(*-)}$

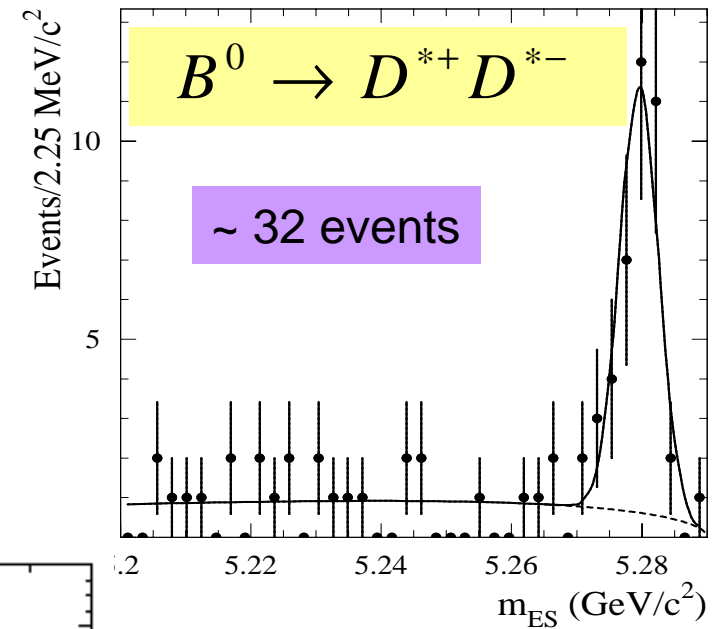
- May contain (small but unknown) penguin pollution
  - »  $D^* D^*$  mode requires angular analysis (in progress)

# New Modes for "Sin2β": 20 fb<sup>-1</sup>

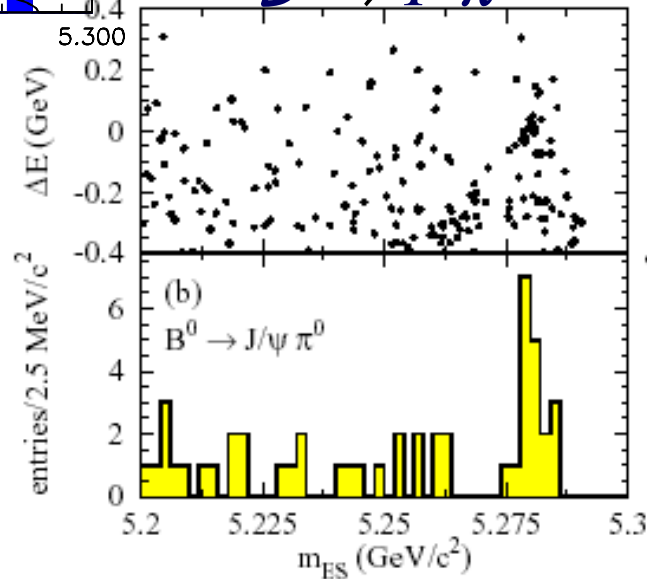
$b \rightarrow s\bar{s}s$



$b \rightarrow c\bar{c}d$

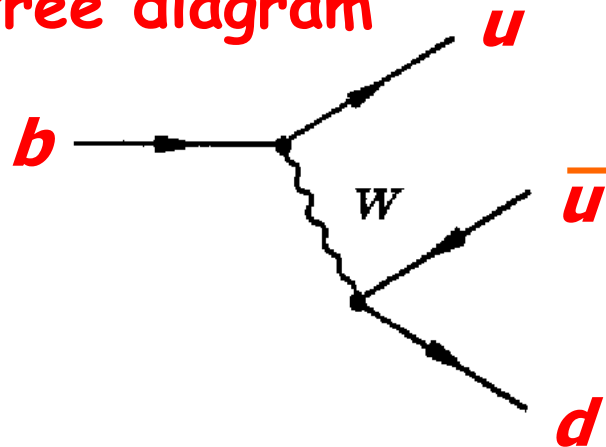


$B \rightarrow \Psi \pi^0$

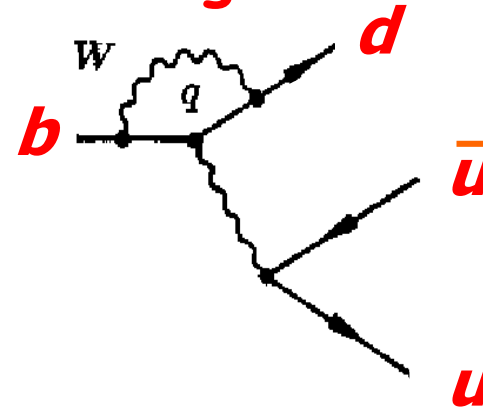


# CP Violation in $B^0 \rightarrow \pi^+\pi^-$ Decays

tree diagram



penguin diagram



Weak phase (only tree diagram)

$$\lambda \equiv \frac{q}{p} \frac{\bar{A}_f}{A_f} = \eta_f e^{-2i(\beta+\gamma)} = \eta_f e^{2i\alpha}$$

$$C_{\pi\pi} = 0, S_{\pi\pi} = \sin 2\alpha$$

Additional phase from penguin diagram

$|\lambda| \neq 1 \Rightarrow$  must fit for direct CP  
 $\text{Im}(\lambda) \neq \sin 2\alpha \Rightarrow$  need to relate  
 asymmetry to  $\alpha$

$$C_{\pi\pi} \neq 0, S_{\pi\pi} = \sin 2\alpha_{\text{eff}}$$

Decay distributions  $f_{\pm}(f_{\pm})$  when tag =  $B^0(\bar{B}^0)$

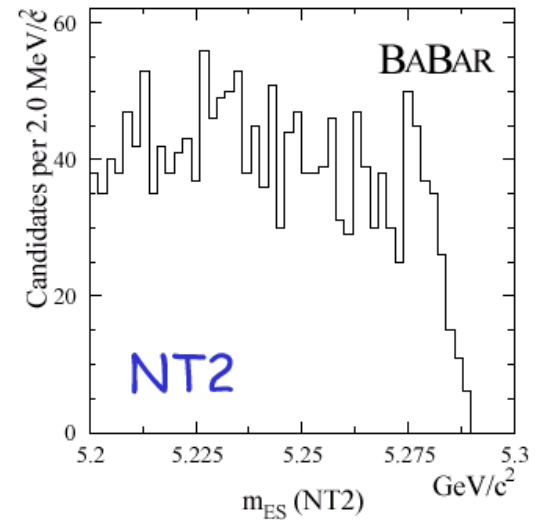
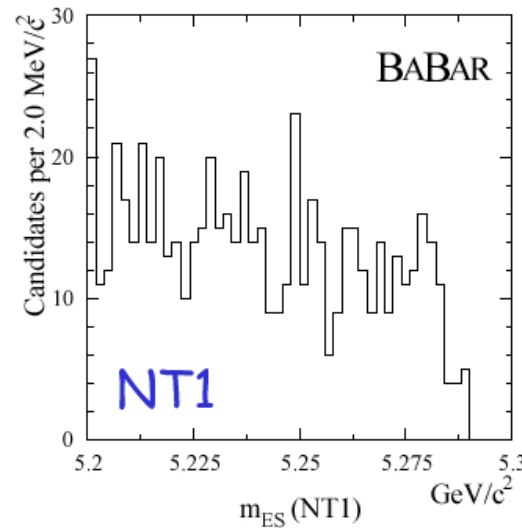
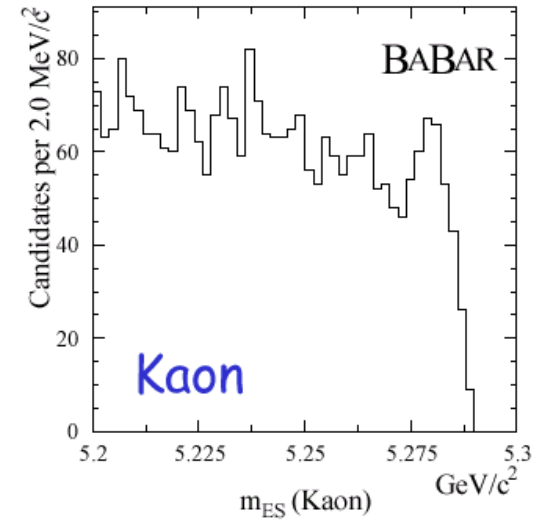
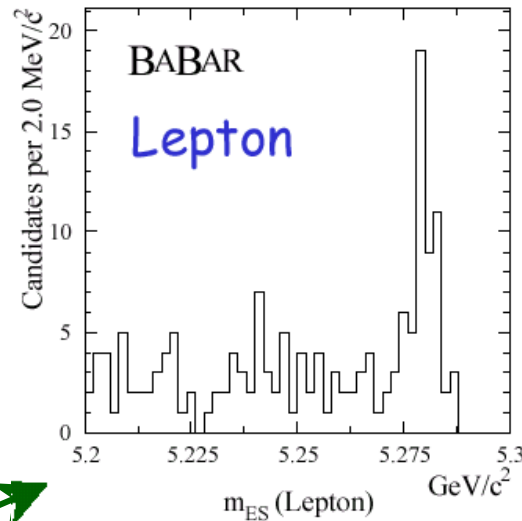
$$f_{\pm}(\Delta t) = \frac{e^{-\Delta t/\tau}}{4\tau} [1 \pm S_{\pi\pi} \sin(\Delta m_d \Delta t) \mp C_{\pi\pi} \cos(\Delta m_d \Delta t)]$$



# $B \rightarrow \pi^+\pi^-, K^+\pi^-, K^+K^-$ Data Sample

**Likelihood Analysis with high reconstruction efficiency:**  
Loose selection criteria yield 9741 two-prong candidates in  $30.4 \text{ fb}^{-1}$  (includes 97% background, almost entirely from continuum)

sum of  $\pi^+\pi^-/K^+\pi^-$   $m_{ES}$  distributions by tagging category (particle ID used in likelihood fit for  $\pi\pi/K\pi$  separation)



# B $\rightarrow$ $\pi^+\pi^-/K^+\pi^-$ Likelihood Fit

- Simultaneous extended ML fit to the BRs and CP asymmetries:
  - 8 event types (Sig and Bkg:  $\pi^+\pi^-$ ,  $K^+\pi^-$ ,  $K^-\pi^+$ ,  $K^+K^-$   $\rightarrow$  measure also direct CP violation in charge asymmetry)
$$A = \frac{N(K^-\pi^+) - N(K^+\pi^-)}{N(K^-\pi^+) + N(K^+\pi^-)}$$
  - Discriminating variables ( $m_{ES}$ ,  $\Delta E$ , *Fisher*, Cherenkov angles,  $\Delta t$ )
  - Mistag rates and  $\Delta t$  signal resolution function same as in  $\sin 2\beta$  fit (uses also untagged events to improve BR measurements)
  - $\Delta m_d$ ,  $B^0$  lifetime fixed
  - Empirical background parameters determined from  $m_{ES}$  sidebands

- With 30.4 fb<sup>-1</sup>:

$$65 \pm \frac{12}{11} \pi^+\pi^-, \quad 217 \pm 18 K^+\pi^-, \quad 4.3 \pm \frac{6.3}{4.3} K^+K^-$$

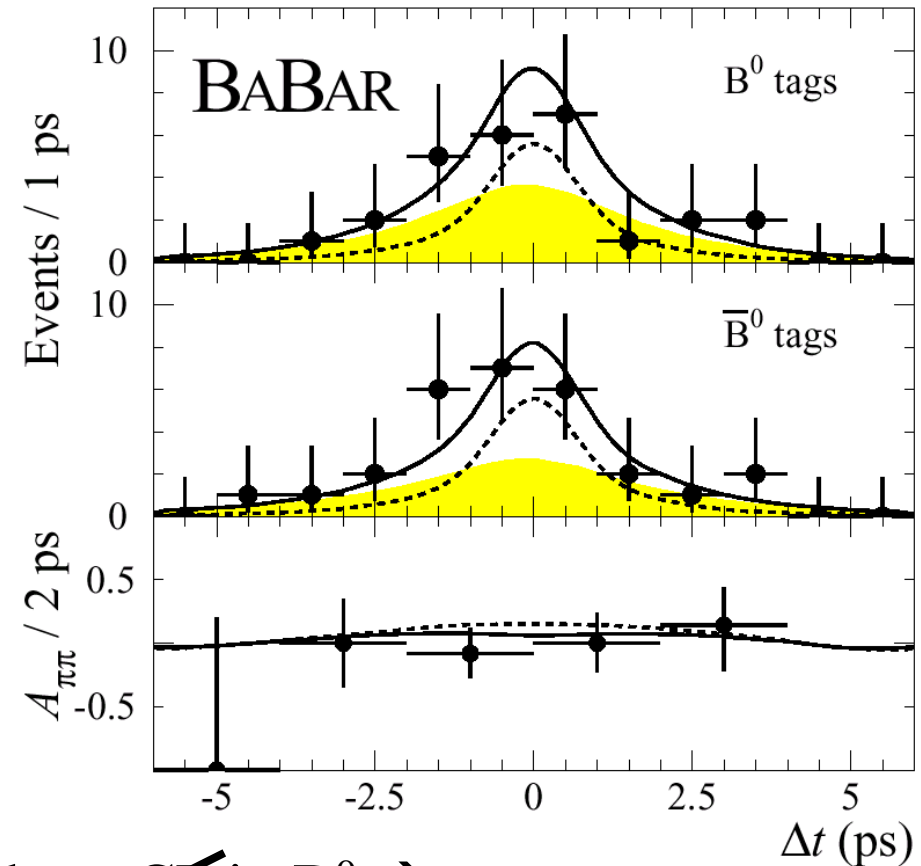
# $B^0 \rightarrow \pi^+\pi^-$ Asymmetry Result

hep-ex/0110062

$$S(\pi^+\pi^-) = 0.03_{-0.56}^{+0.53} (stat) \pm 0.11 (syst)$$

$$C(\pi^+\pi^-) = -0.25_{-0.47}^{+0.45} (stat) \pm 0.14 (syst)$$

$$A_{CP}(K^\pm\pi^\mp) = -0.07 \pm 0.08 (stat) \pm 0.02 (sys)$$



- Measurement compatible with no ~~CP~~ in  $B^0 \rightarrow \pi^+\pi^-$
- Statistically limited due to small branching fraction
- Need  $\sim 500/\text{fb}$  for  $\sigma(S_{\pi\pi}) \sim 0.10-0.15$

# Summary and Outlook

- New precision measurements of  $B^0/B^+$  lifetimes and  $B^0\bar{B}^0$  mixing frequency  $\Delta m_d$

$$\tau_0 = 1.546 \pm 0.032 \pm 0.022 \text{ ps}$$

$$\tau_{\pm} = 1.673 \pm 0.032 \pm 0.022 \text{ ps}$$

$$\tau_0/\tau_{\pm} = 1.082 \pm 0.026 \pm 0.011$$

$$\Delta m_d = 0.516 \pm 0.016 \pm 0.010 \text{ ps}^{-1} \text{ (hadronic)}$$

$$\Delta m_d = 0.493 \pm 0.012 \pm 0.009 \text{ ps}^{-1} \text{ (dileptons)}$$

- Measurement of flavor-tagged, time-dependent B decays at asymmetric B factory has become established technique
- BaBar observes CP violation in the  $B^0$  system at  $4\sigma$  level

$$\sin(2\beta) = 0.59 \pm 0.14 \pm 0.05$$

- Probability is  $< 3 \times 10^{-5}$  to observe an equal or larger value if no CP violation exists
- Corresponding probability for only the  $\eta_{CP} = -1$  modes is  $2 \times 10^{-4}$

# Summary and Outlook (cont.)

- Best measurement of CPV in mixing:

$$|\mathbf{q/p}| = 0.998 \pm 0.006 \pm 0.007$$

- First measurement of time-dependent CP asymmetry in rare B decay mode  $B \rightarrow \pi^+\pi^-$

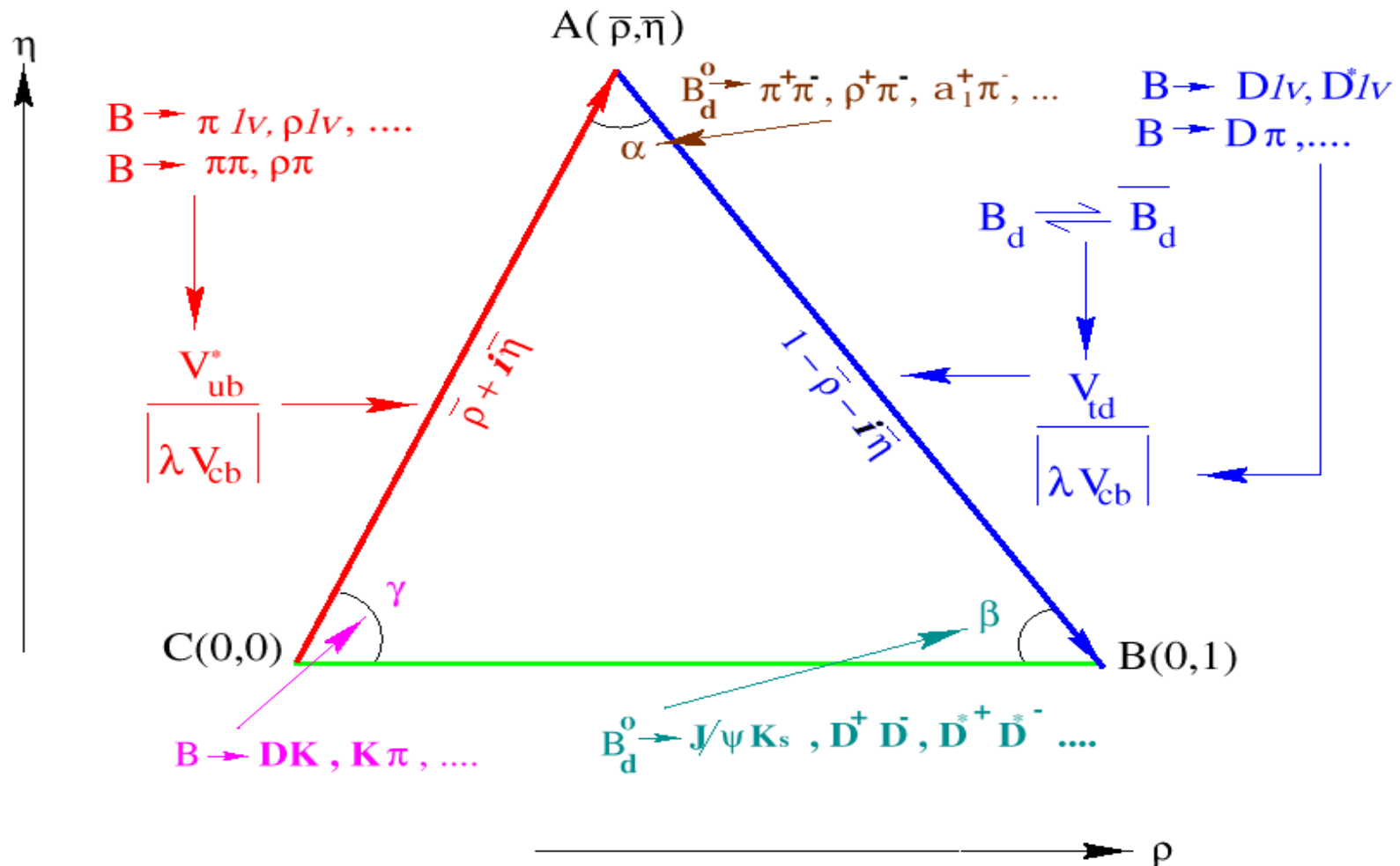
$$S(\pi^+\pi^-) = 0.03_{-0.56}^{+0.53} (stat) \pm 0.11 (syst)$$

$$C(\pi^+\pi^-) = -0.25_{-0.47}^{+0.45} (stat) \pm 0.14 (syst)$$

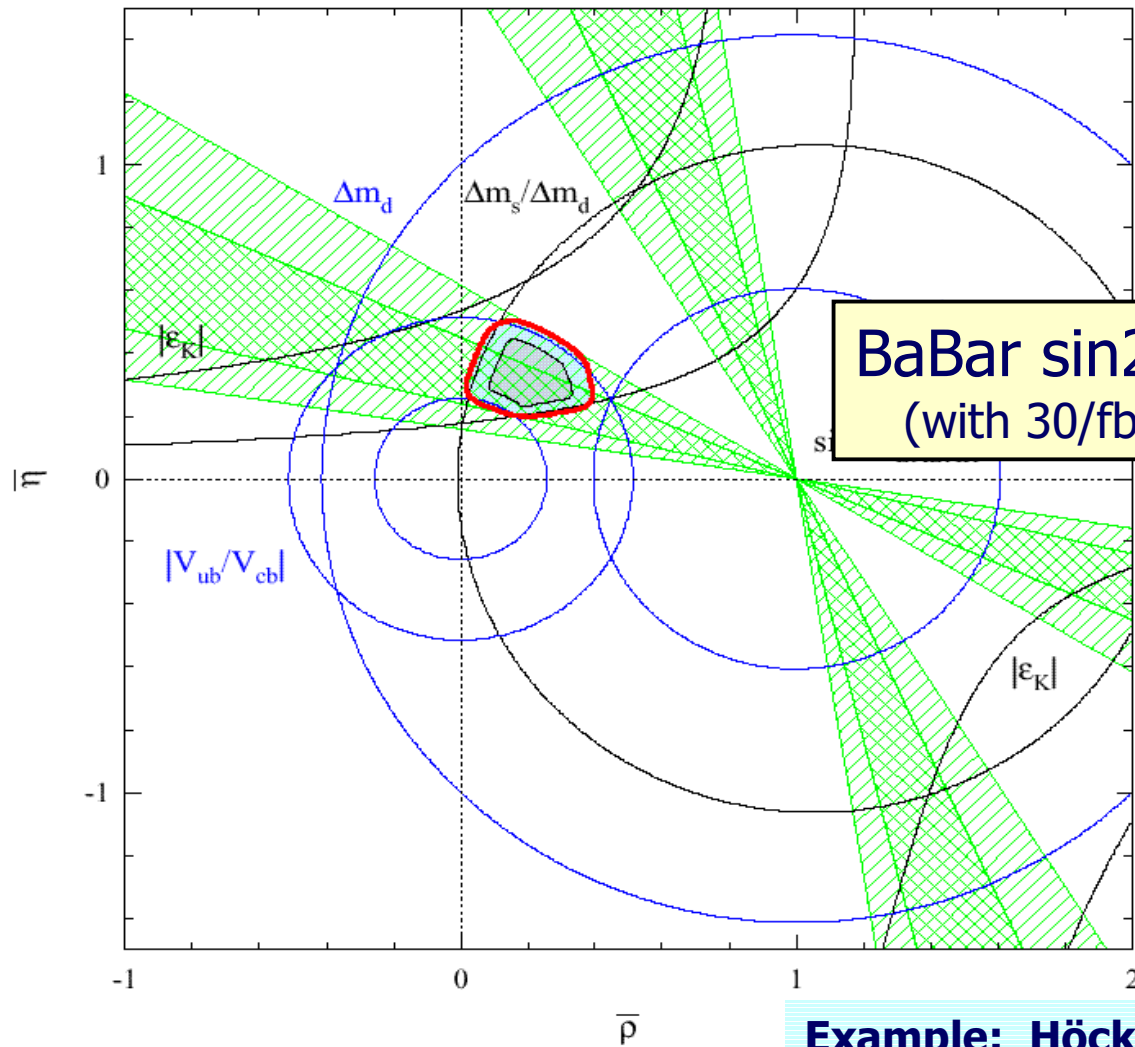
- The study of CP violation in the B system has started:
  - $\sin(2\beta)$  will very soon become precision measurement ( $\rightarrow$  unitarity triangle constraints will be limited by other CKM parameters)
  - Need to compare  $\sin(2\beta)$  from different decay modes to test standard model
- With anticipated  $100 \text{ fb}^{-1}$  by next summer, error in  $\sin(2\beta)$  will be 0.08 and for the asymmetry in  $B \rightarrow \pi^+\pi^-$  error will be  $\sim 0.3$

# BaBar Aim : Multiple Measurements and Tests to Overconstrain the Unitarity Triangle

Sin2 $\beta$  is just one focus of BaBar: Work in progress on Many Fronts  
An Exciting era of B physics in Progress !



# The Unitarity Triangle and This Measurement



**BaBar  $\sin 2\beta$**   
(with 30/fb)

One solution for  $\beta$  is consistent with measurements of sides of Unitarity Triangle

Error on  $\sin 2\beta$  is dominated by statistics  
 $\rightarrow$  will decrease as

$$\frac{1}{\sqrt{\text{Luminosity}}}$$

**Example: Höcker et al, hep-ph/0104062 (also other recent global CKM matrix analyses)**