

# Level Densities and $\gamma$ Strength Functions in Light Sc and Ti Isotopes

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# Overview

- The Oslo Method
  - Assumptions
  - Procedure
- Results for light Sc and Ti isotopes
  - $^{43}\text{Sc}$ ,  $^{44,45,46}\text{Ti}$
- Outlook

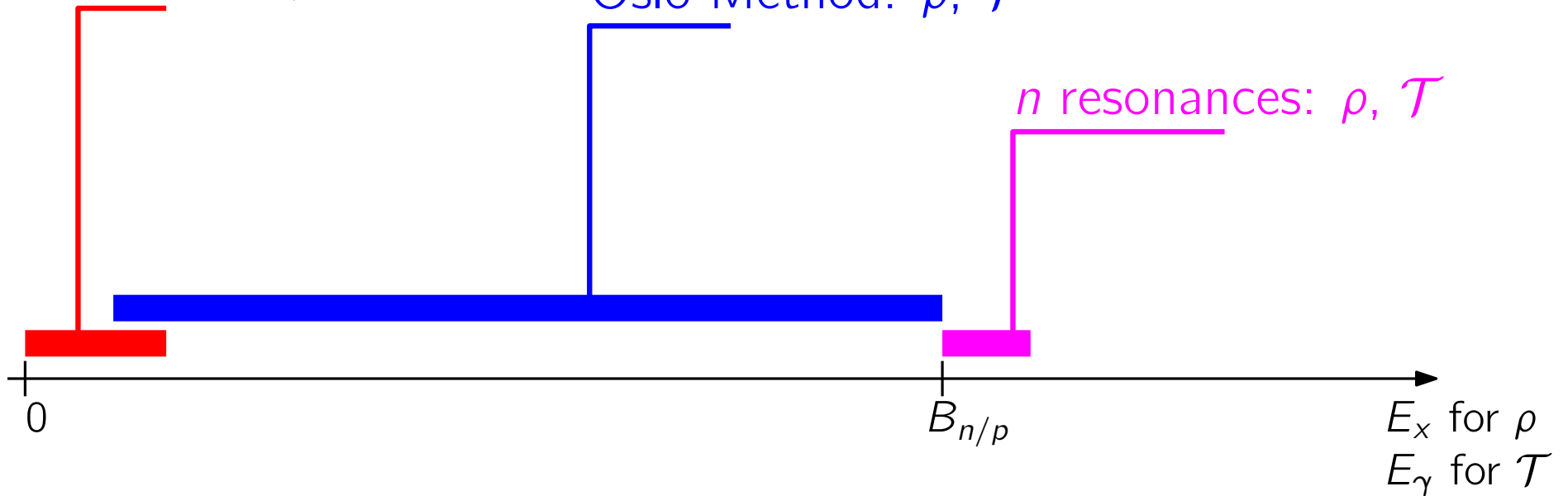
# The Oslo Method – Aim

measure  $\rho$  and  $\mathcal{T}$  simultaneously

discrete levels:  $\rho$

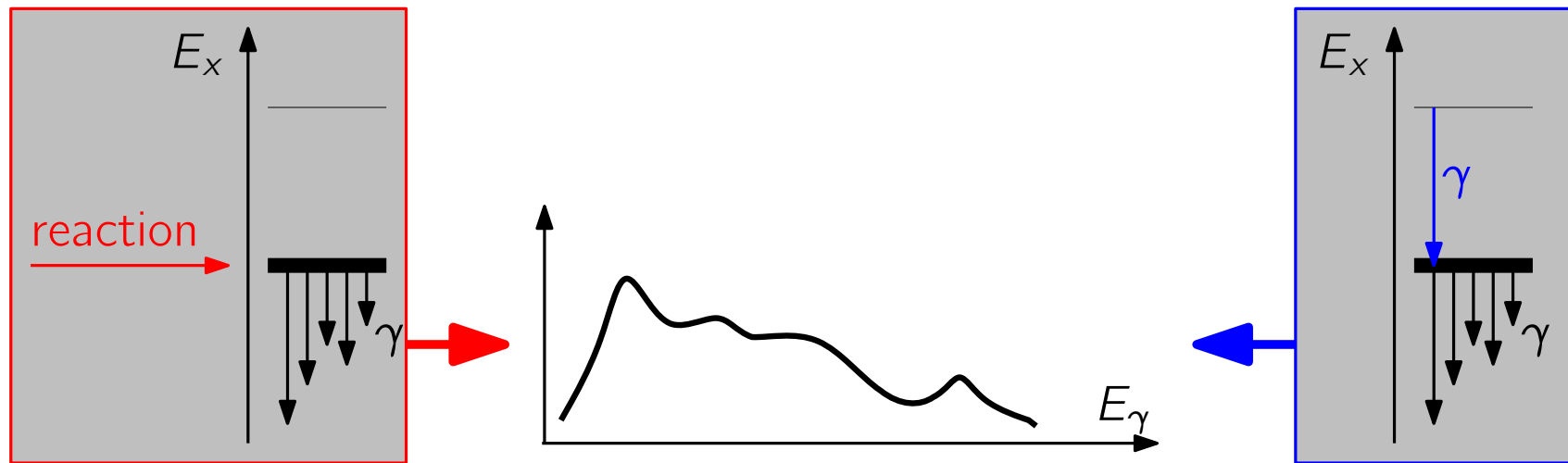
Oslo Method:  $\rho, \mathcal{T}$

$n$  resonances:  $\rho, \mathcal{T}$



# The Oslo Method – Assumptions

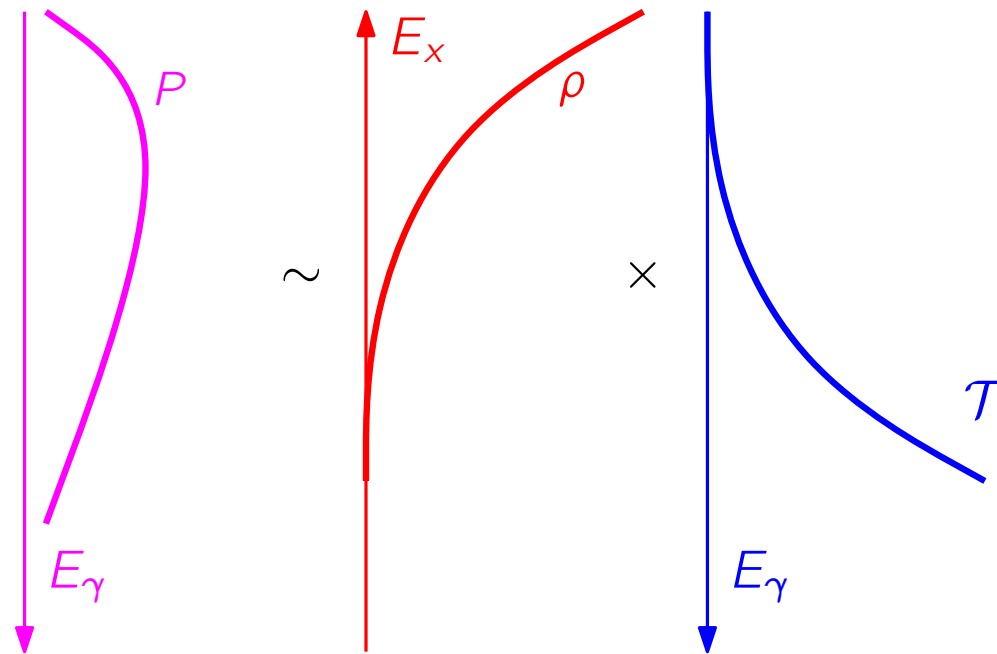
- shape of spectra independent of “population path”



# The Oslo Method – Assumptions

- shape of spectra independent of “population path”
- Brink-Axel hypothesis:  $\mathcal{T}$  independent of  $E_{i/f}$
- Generalized Fermi’s golden rule: transition probability factorizeable as

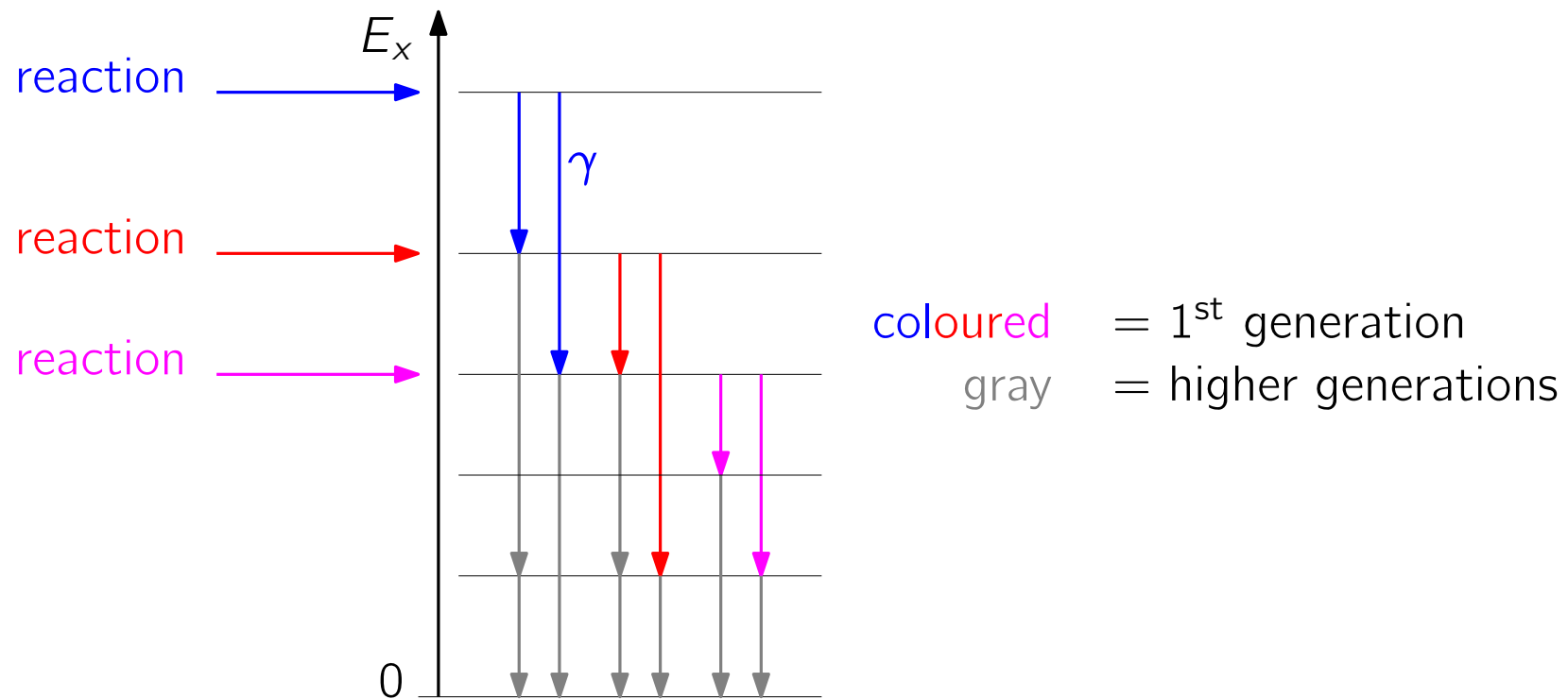
$$P(E_i, E_\gamma) \sim \rho(E_i - E_\gamma) \mathcal{T}(E_\gamma)$$



for  $E1$  and  $M1$ :  $\mathcal{T} \sim f(E_\gamma) E_\gamma^3$

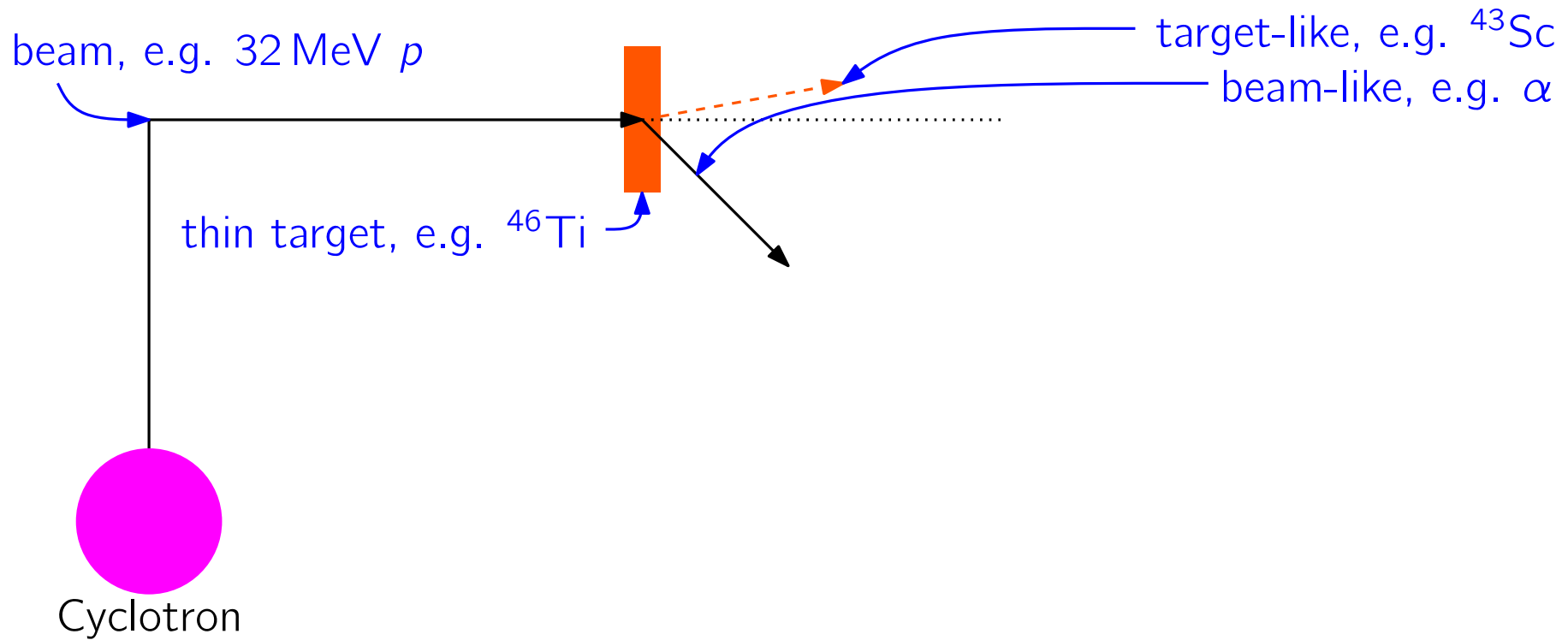
# The Oslo Method – Procedure

- measure  $E_x$  vs.  $E_\gamma$  matrix
- correct  $E_\gamma$  for detector response function (“unfolding”)
- extract 1<sup>st</sup> generation spectra ( $P$ )

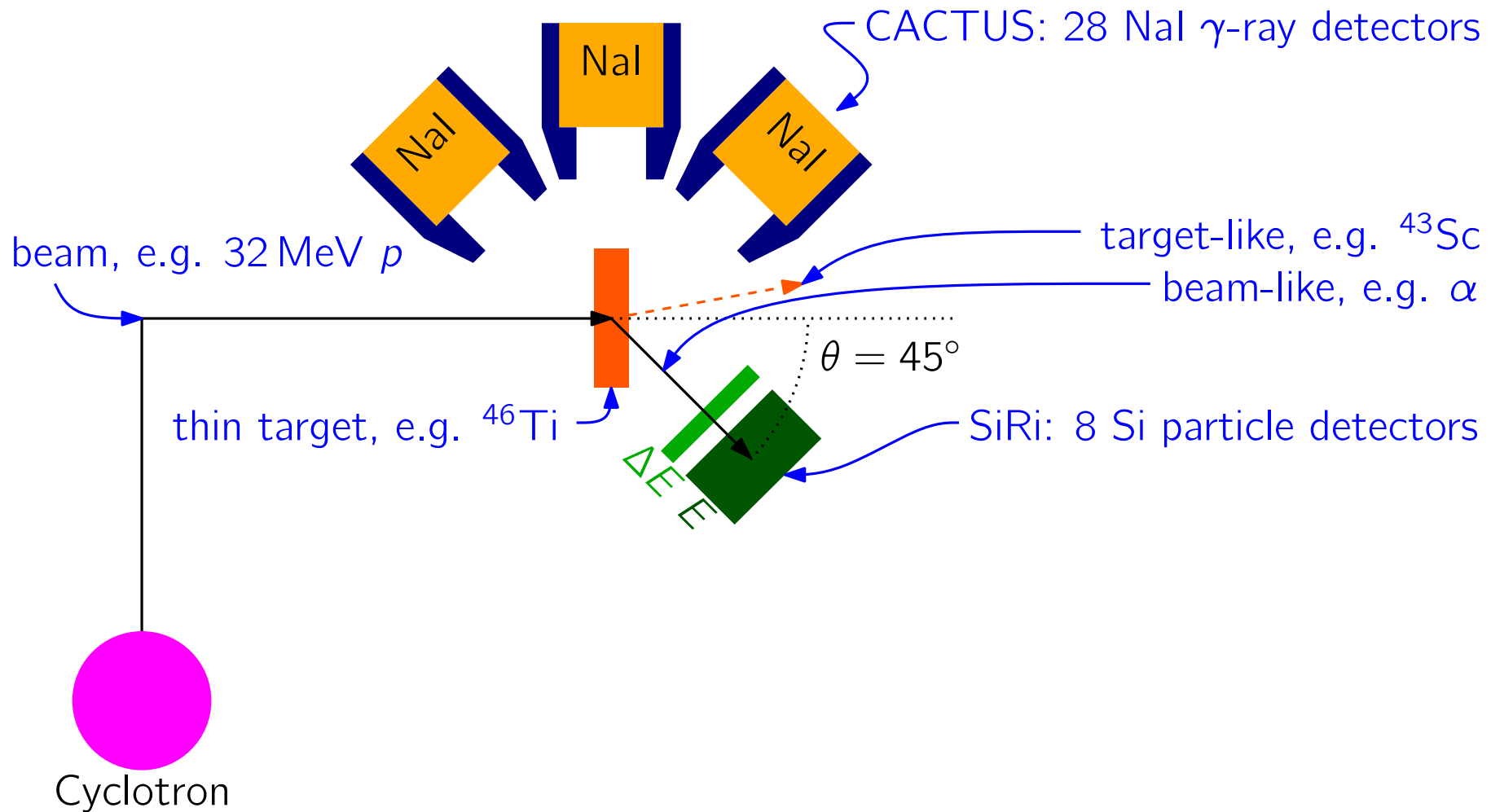


- derive  $\rho$  and  $\mathcal{T}$  according to factorization  $P(E_i, E_\gamma) \sim \rho(E_i - E_\gamma)\mathcal{T}(E_\gamma)$
- normalize  $\rho$  and  $\mathcal{T}$

# The Oslo Method – Experiment



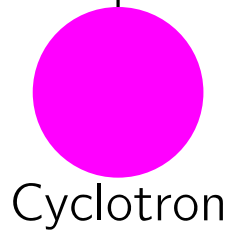
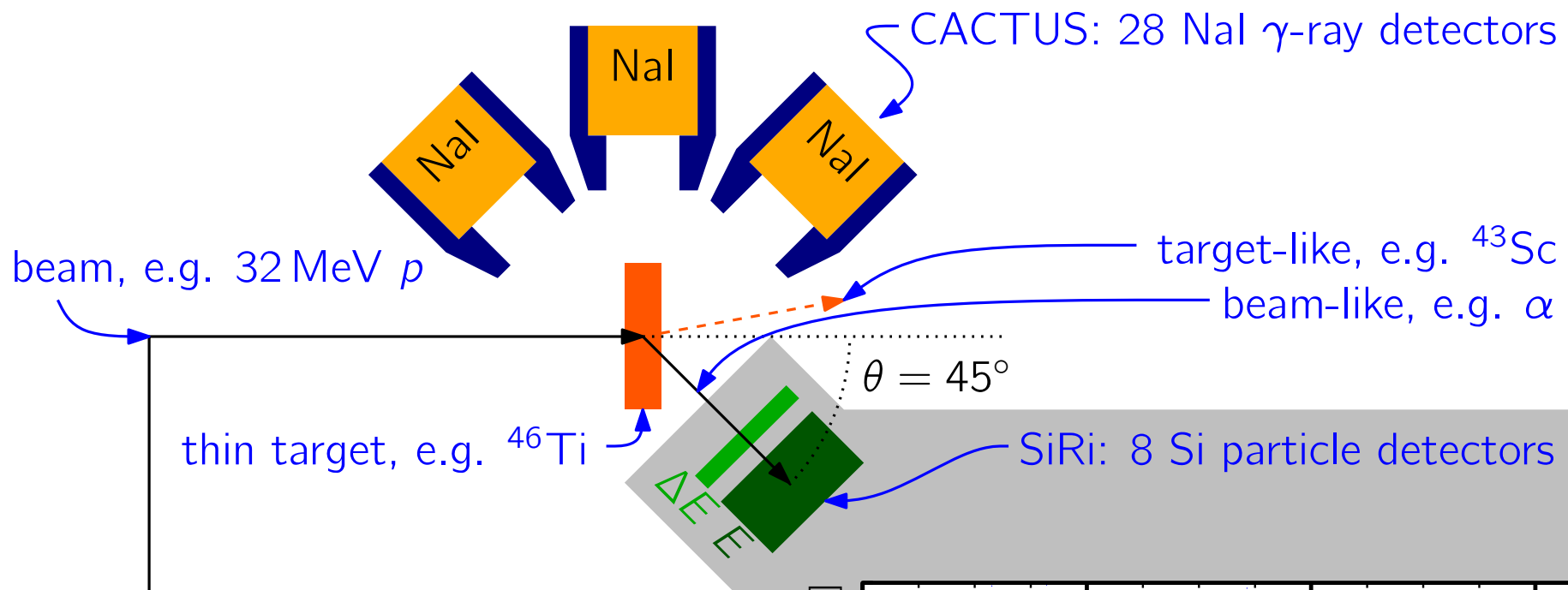
# The Oslo Method – Experiment



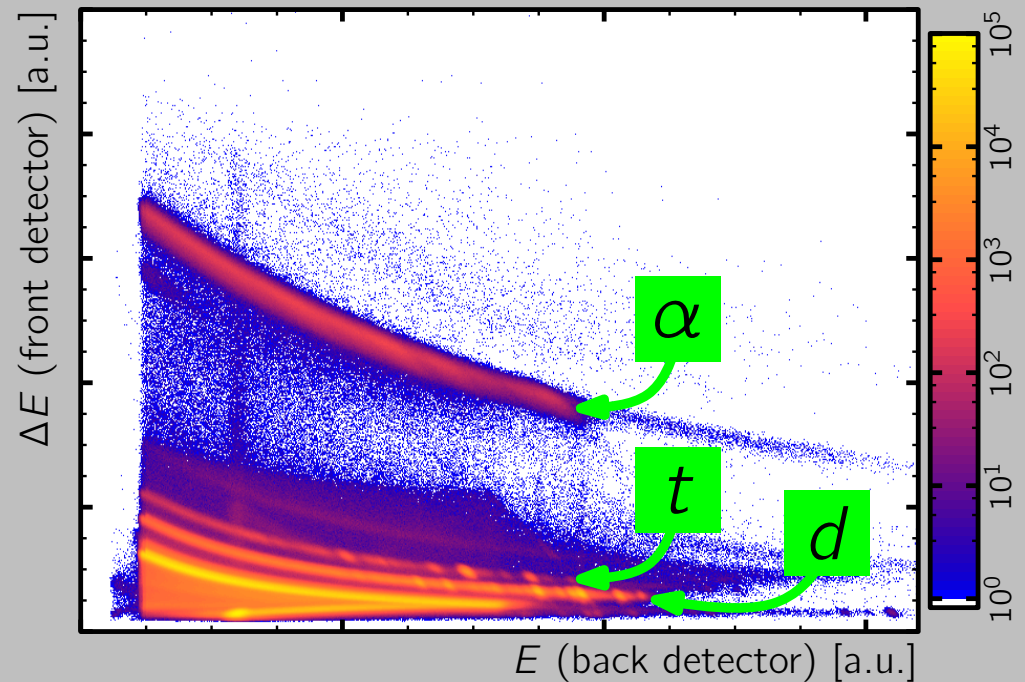
- measure  $E_x$  vs.  $E_\gamma$  matrix
- $(E + \Delta E)$ ,  $E_{\text{beam}}$ , kinematics, energy losses  $\rightarrow E_x$



# The Oslo Method – Experiment



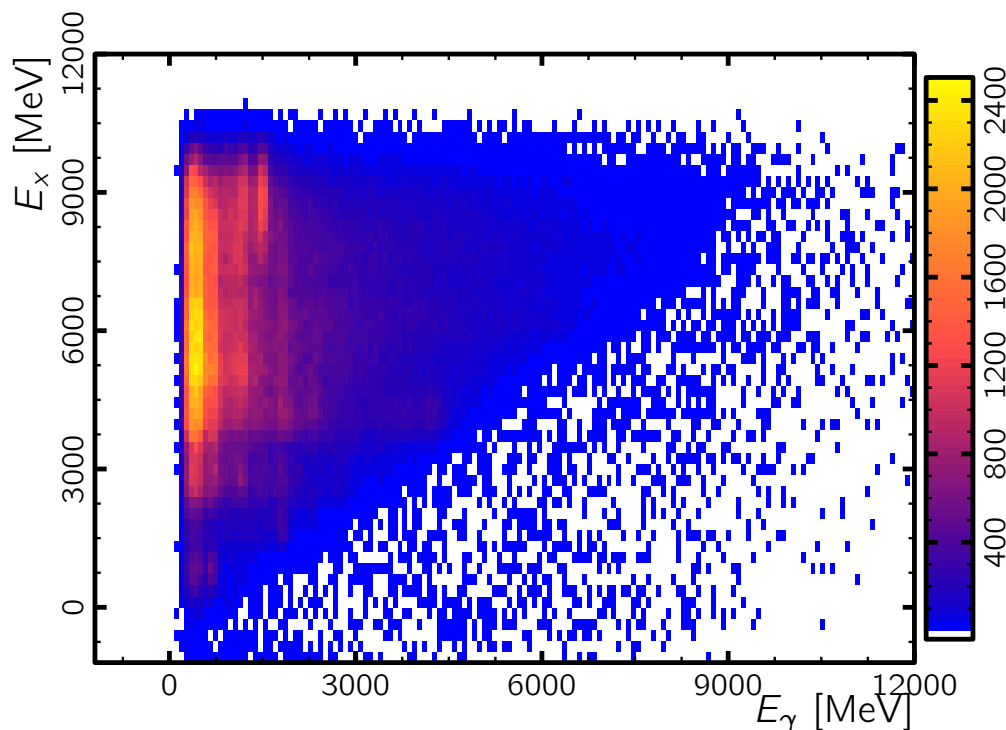
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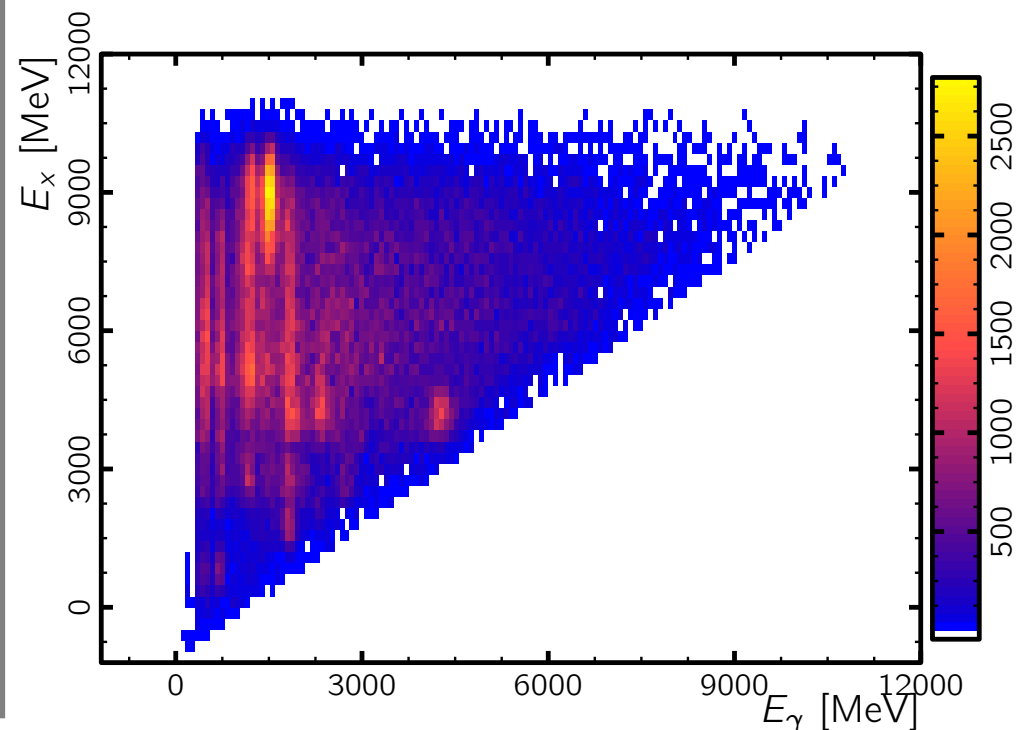
# The Oslo Method – Unfolding

- “unfolding” — correct  $E_\gamma$  for detector response function:
  - remove Compton background, pair production effects, ...
  - correct for  $E_\gamma$  dependence of NaI efficiency

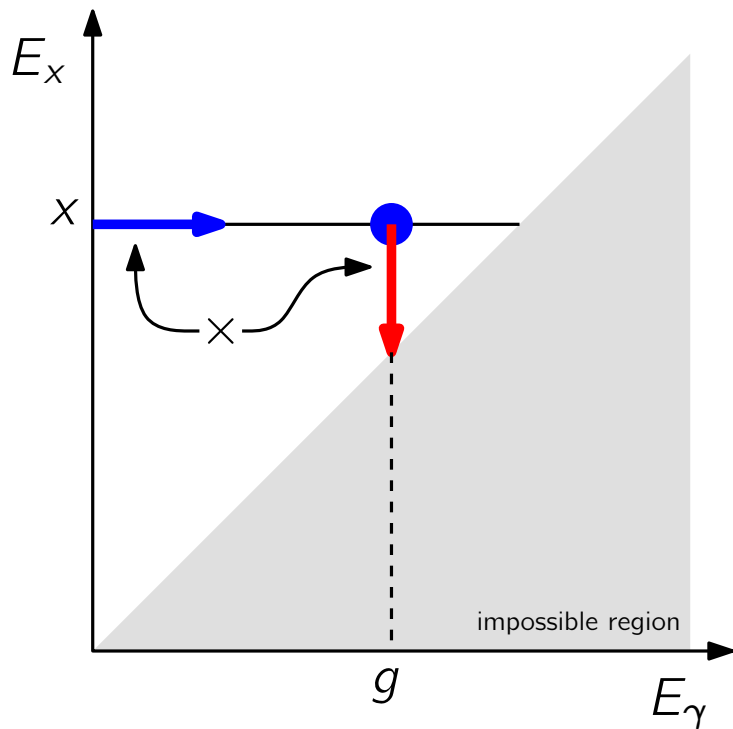
“raw” matrix



“unfolded” matrix



# The Oslo Method – 1<sup>st</sup> Generation

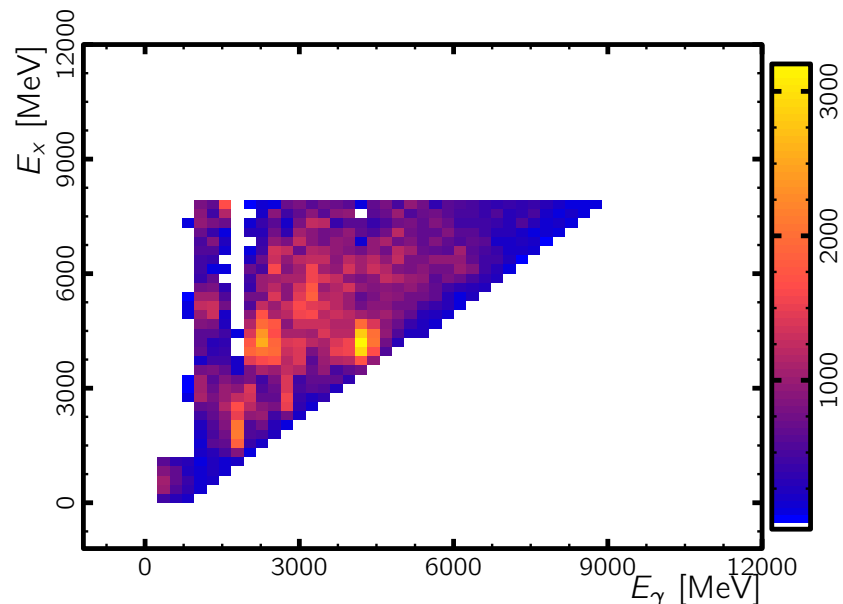


- extract 1<sup>st</sup> generation spectra
- $u(g, x)$ : unfolded matrix, contains 1<sup>st</sup> + all higher generations
- $p(g, x)$ : 1<sup>st</sup> generation matrix

$$u(g, x) = p(g, x) + \sum_{g'} p(g', x) u(g, x - g')$$

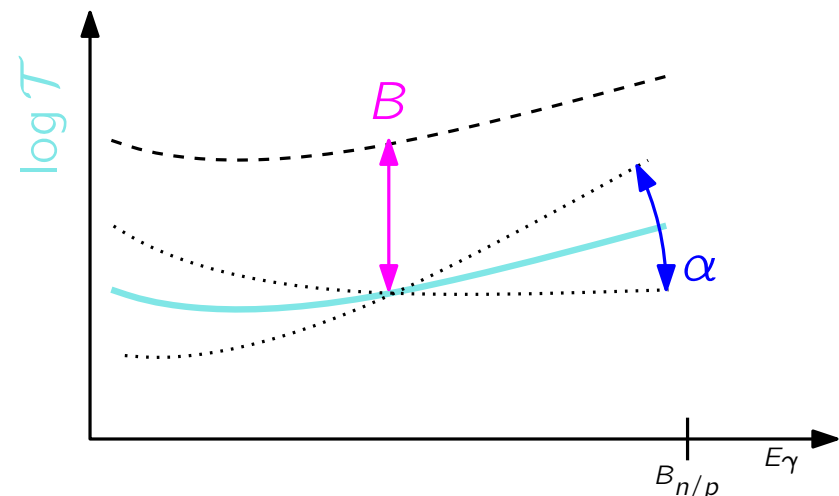
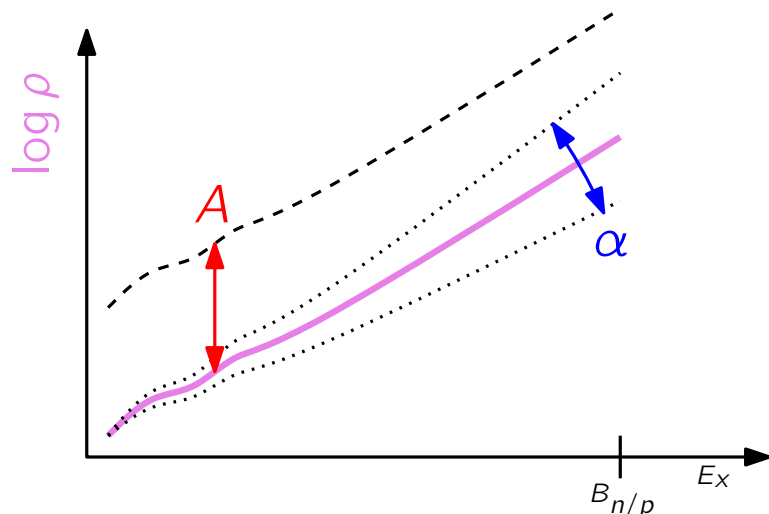
“weight” higher generations

- find  $p(g, x)$  iteratively



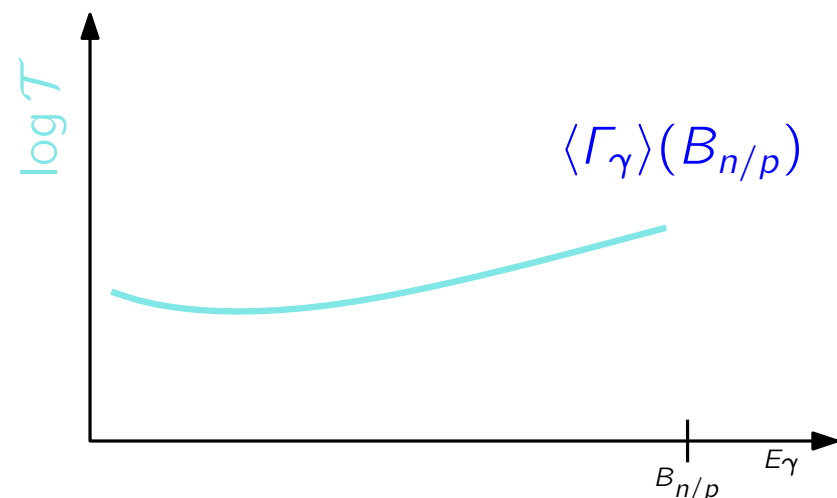
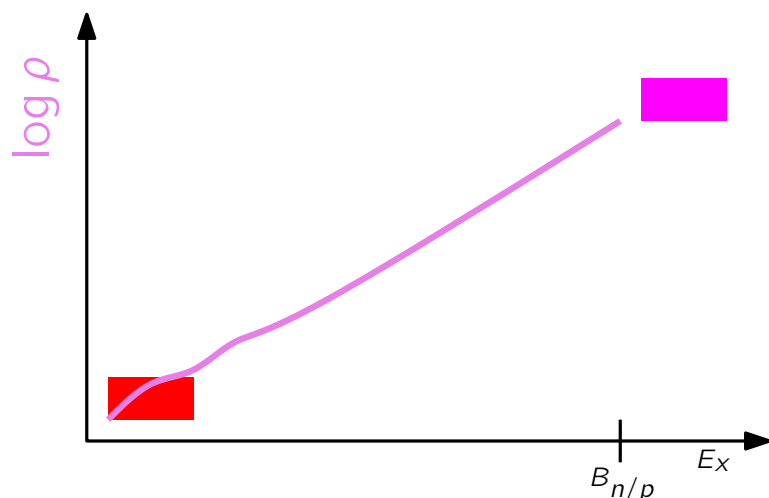
# The Oslo Method – $\rho$ and $\mathcal{T}$

- derive level density and strength function from 1<sup>st</sup> generation spectra
  - more data points than variables, iterative  $\chi^2$  minimization
- solutions can be re-normalized
  - $\rho(E_f) \rightarrow A \exp(\alpha E_f) \rho(E_f)$
  - $\mathcal{T}(E_\gamma) \rightarrow B \exp(\alpha E_\gamma) \mathcal{T}(E_\gamma)$



# The Oslo Method – $\rho$ and $\mathcal{T}$

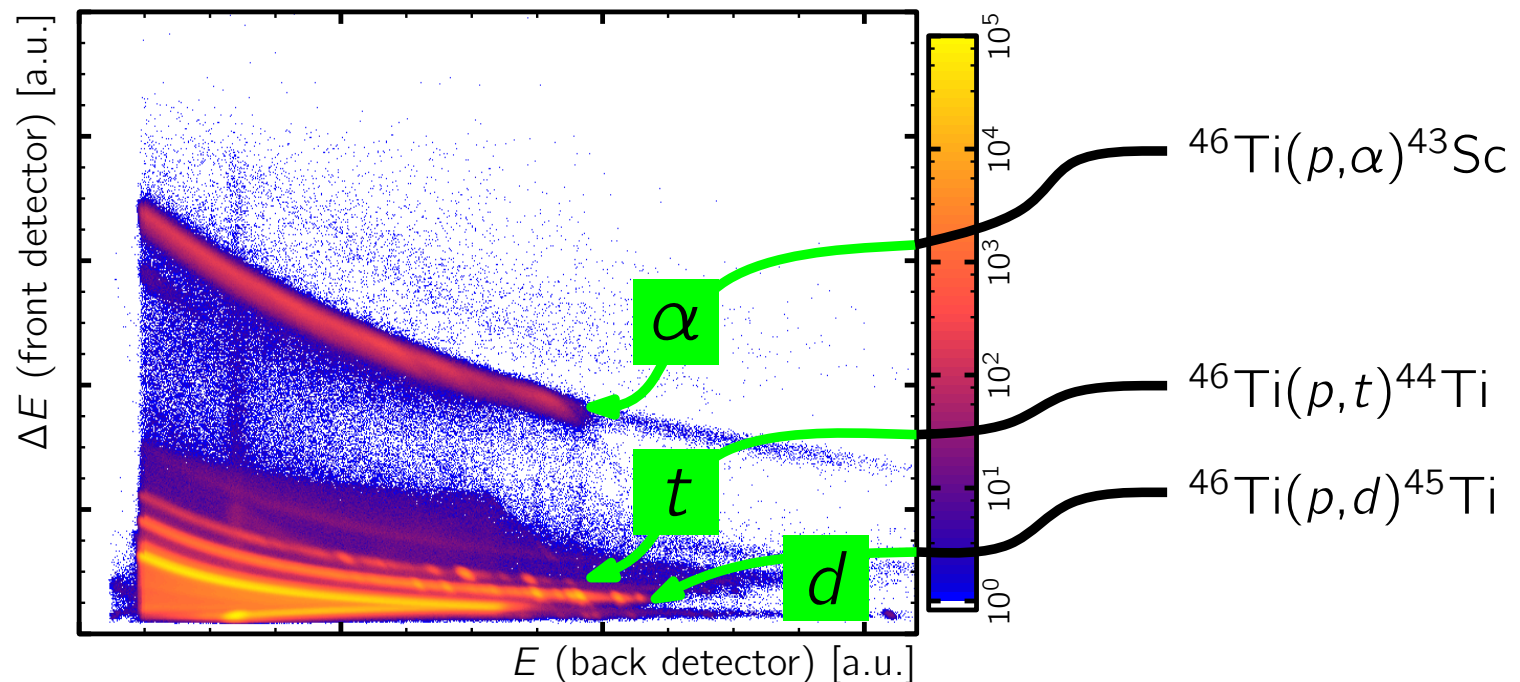
- derive level density and strength function from 1<sup>st</sup> generation spectra
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- solutions can be re-normalized
  - $\rho(E_f) \rightarrow A \exp(\alpha E_f) \rho(E_f)$
  - $\mathcal{T}(E_\gamma) \rightarrow B \exp(\alpha E_\gamma) \mathcal{T}(E_\gamma)$
- $\Rightarrow$  need “external” normalization
  - discrete levels at low energy
  - resonance spacings and  $\gamma$  widths near  $B_n$



# $^{46}\text{Ti}(p, X)$ Experiment

Aim:

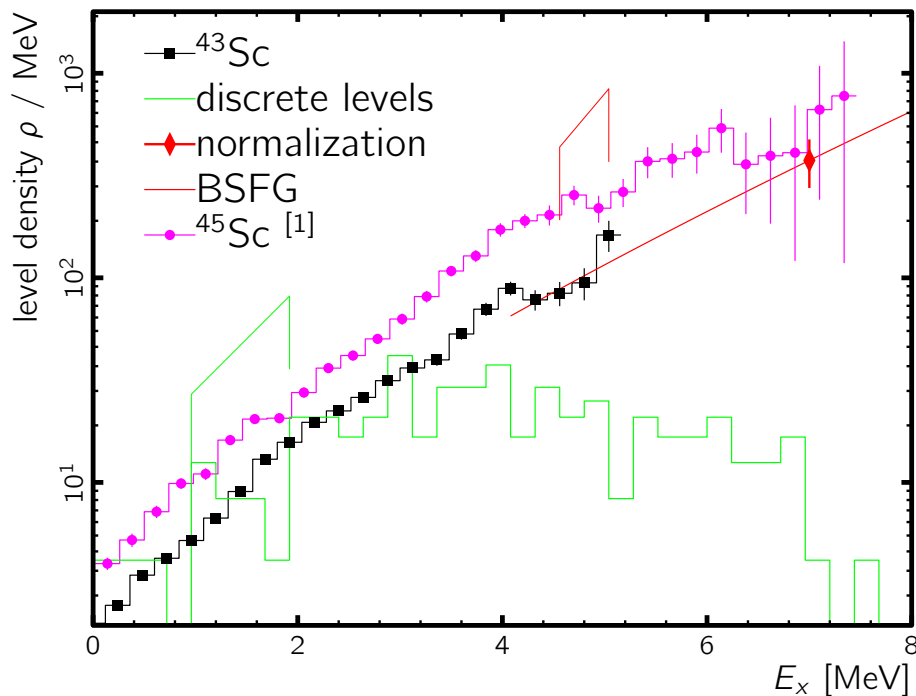
- investigate level density of  $^{44}\text{Ti}$ 
  - astrophysical interest — large  $^{44}\text{Ti}$  abundance not understood
- study other reaction channels, and compare with previous results (e.g.  $(p, \alpha)$  reaction)



# $^{43}\text{Sc}$ Preliminary Level Density

Normalization:

- $p$  resonances at  $B_p + 2 \text{ MeV}$ 
  - distribution of known spins extrapolated for unassigned levels
- discrete levels at  $1 \dots 2 \text{ MeV}$



Comparison with  $^{45}\text{Sc}$ :

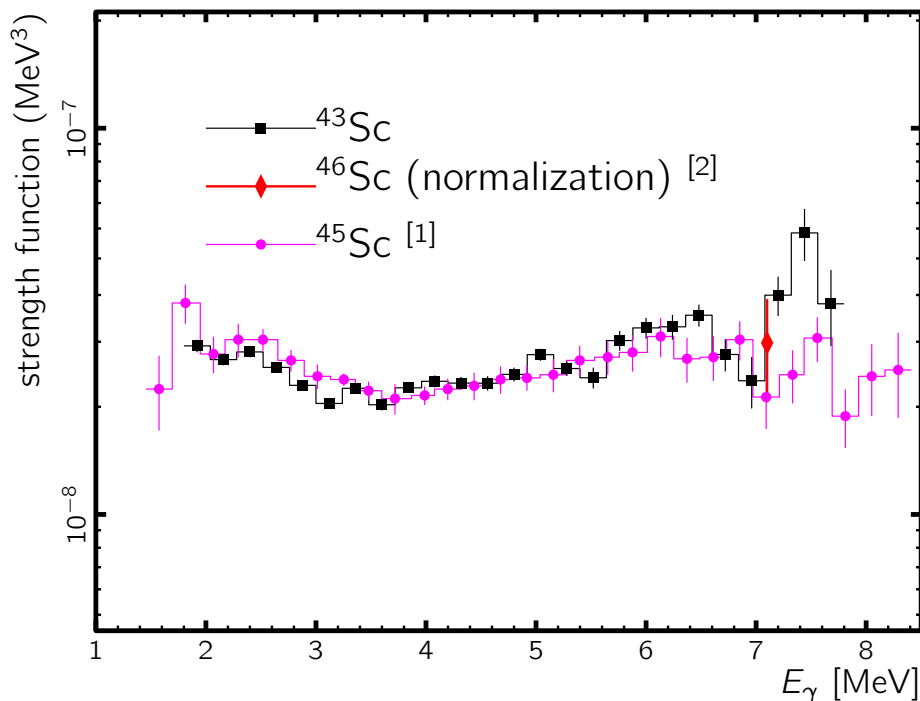
- level density slightly lower
  - usually  $\rho$  very similar for neighbours
  - possible reason: fewer particles outside core — but why at low  $E_x$ ?

[1] A.C. Larsen *et al.*, PRC 76, 044303 (2007)

# $^{43}\text{Sc}$ Preliminary $\gamma$ Strength Function

Normalization:

- no data available for  $^{43}\text{Sc}$
- use  $^{46}\text{Sc}$  (as for  $^{45}\text{Sc}$  in [1])



Comparison to  $^{45}\text{Sc}$ :

- almost identical — different reactions!
  - $^{43}\text{Sc}$ : ( $p, \alpha \gamma$ )
  - $^{45}\text{Sc}$ : ( $^3\text{He}, ^3\text{He}' \gamma$ )
- upbend at low  $E_\gamma$ , minimum at  $E_\gamma \approx 3 \text{ MeV}$ 
  - origin unknown

[1] A.C. Larsen *et al.*, PRC 76, 044303 (2007) [2] RIPL-2

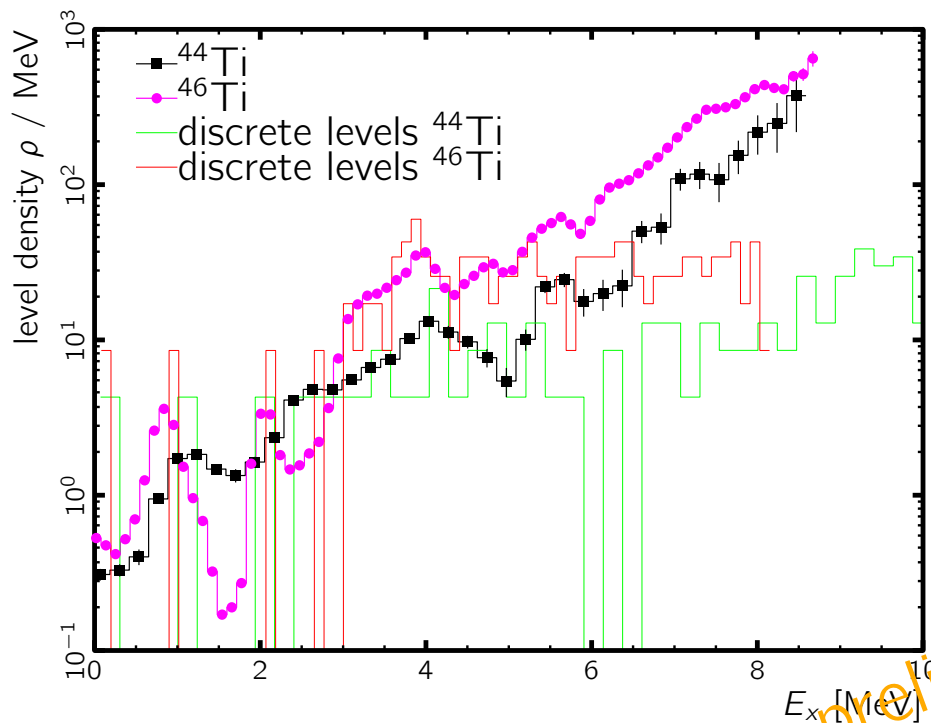


# $^{44,46}\text{Ti}$ Preliminary Results

Ann-Cecilie Larsen

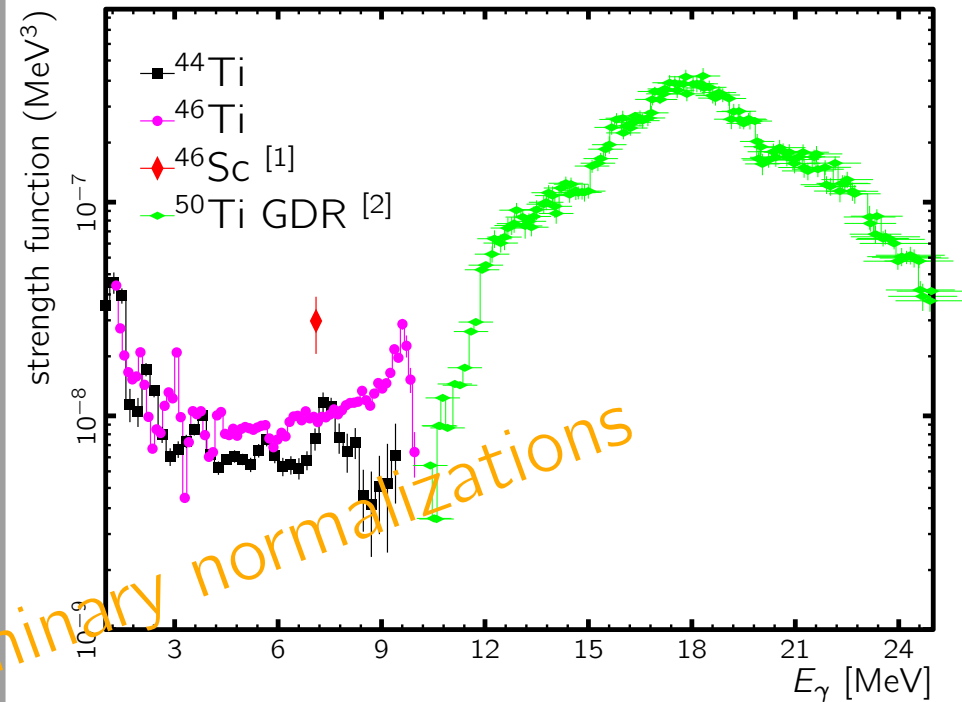
Level density:

- normalized to theoretical value
- very good agreement with discrete levels
- $\rho(^{44}\text{Ti})$  smaller than  $\rho(^{46}\text{Ti})$



Strength function:

- no normalization point yet . . .
- $^{46}\text{Ti}$  seem to match well to the  $^{50}\text{Ti}$  GDR data
- upbend at low  $E_\gamma$



very preliminary normalizations

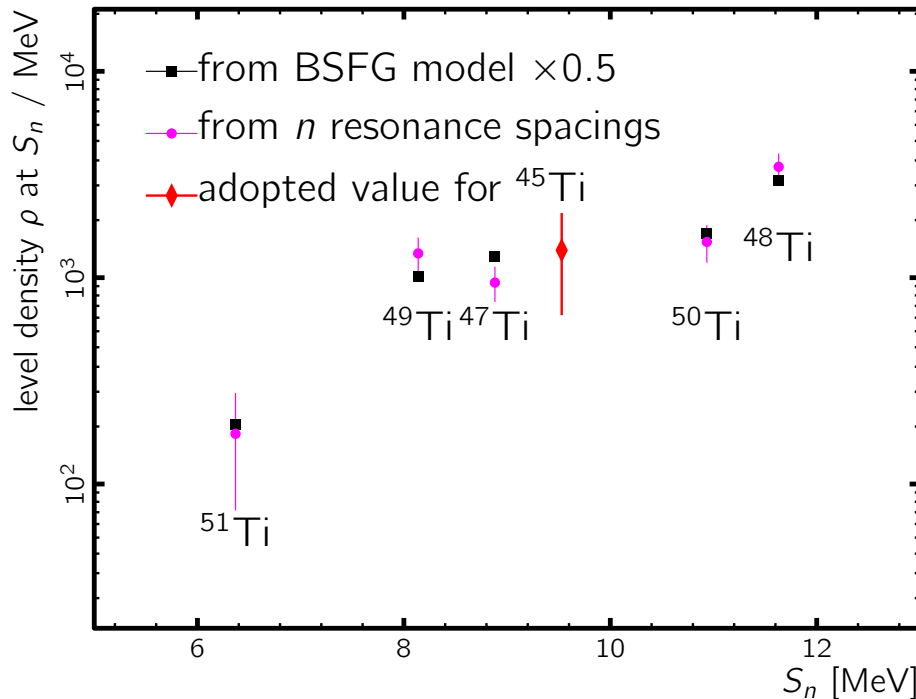
[1] RIPL-2 [2] Pywell *et al.*, NPA 325, 116 (1979)

# $^{45}\text{Ti}$ Level Density

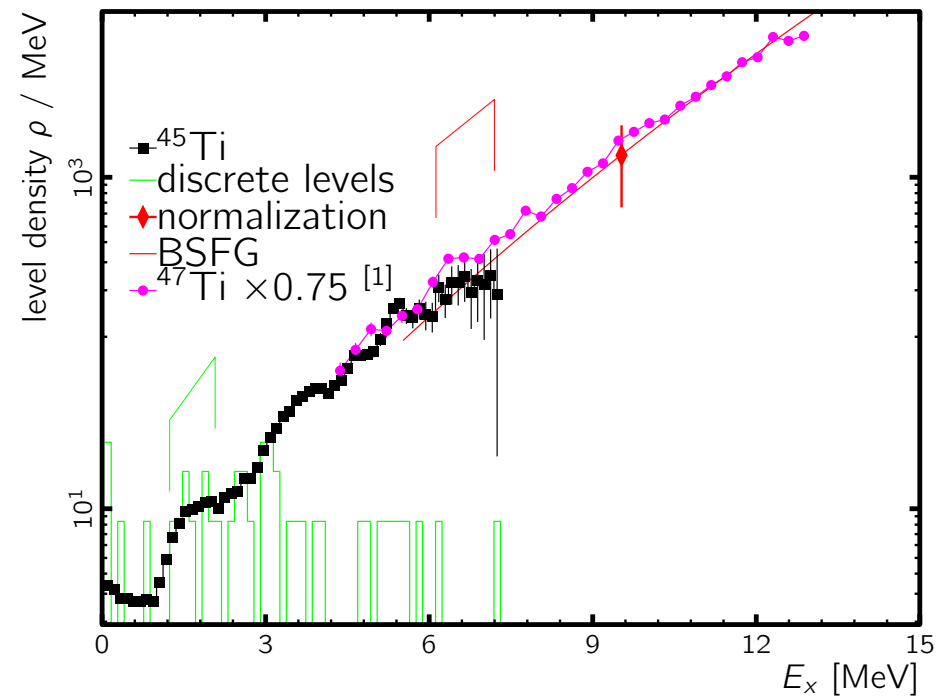
Naeem U.H. Syed *et al.*  
(submitted to PRC)

- normalization at  $B_n$ :
  - no data available for  $^{45}\text{Ti}$
  - derive estimate from neighbouring nuclei
- step structures
  - correspond to pair-breaking

Normalization:



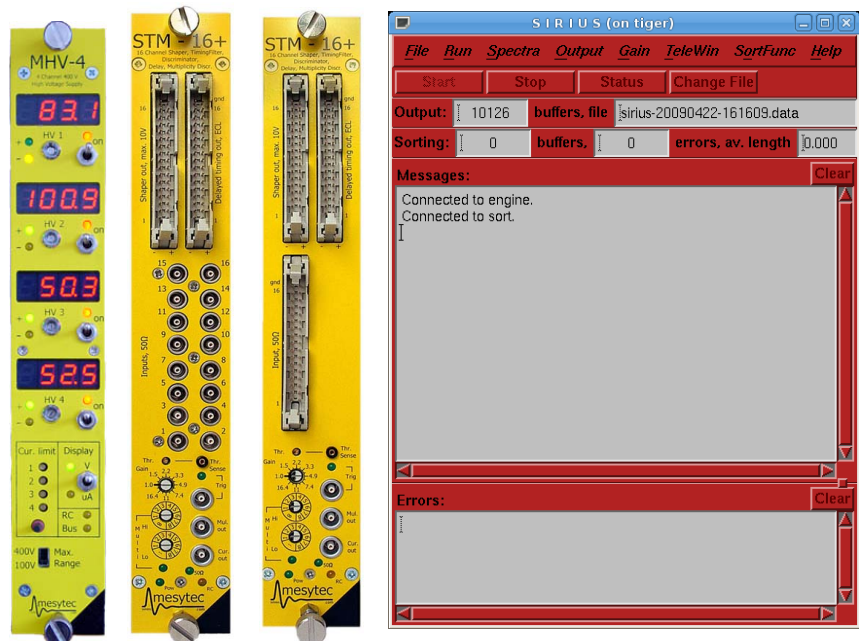
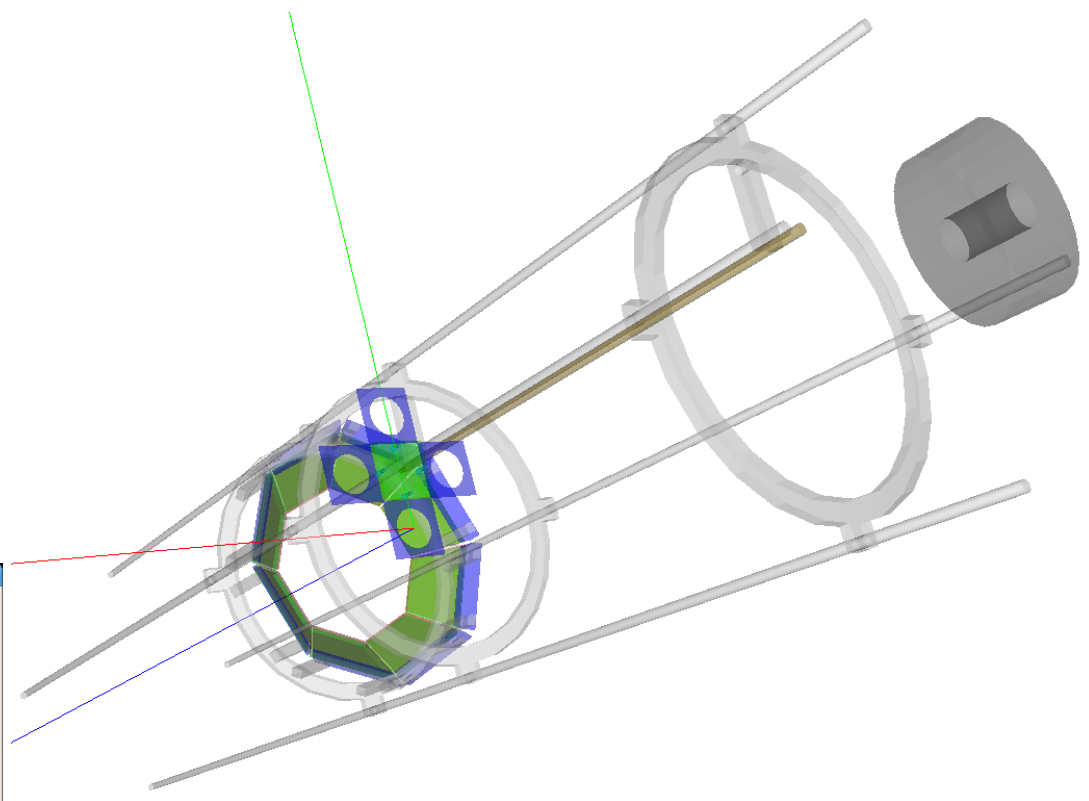
Level density:



[1] A. Voinov *et al.*, PRC 77, 034613 (2008)

# Outlook – New SiRi Detectors

- new Si detectors
  - 8 segments in  $\theta$ , each  $\approx 40^\circ$  coverage in  $\phi$
- new electronics
- updated data acquisition



Come and see it — today 18:00, pizza at the lab!

## Collaboration:

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[M. Guttormsen](#), H. Nyhus, S. Siem  
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Nilsson level scheme  $^{45}\text{Ti}$ 