

**Radiative strength functions  
in deformed nuclei ( $^{162,4}\text{Dy}$ ,  $^{168}\text{Er}$ )  
and population of  $K^\pi=4^+$  isomeric state in  $^{168}\text{Er}$   
from resonance neutron capture**

**Milan Krtička**

CHARLES UNIVERSITY PRAGUE

faculty of mathematics and physics



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IAEA Coordinated Research Project F41032

# Outline

- Experiment and data processing
- Results
  - Radiative Strength Functions and  
“unexpected” fluctuations properties of  $^{162,4}\text{Dy}$  spectra  
*PhD thesis of Standa Valenta*
  - Radiative Strength Functions and  
“very high” population of the isomeric state in  $^{168}\text{Er}$   
*Diploma thesis of Ingrid Knapová*

Other collaborators:

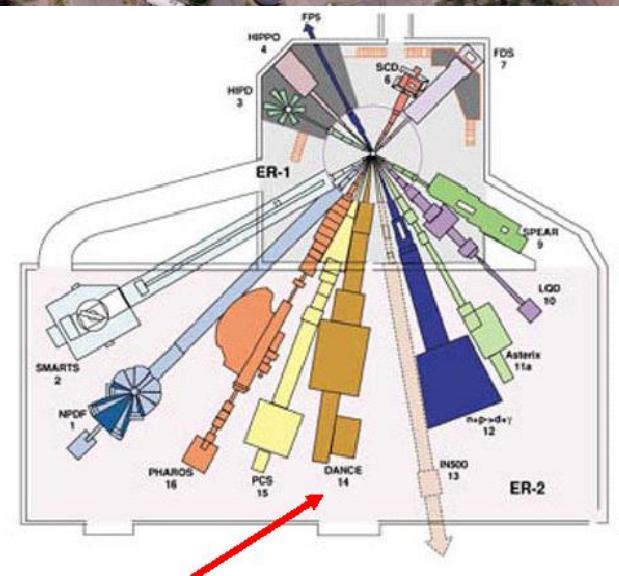
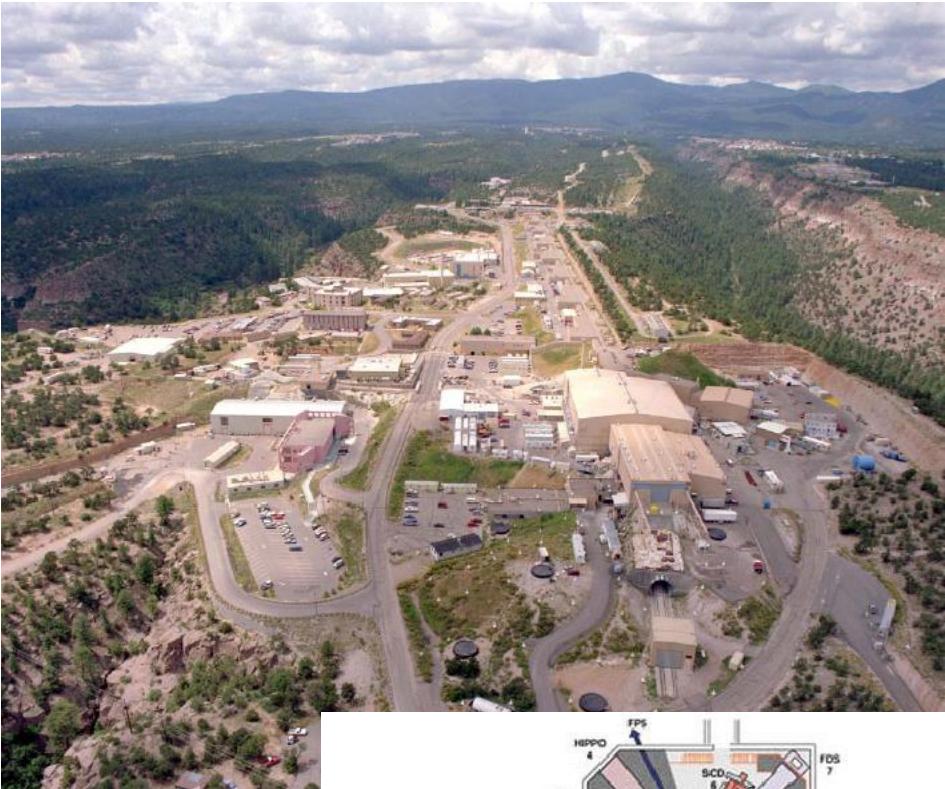
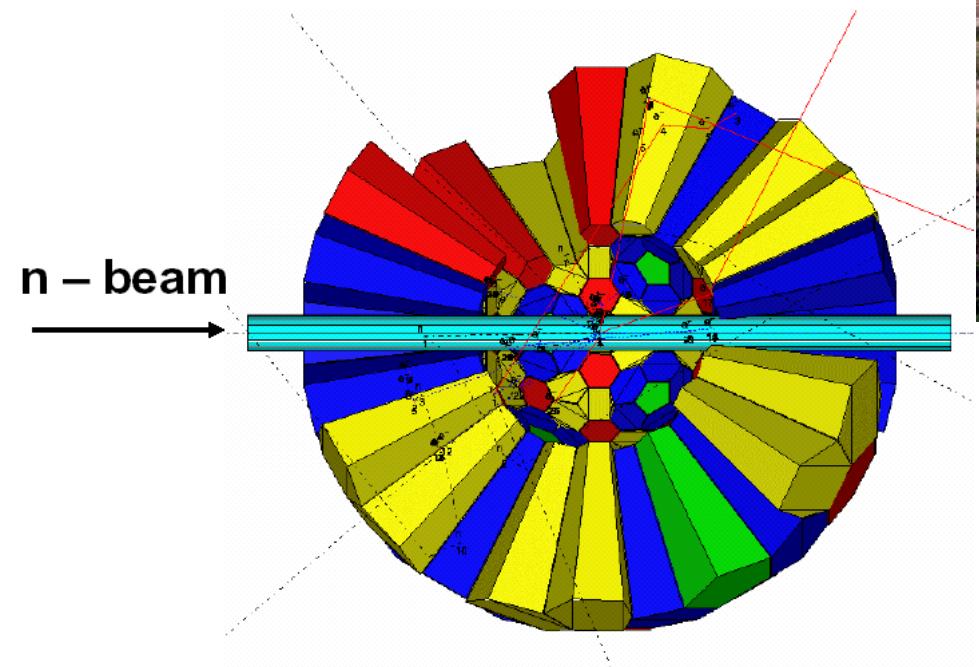
LANL: R.F. Casten, A.J. Couture, J.L. Ullmann, B. Baramsai

Prague: F. Becvar

NCSU: G.E. Mitchell

# Experiment - DANCE @ LANSCE

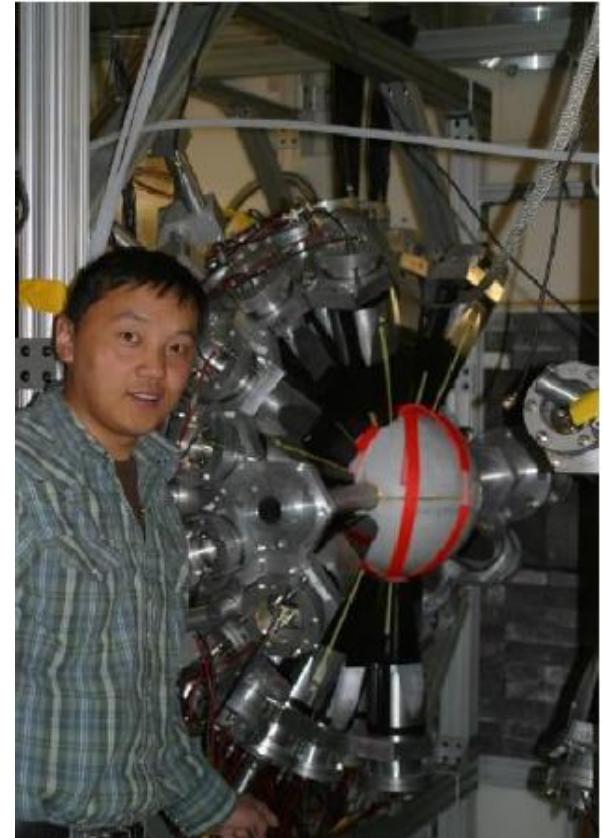
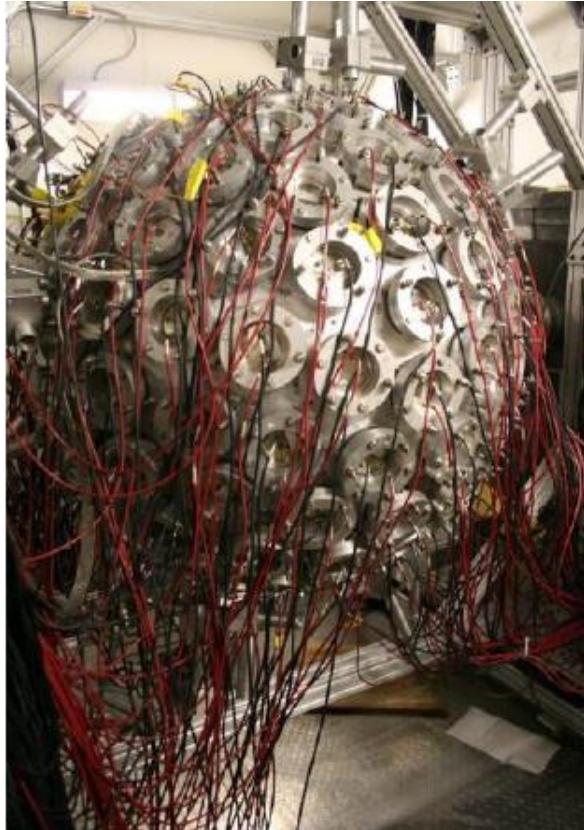
- Moderated W target gives “white” neutron spectrum,  $\sim 14$  n’s/proton
- DANCE is on a 20 m flight path /  $\sim 1$  cm @ beam after collimation
- repetition rate 20 Hz
- pulse width  $\approx 125$  ns
- DANCE consists of 160  $\text{BaF}_2$  crystals



see also talks of J. Ullmann, O. Roig, and N. Bazhazhina

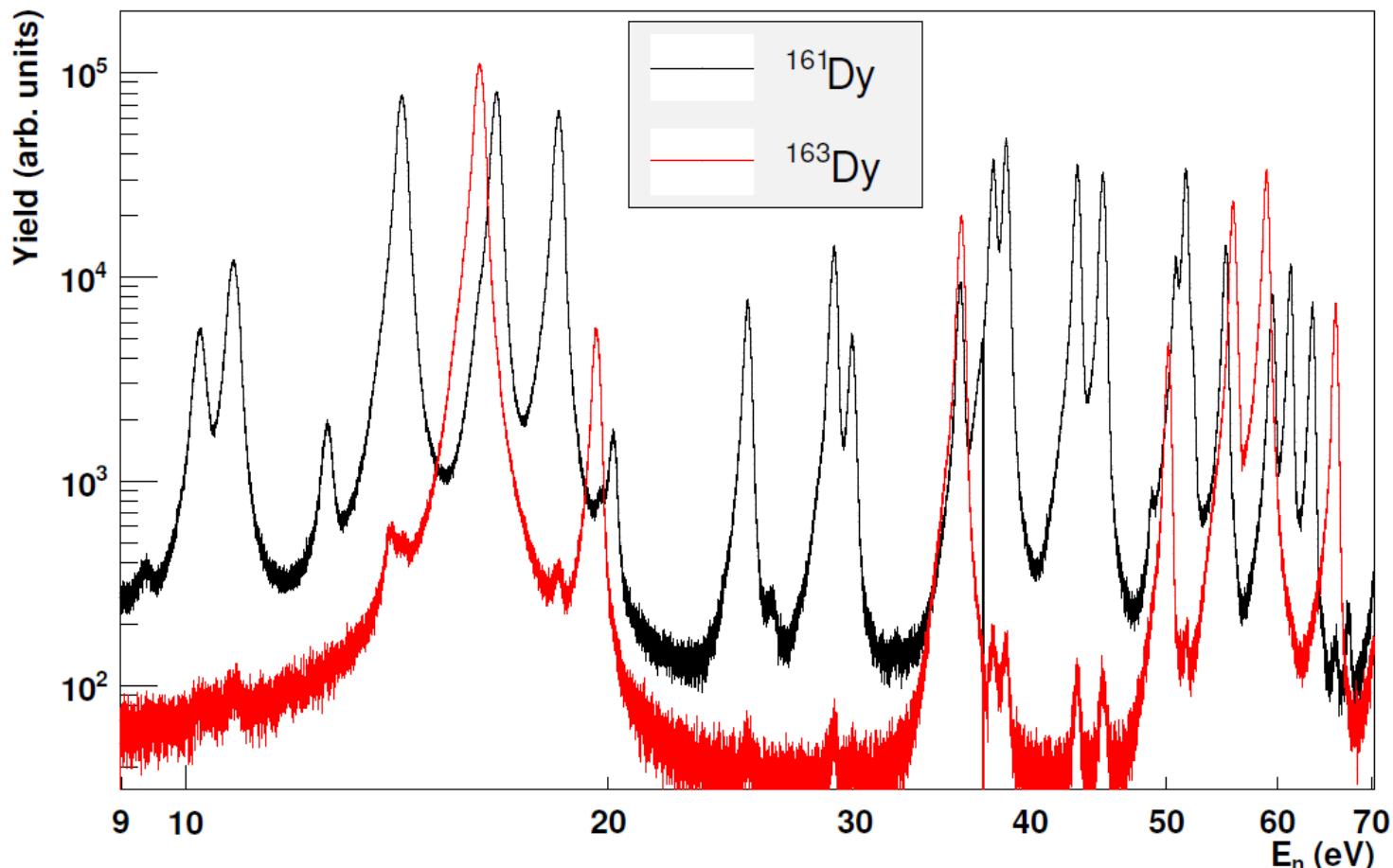
# Experiment

- Radiative neutron capture measured for sub keV region using Detector for Advanced Neutron Capture Experiments (DANCE)  
with aim to study RSF (and perform resonance spin assignment)



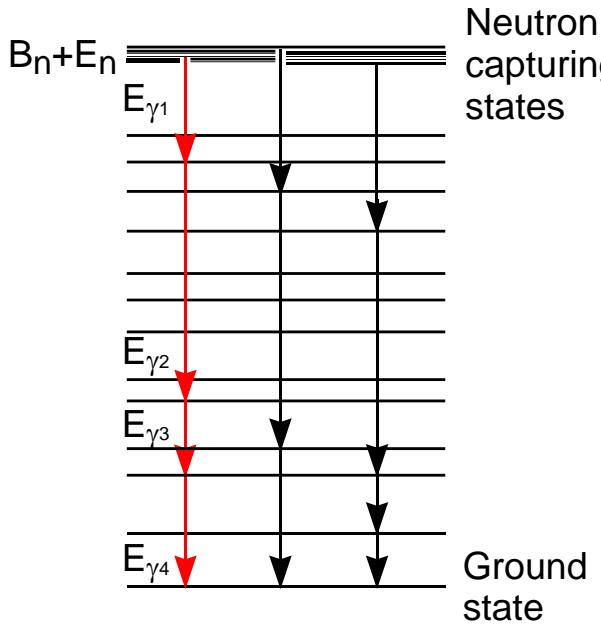
# ToF spectra

Spectra can be obtained from several neutron resonances

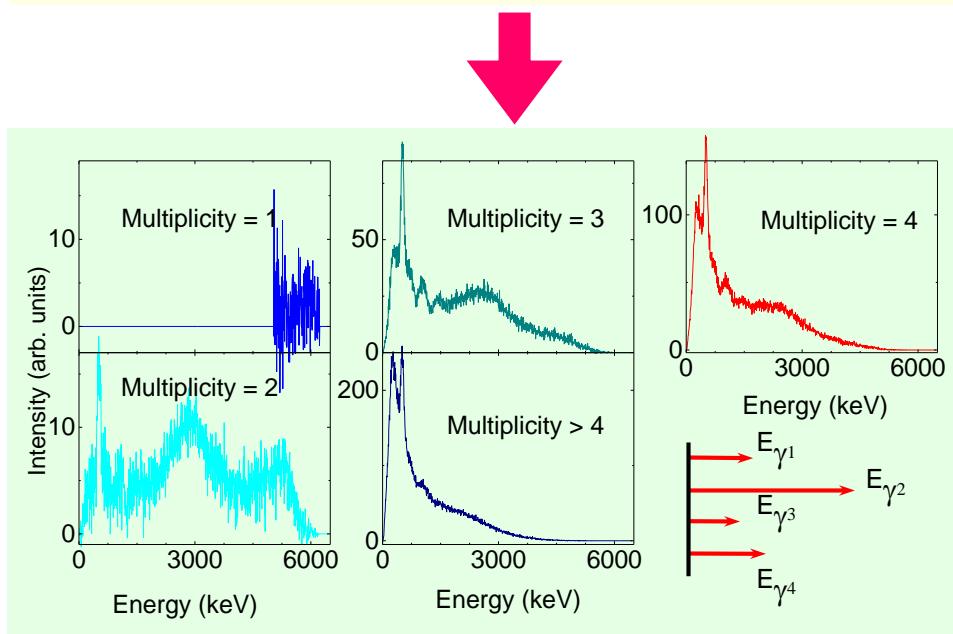
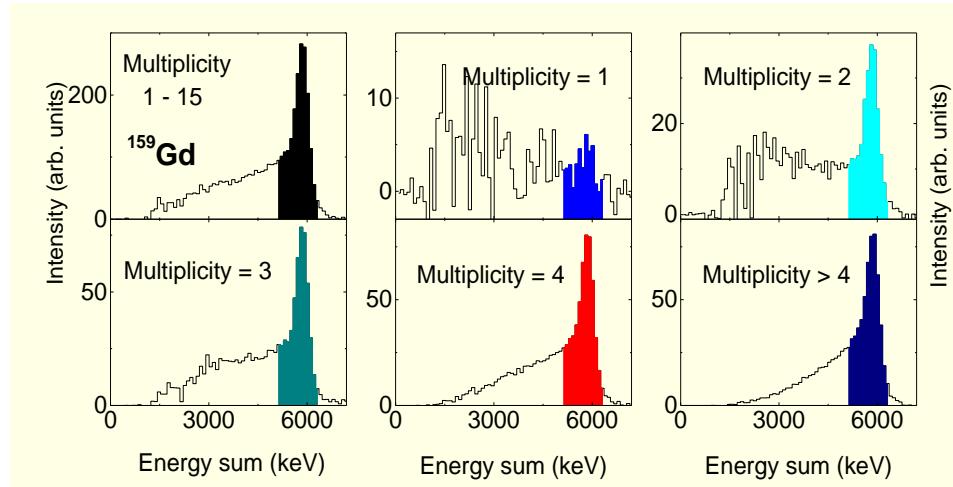


(Narrow) gate on Esum near Sn applied – 800 keV wide cuts

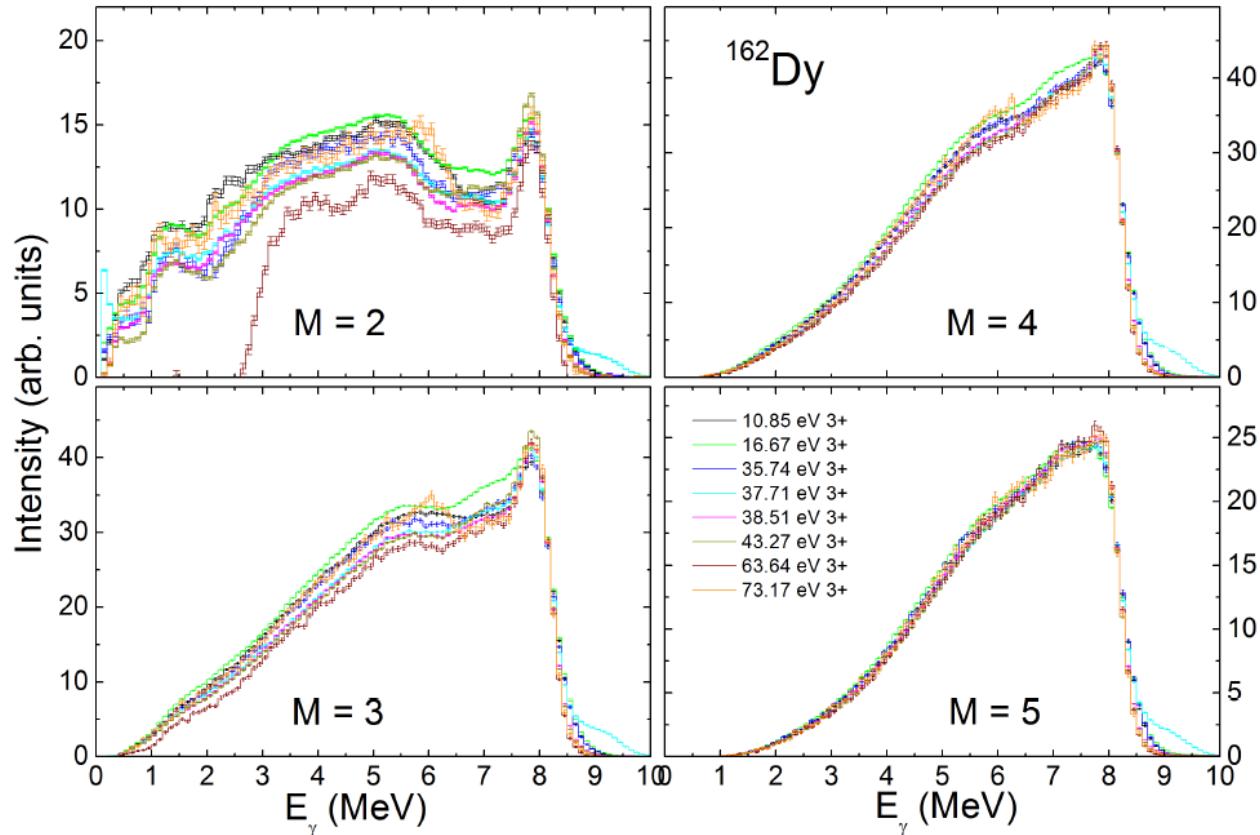
# Spectra of our interest



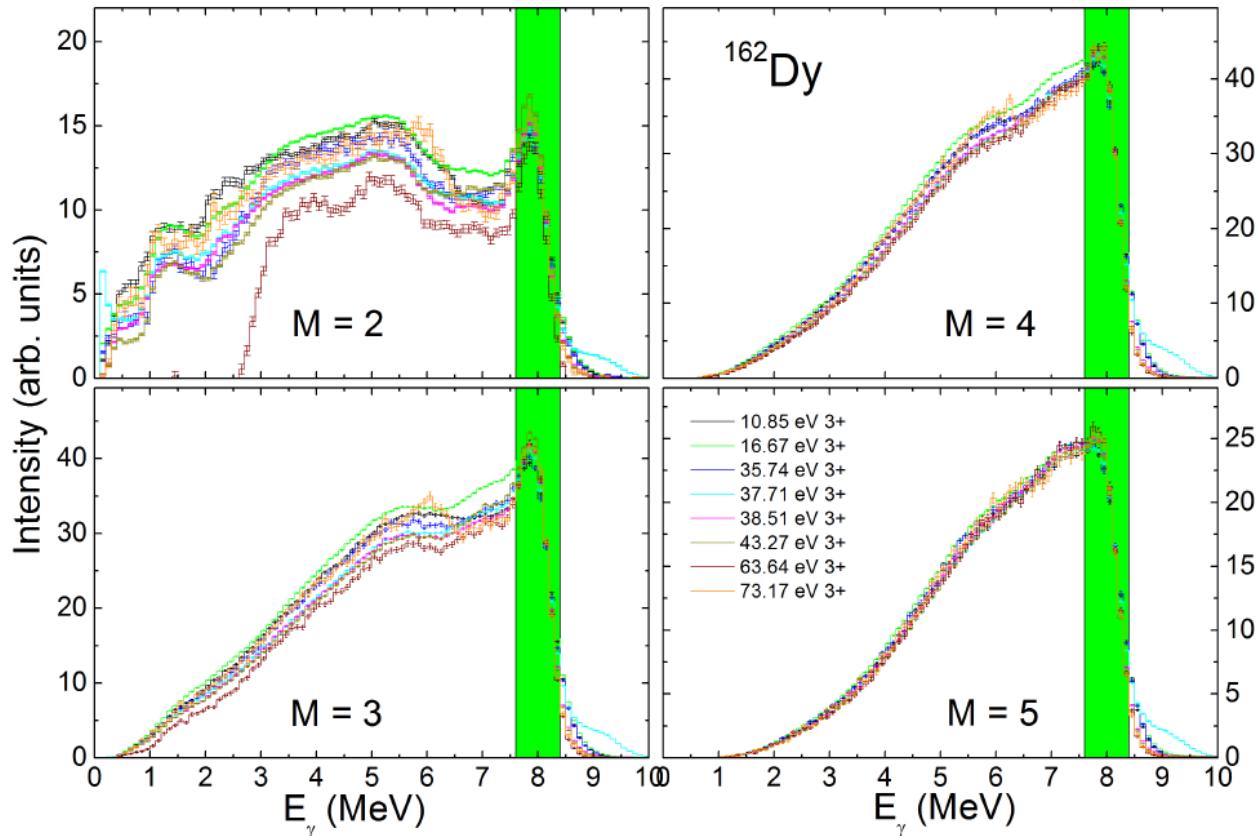
Verification of possible validity of various RSF and NLD models based on comparison of observables – sum-energy and MSC spectra with predictions of simulations based on statistical model of nucleus



# Sum-energy spectra

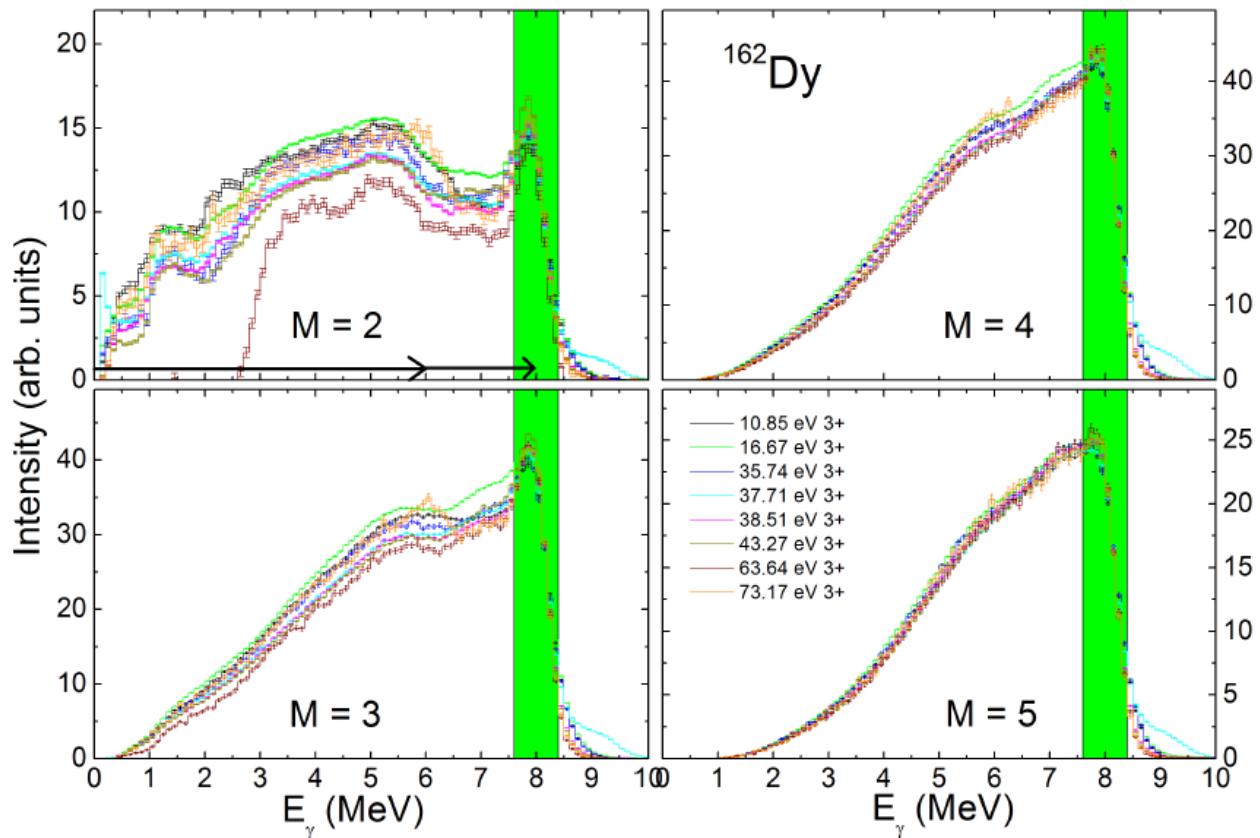


# Sum-energy spectra

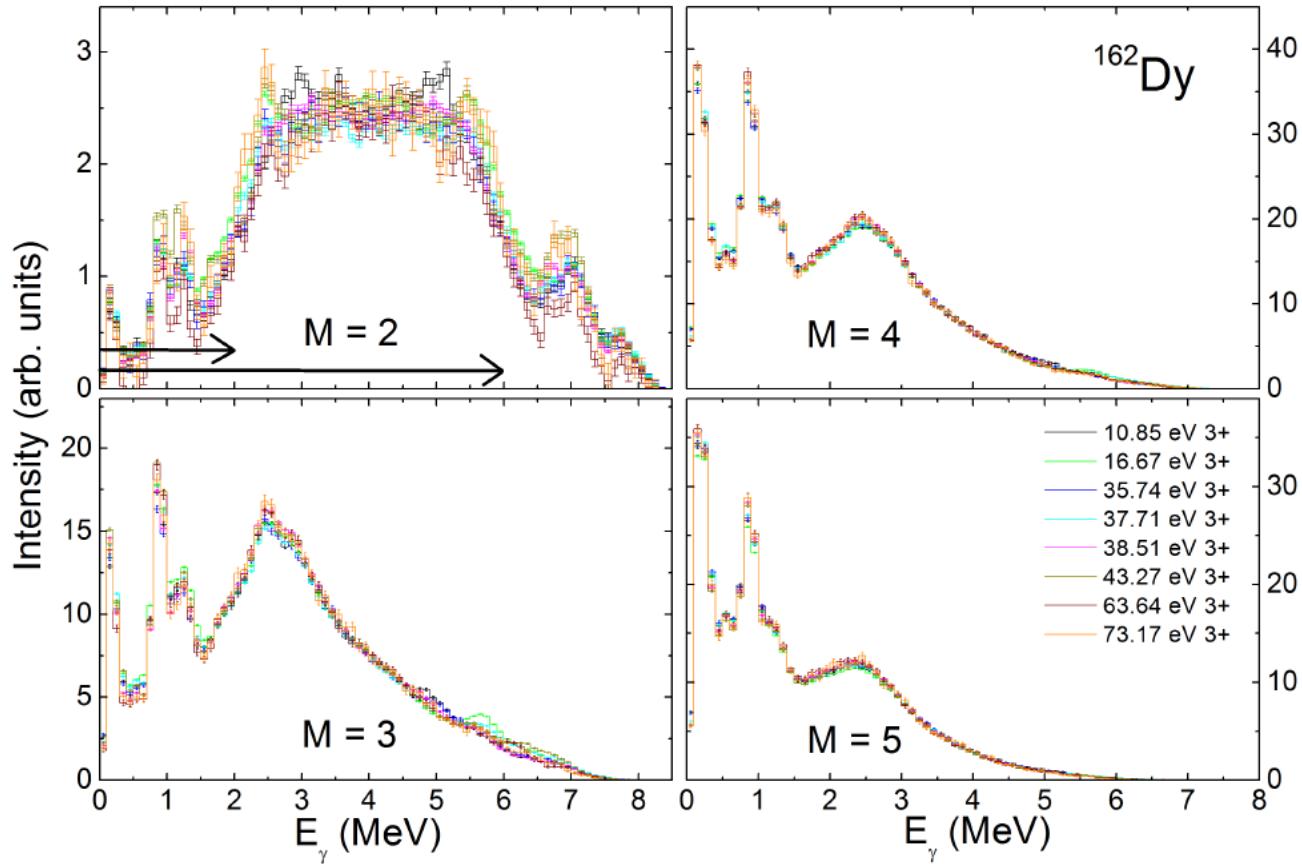


Normalization to the same number of events in  $M=2-7$   
in sum-energy peak (highlighted area)

# Sum-energy spectra



# MSC spectra



Spectra obtained for “many” well-isolated resonances

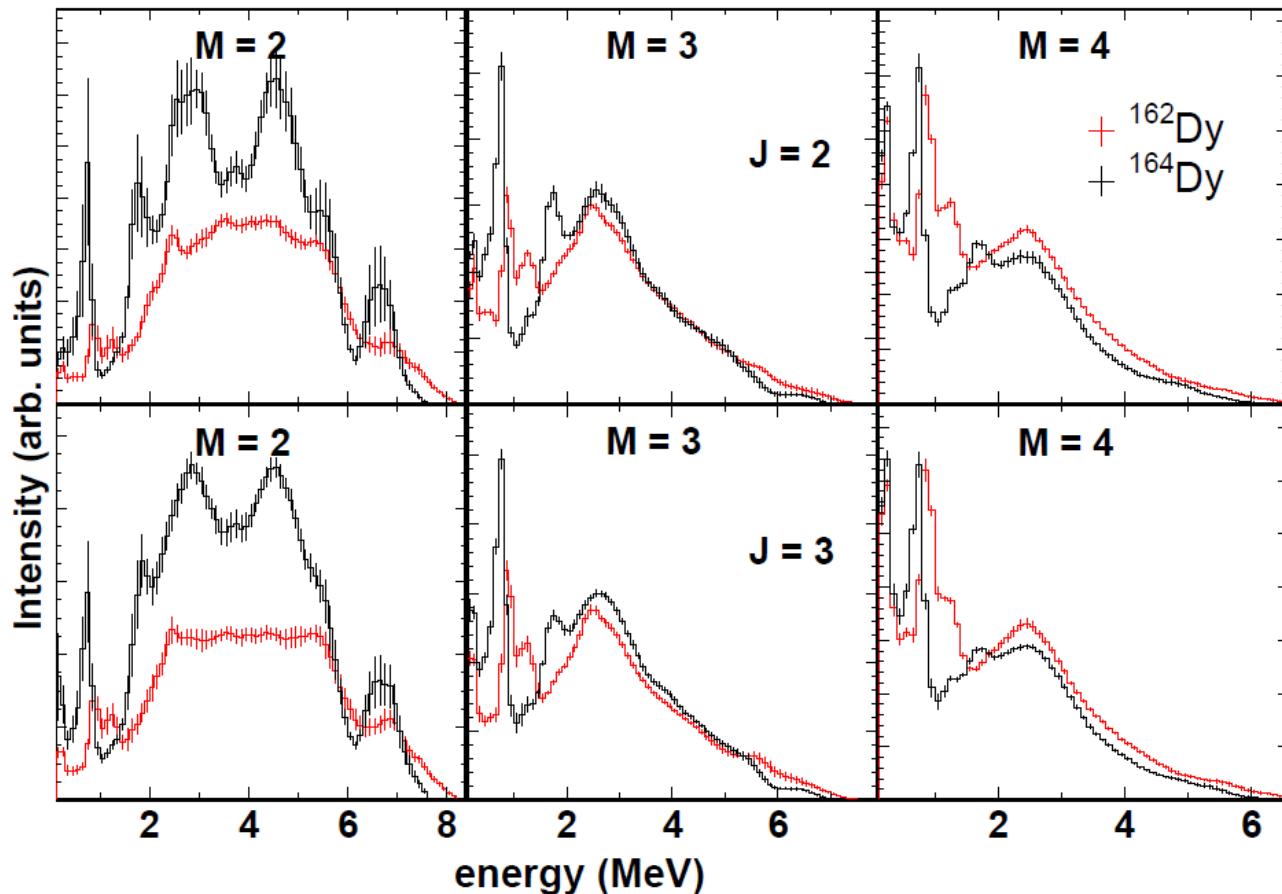
$^{161}\text{Dy}(n,\gamma)$ : 25x  $J^\pi = 2^+$ , 22x  $J^\pi = 3^+$

$^{163}\text{Dy}(n,\gamma)$ : 14x  $J^\pi = 2^-$ , 26x  $J^\pi = 3^-$

At least some checks of fluctuation properties become possible

# “Average” MSC spectra

Distribution of resonances - mean and variance – can be obtained by different approaches (**simple averaging**, weighted averaging, estimate of distribution parameters from Maximum-likelihood method)



Different resonance parities:

positive in  $^{162}\text{Dy}$   
( $S_n = 8.2 \text{ MeV}$ ),

negative in  $^{164}\text{Dy}$   
( $S_n = 7.65 \text{ MeV}$ )

# Data processing

- Experimental spectra come from a complicated interplay between radiative strength functions (RSFs) and level density (LD)
- Complicated detector response to each cascade

⇒ Comparison of predictions based on statistical model simulations with experimental counterparts

- Cascades generated using statistical model of  $\gamma$  decay (using DICEBOX code)
- Detector response (GEANT4) applied to each  $\gamma$  cascade

# Simulation of $\gamma$ cascades - DICEBOX

## Main assumptions:

- For nuclear levels below certain “critical energy” spin, parity and decay properties are known from experiments
- Energies, spins and parities of the remaining levels are assumed to be a random discretization of an *a priori* known level-density formula
- A partial radiation width  $\Gamma_{i,f}^{(XL)}$ , characterizing a decay of a level  $i$  to a level  $f$ , is a random realization of a chi-square-distributed quantity the expectation value of which is equal to

$$f^{(XL)}(E_\gamma) E_\gamma^{2L+1} / \rho(E_i),$$

where  $f^{(XL)}$  and  $\rho$  are also *a priori* known

- Selection rules governing the  $\gamma$  decay are fully observed
- Any pair of partial radiation widths  $\Gamma_{i,f}^{(XL)}$  is statistically uncorrelated

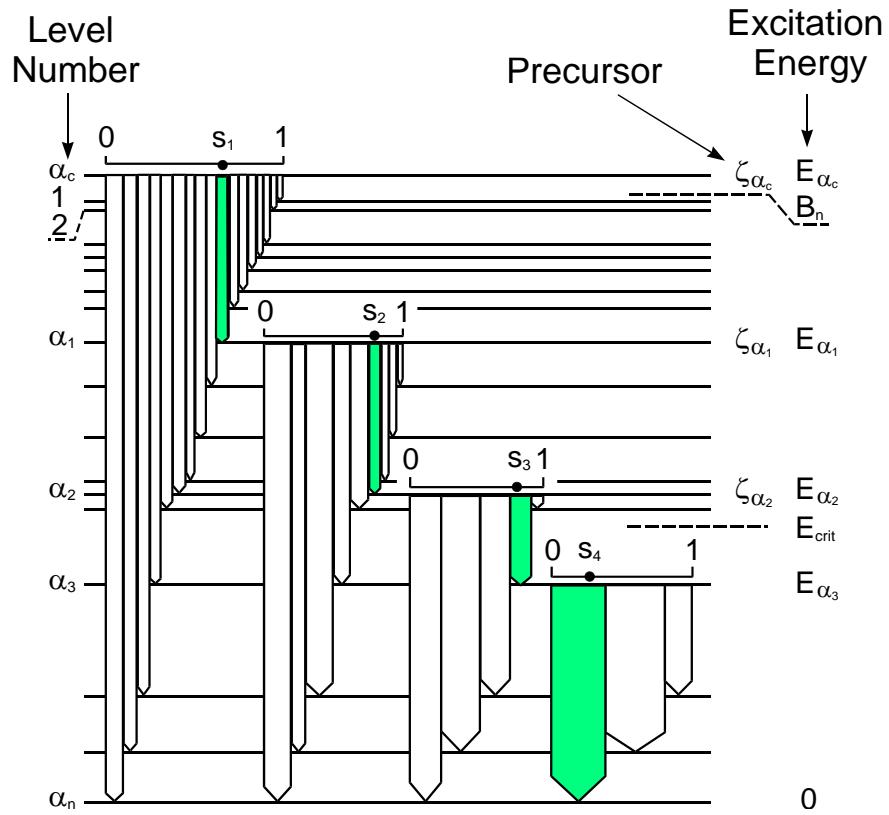
# DICEBOX – Statistical decay simulations

Modelling of the decay:

- “nuclear realization”  
( $10^6$  levels  $\Rightarrow 10^{12} \Gamma_{\lambda\gamma f}$ )
- “precursors” are introduced
- comparable quantities  
(shapes of spectra, multiplicity, population of low-lying levels, shapes of TSC spektra) are „integral“ quantities
- fluctuations originating from nuclear realizations cannot be suppressed

Outcomes from modelling are compared with experimental data

Deterministic character of random number generators is exploited



# Main features of DICEBOX - fluctuations

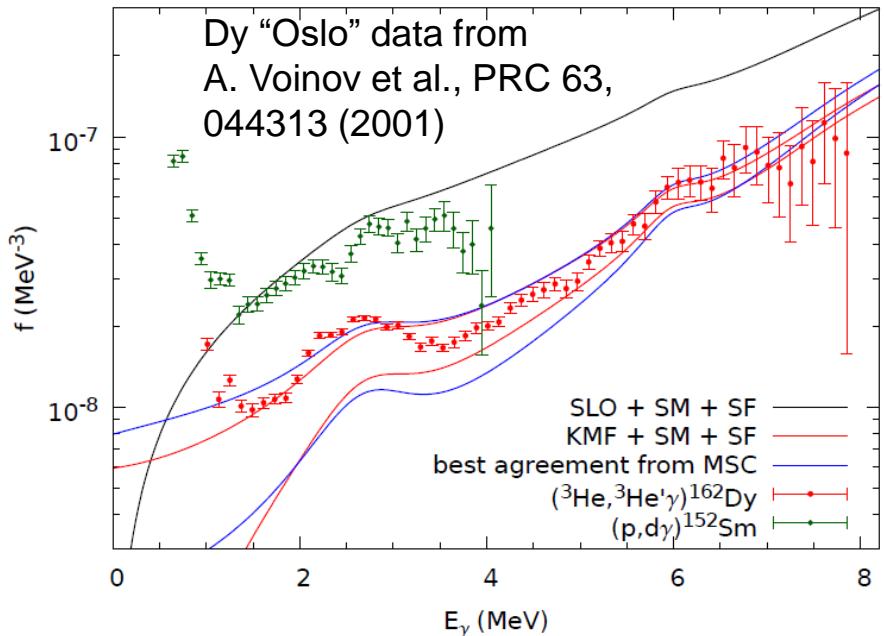
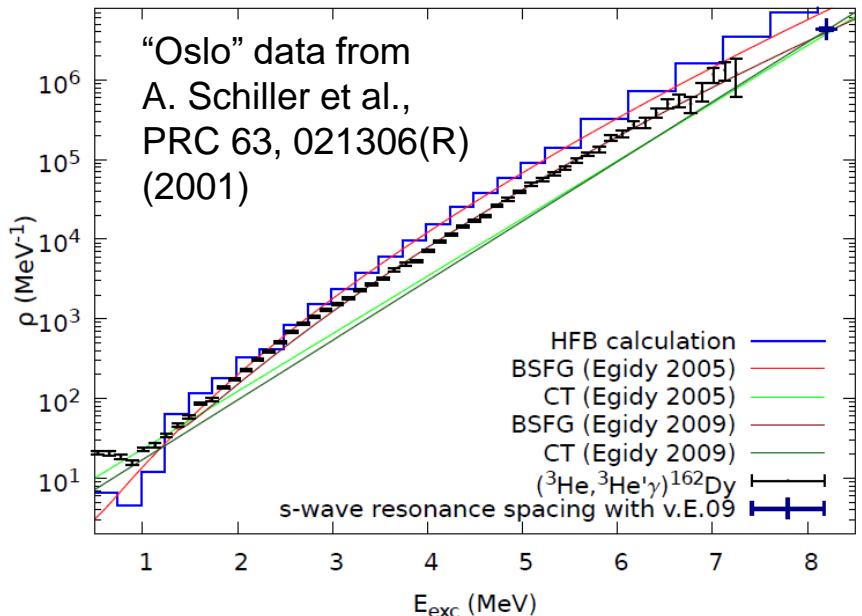
- Infinite number of artificial nuclei (nuclear realizations) can be obtained for the same set of level density and RSFs models – nuclear realizations differ in exact number of levels and intensities of transitions between each pair of them  
⇒ leads to different predictions from different nuclear realizations
- DICEBOX allows us to treat predictions from different nuclear realizations, i.e. expected fluctuations
- The size of fluctuations depends on the (observable) quantity and nucleus
- Majority of results (sum-energy and MSC spectra) insensitive to absolute values of RSFs but only to energy dependence of RSFs and their “composition” (E1, M1)

# Analysis of Dy data

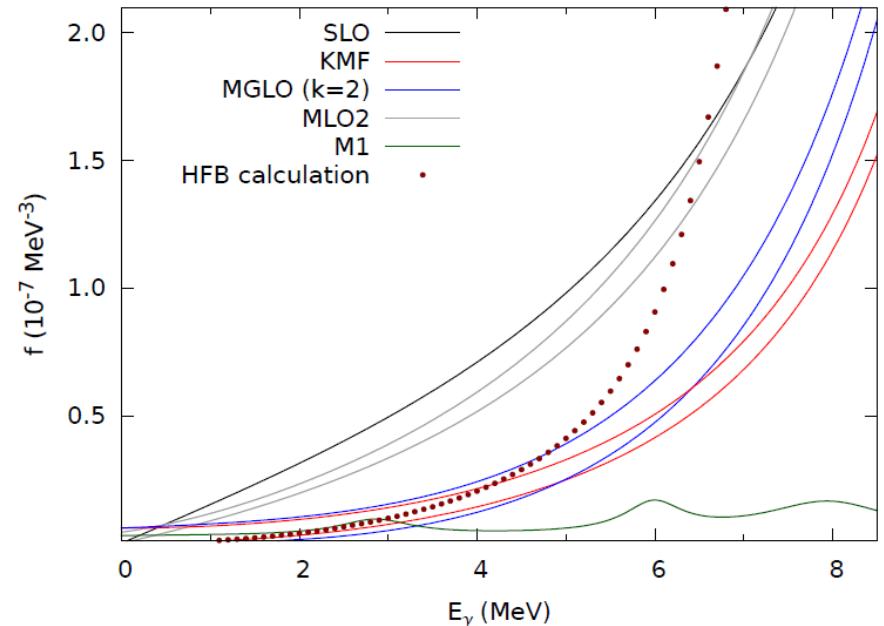
Dy – first nuclei in RE region, with data from NRF, Oslo and DANCE

Many different RSF and LD models tested in simulations

- LD – BSFG and CTF
- RSF – all models listed in RIPL-3 + some additional models



Sm data from A. Simon et al., PRC 93, 034303 (2016)

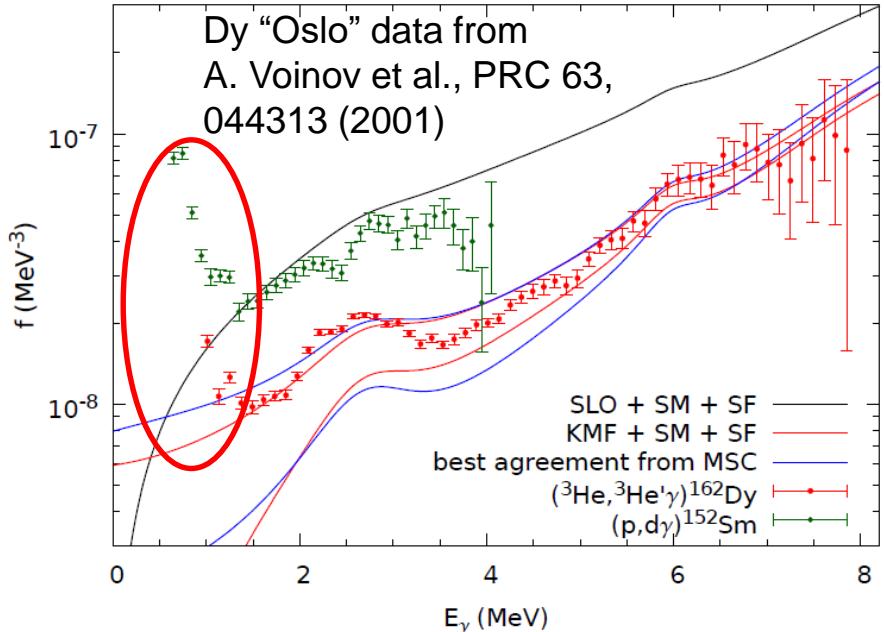
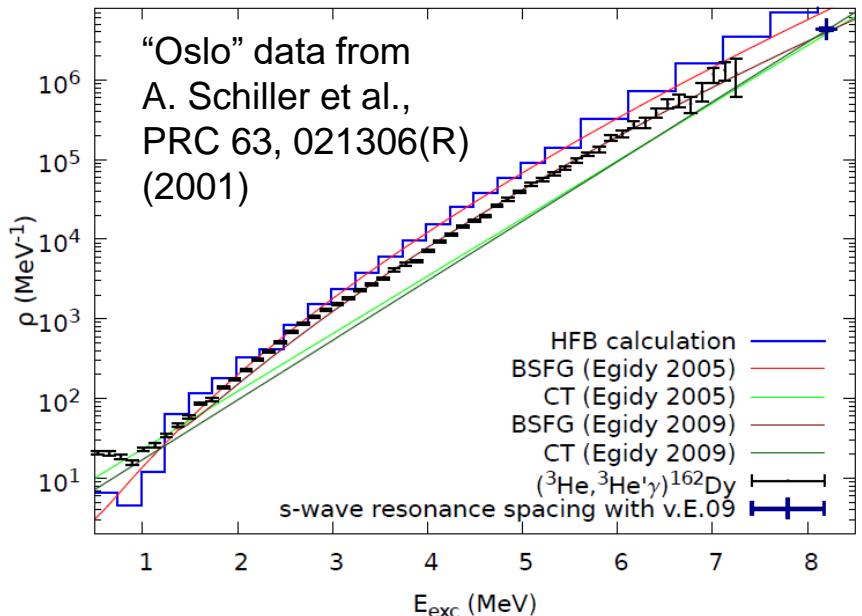


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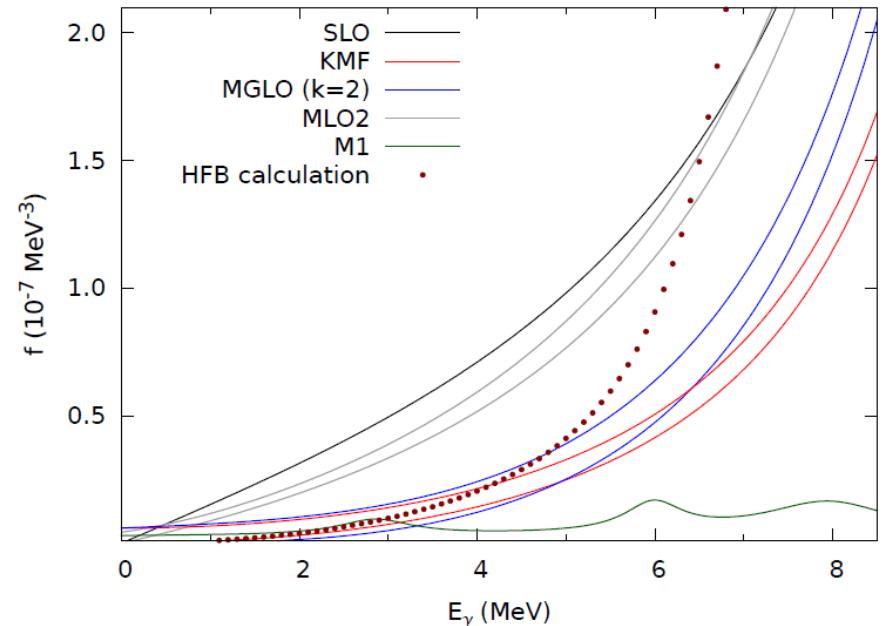
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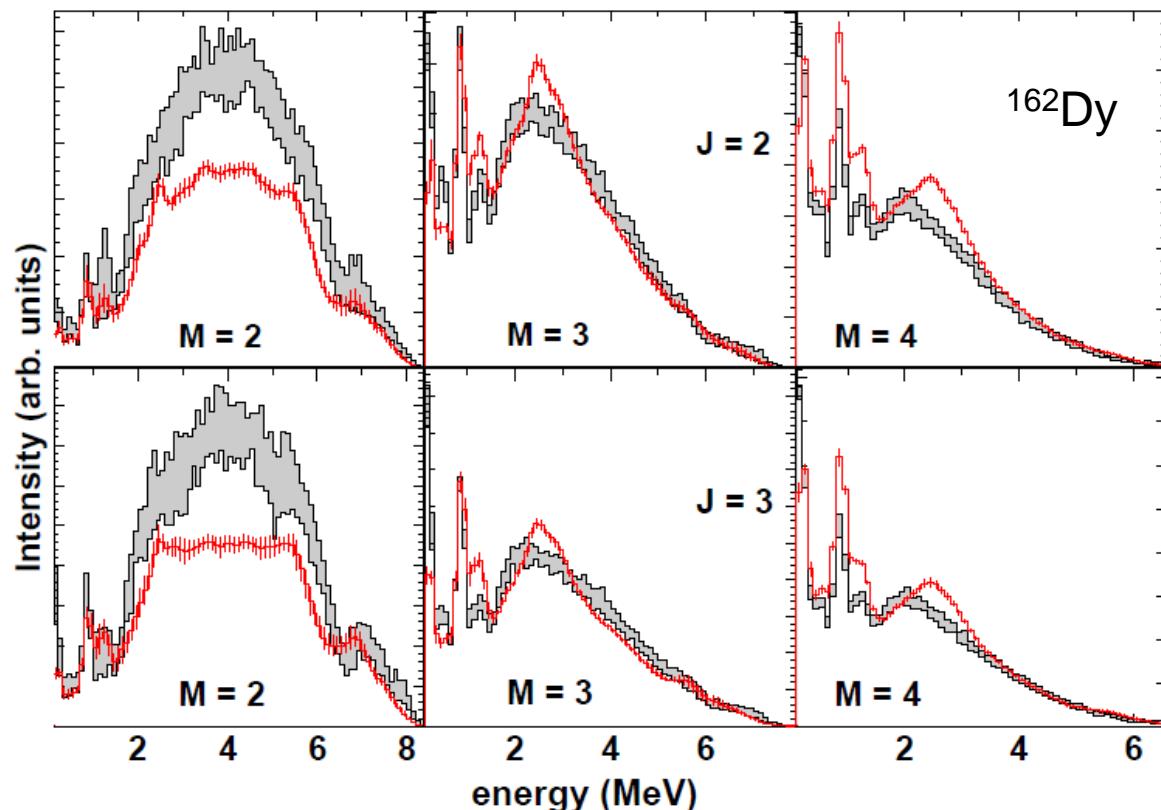


# Results - Dy

- Two different spins
- Different parity of resonances ( $^{162}\text{Dy} \times ^{164}\text{Dy}$ )
- Validity of many models can be rejected

# Results - Dy

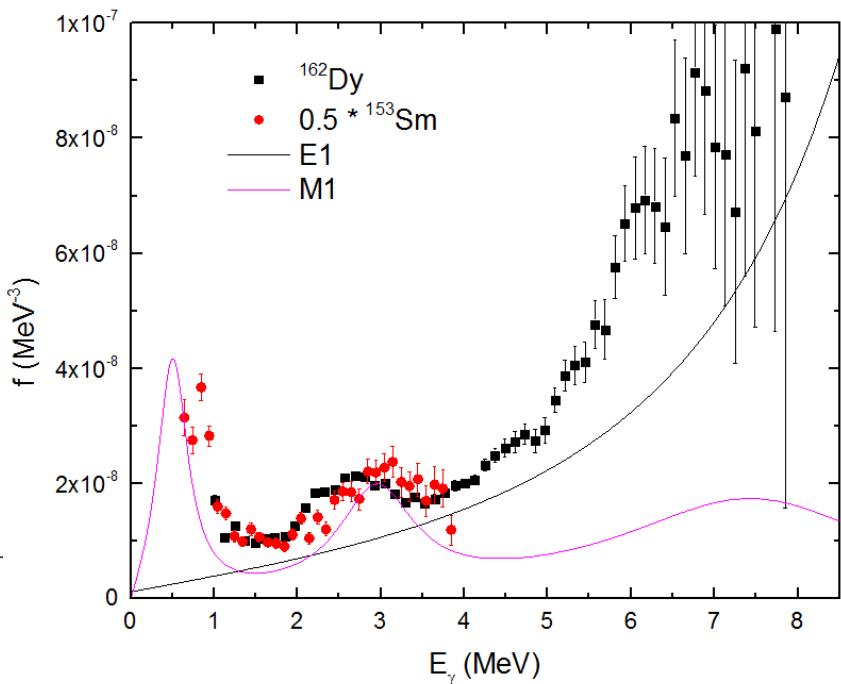
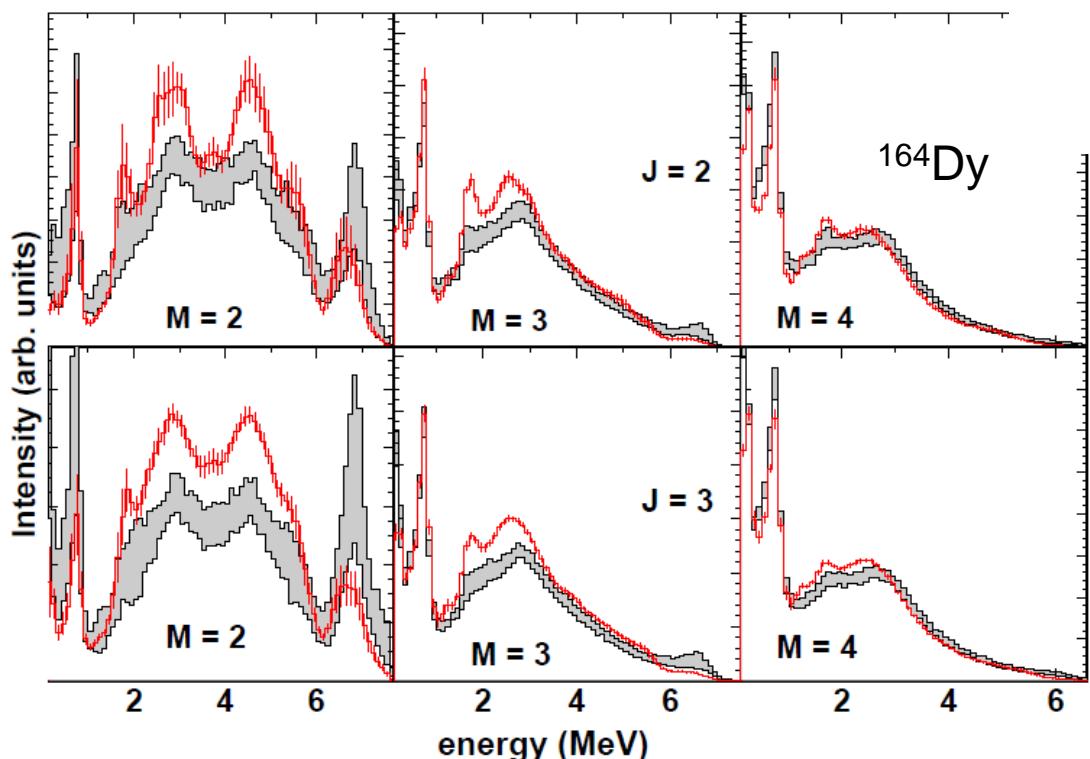
- Resonance near 3 MeV has to be postulated also for primary transitions and has to be of M1 character (scissors mode)
- E1 character of the resonance structure not consistent with data;  
 $E_{SM} = 2.8\text{-}3.0 \text{ MeV}$ ,  $\Gamma_{SM} = 1.0\text{-}1.4 \text{ MeV}$



No scissors mode assumed

# Results - Dy

- A low-energy RSF enhancement was tested
- “Very conservative low-energy enhancement” describing data from  $^{152,154}\text{Sm}(p,d\gamma)$  is unable to reproduce spectra

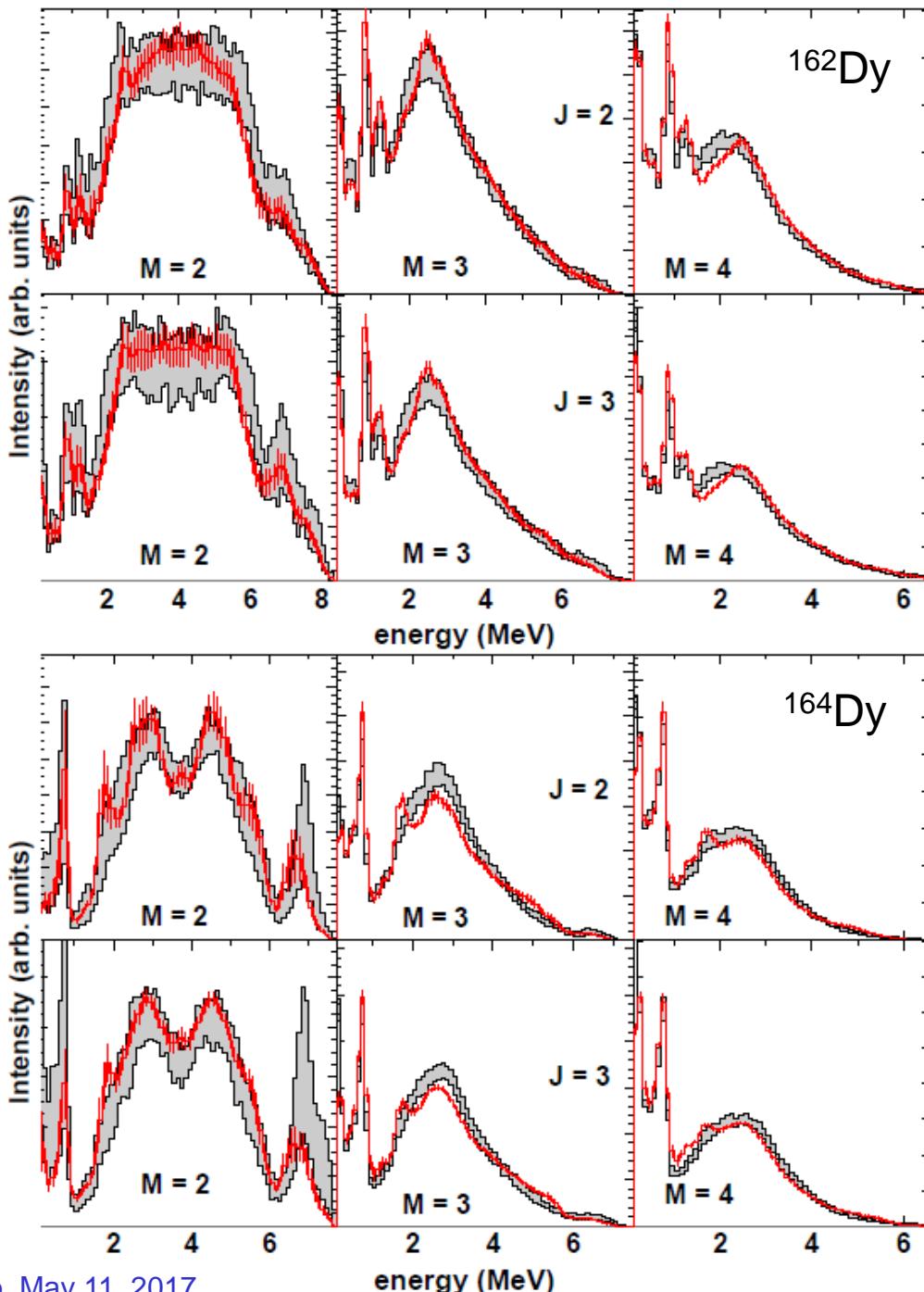


Dy data: A. Voinov et al.,  
PRC 63, 044313 (2001)

Sm data: A. Simon et al.,  
PRC 93, 034303 (2016)

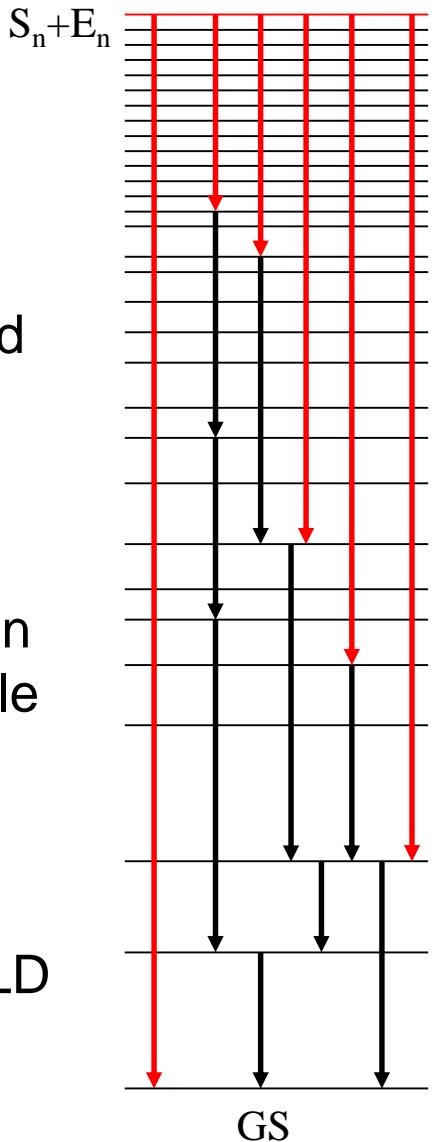
# Results - Dy

- Good agreement obtained with models “similar but not exactly the same” as Oslo models
- It is difficult to reproduce both isotopes with exactly the same RSF model – especially taking into account total radiation width



# Expected fluctuations

- Different “sources” of fluctuations in simulations
- In a real nucleus, the fluctuations come only from intensities of primary transitions – all levels below neutron resonances and secondary intensities are fixed
- Unfortunately, we do not know which realization of the decay scheme is realized in nature
- So far, simulations made with different level schemes in each simulated artificial nucleus – CPU time reasonable
- Is such an approach correct?
- For Dy nuclei we have made for the first time (time-consuming) tests for fixed levels below capturing state and intensities of secondary transitions (for two RSF+LD combinations)

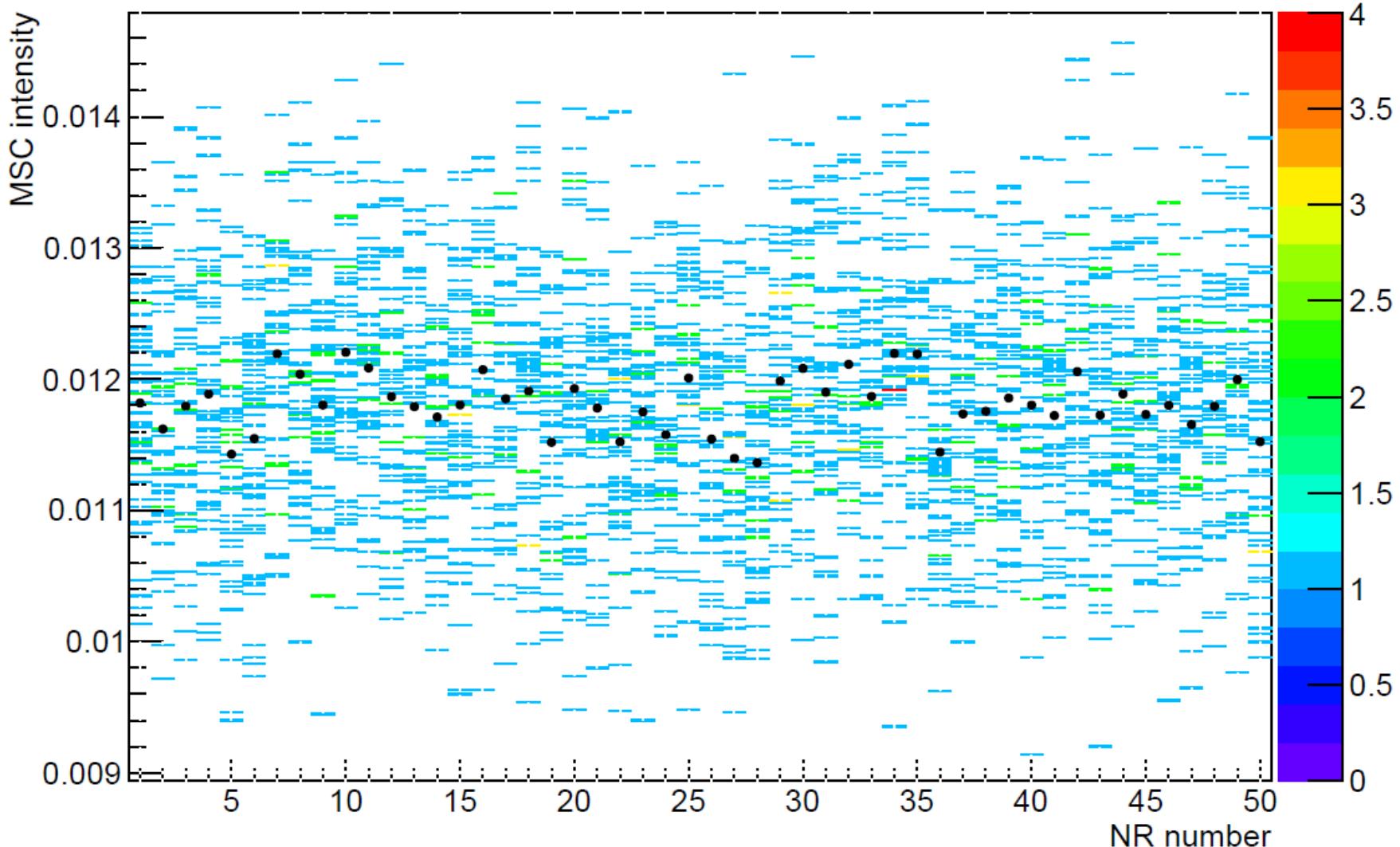


# Findings related to widths of distribution

## Results from simulations

- For chosen combination of RSFs and LD, fluctuations due to primary transitions do not strongly depend on actual choice of the level scheme – we can reasonably well separate fluctuations due to (i) “unknown level scheme” and (ii) “fluctuation of primary intensities”
- For all bins via region of “high level density” the fluctuations of type (ii) are higher than that of type (i), usually dominantly – perfect justification of the comparison used in all previous RE nuclei

# Different fluctuation sources



50 different nuclear resonances (NR) in a bin in MSC M=2 spectrum  
For each, 50 different realizations of primaries simulated

# Findings related to widths of distribution

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- **Results can strongly depend on the isotope (mass, LD) but should be similar in nuclei in the same mass range (similar LD)**

# Findings related to widths of distribution

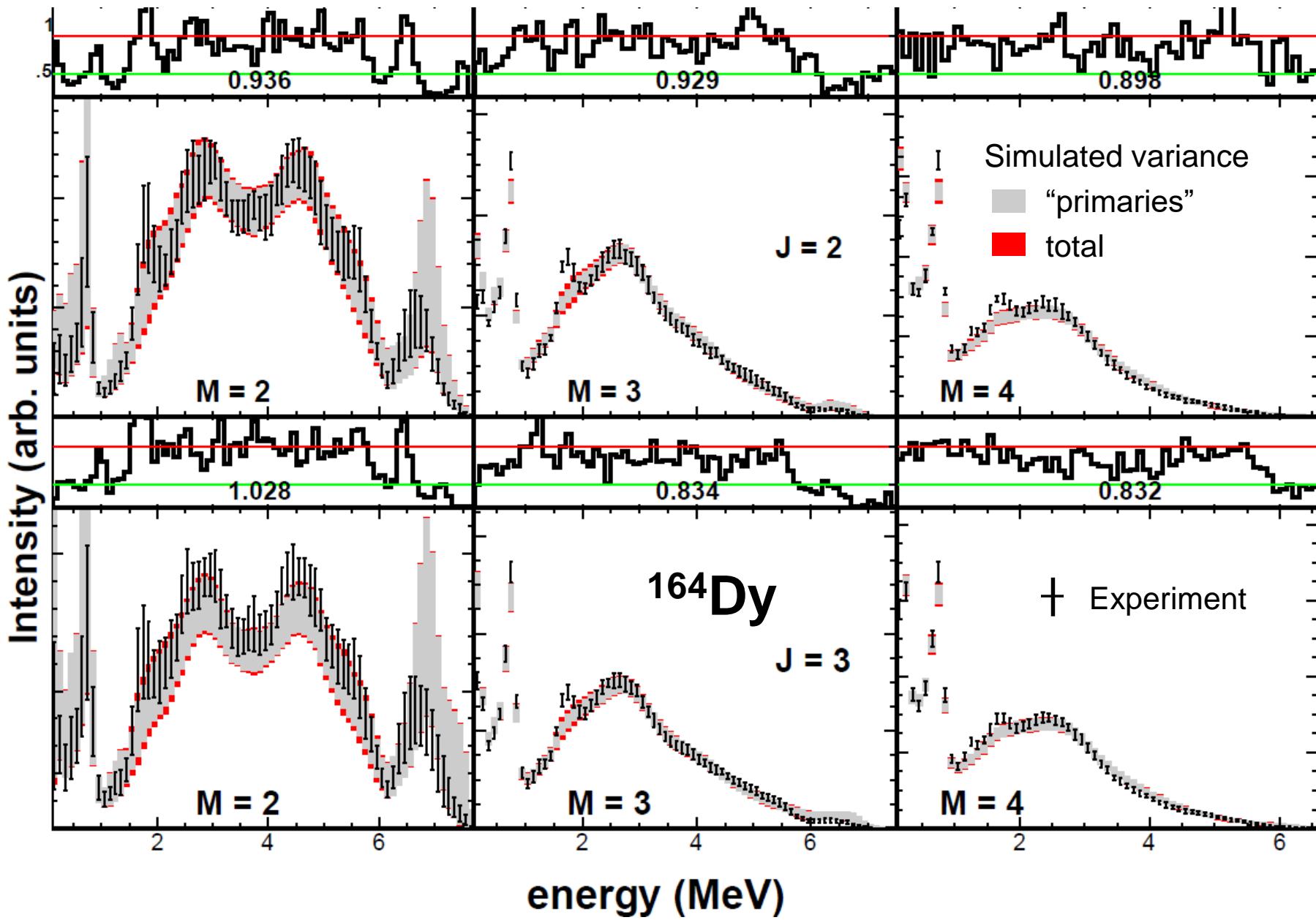
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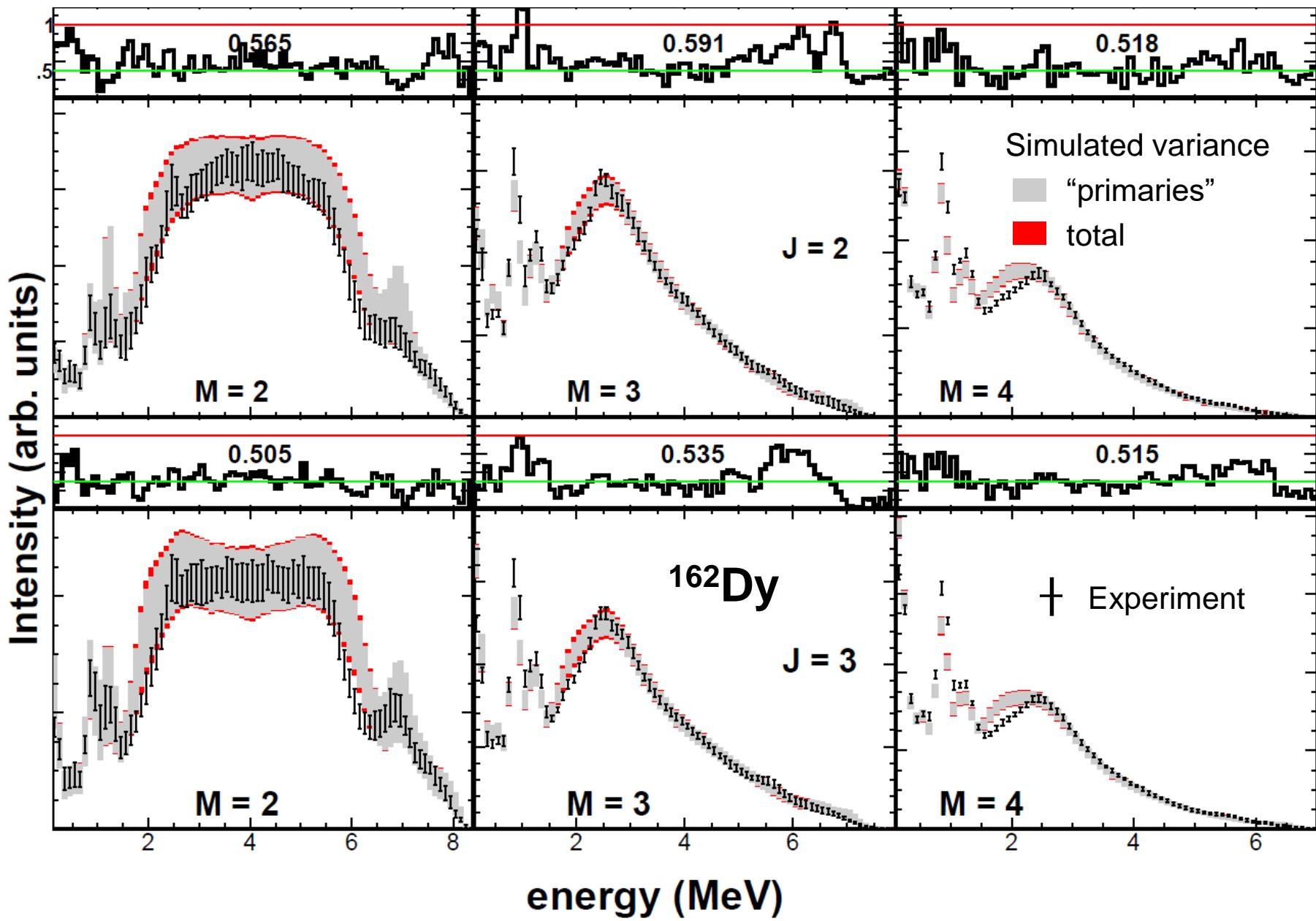
## Comparison between experiment and simulations

- Results are rather puzzling

# Comparison of distributions



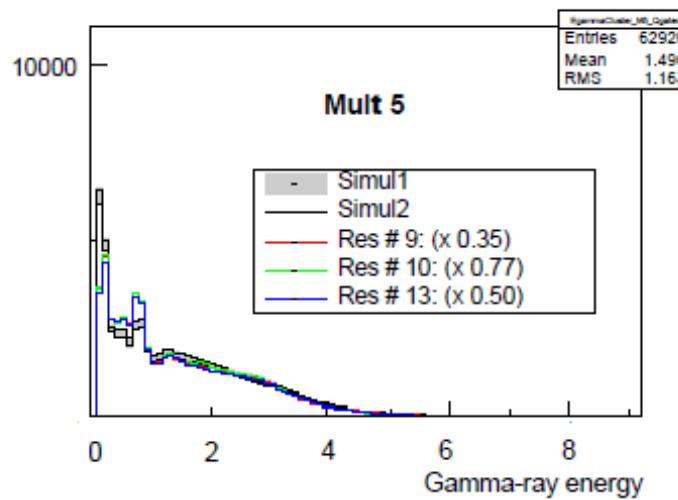
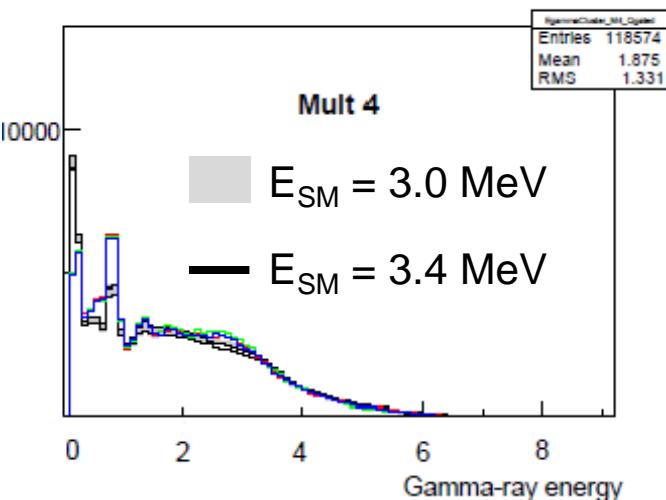
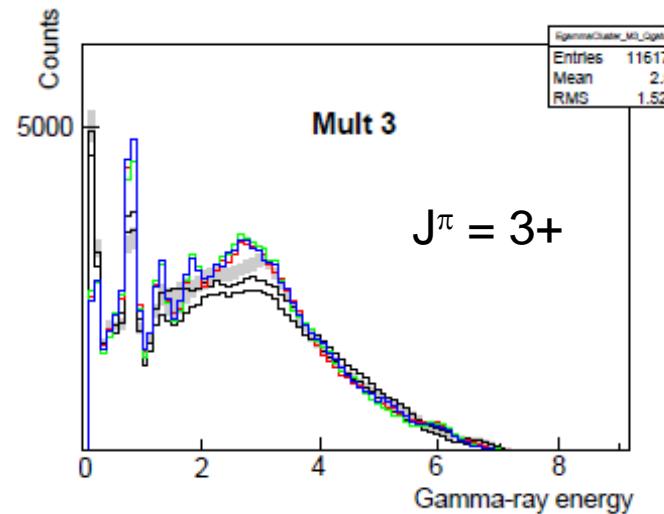
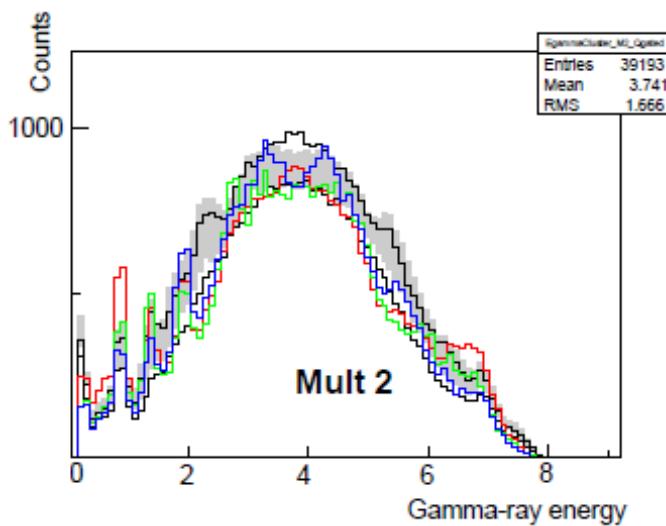
# Comparison of distributions



# $^{168}\text{Er}$ – very preliminary results

# $^{168}\text{Er}$ results – MSC spectra

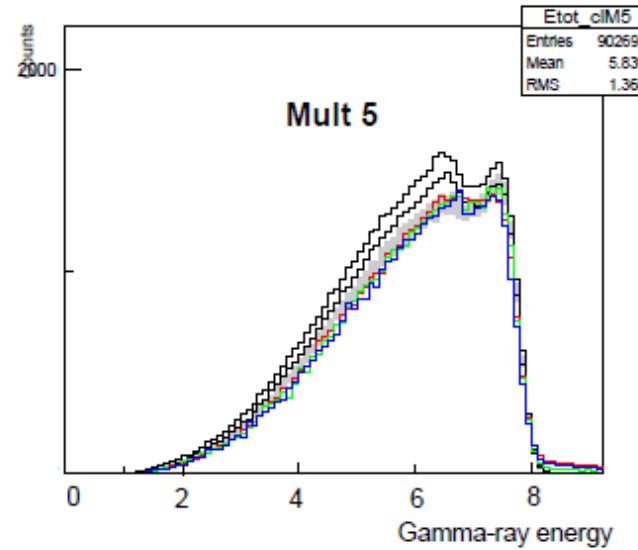
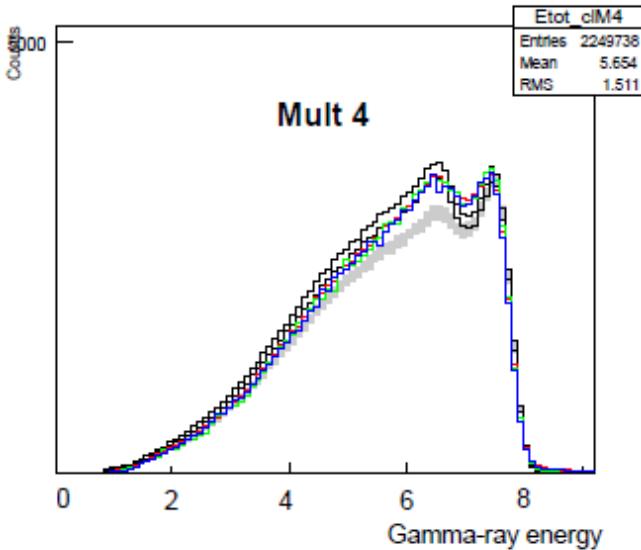
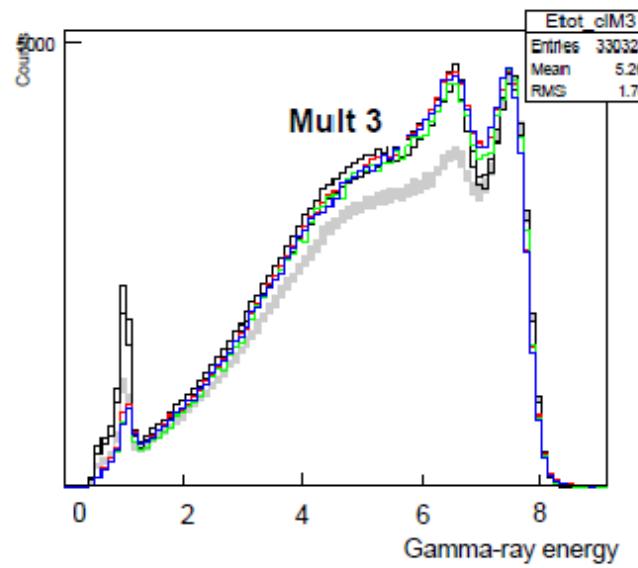
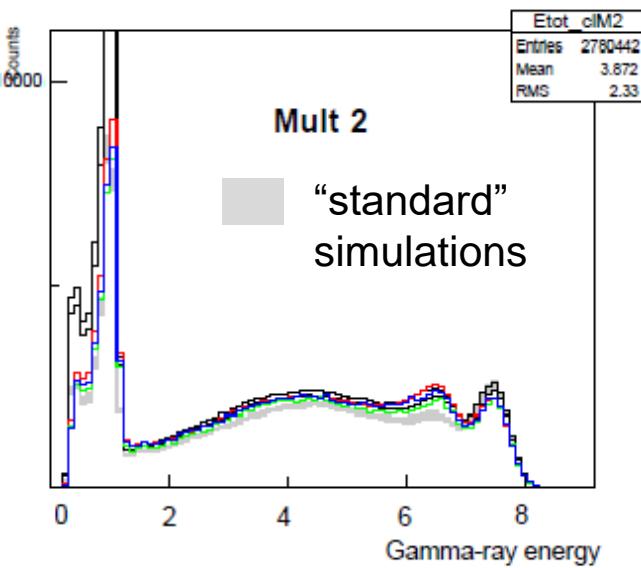
- MSC spectra are well reproduced with similar model combinations as Dy (and Gd) spectra, i.e. with the scissors mode, BSFG LD model,...



... no surprise

# $^{168}\text{Er}$ results – Sum-energy spectra

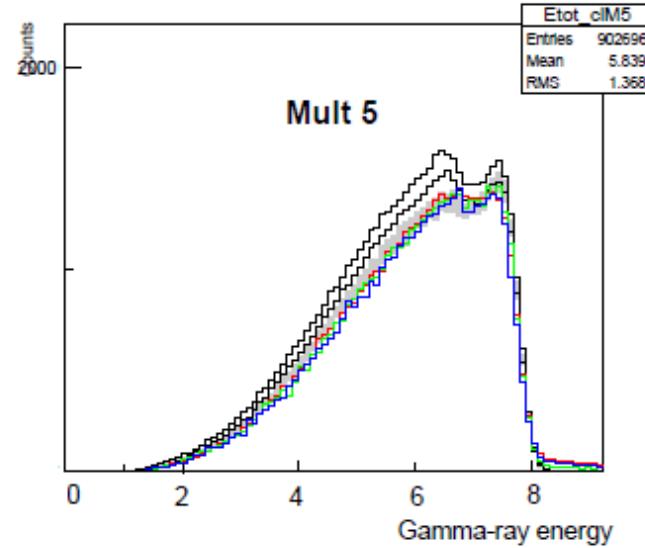
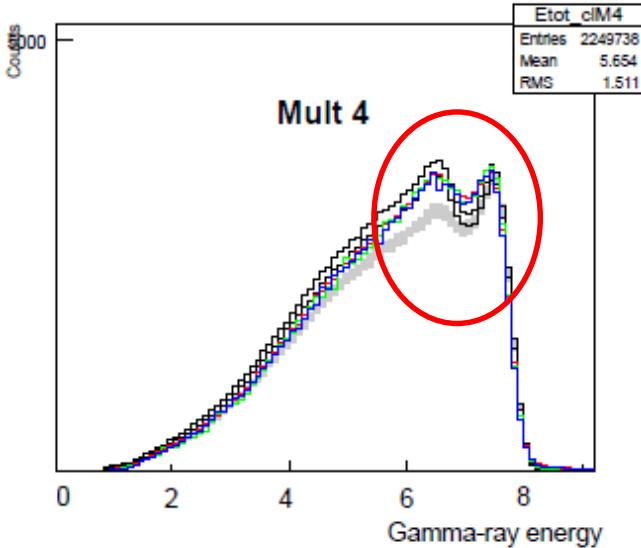
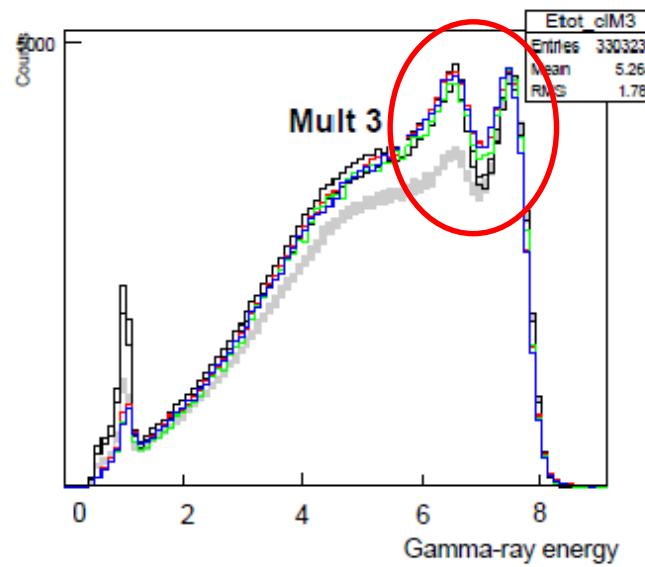
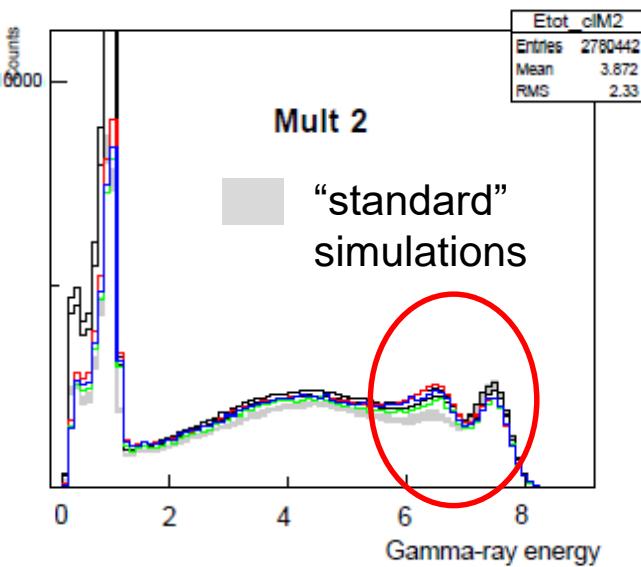
spectra for 20 ns coincidence window



# $^{168}\text{Er}$ results – Sum-energy spectra

spectra for 20 ns coincidence window

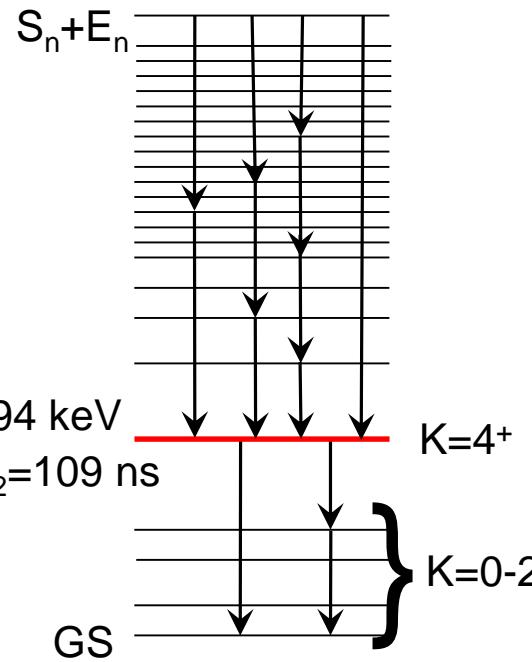
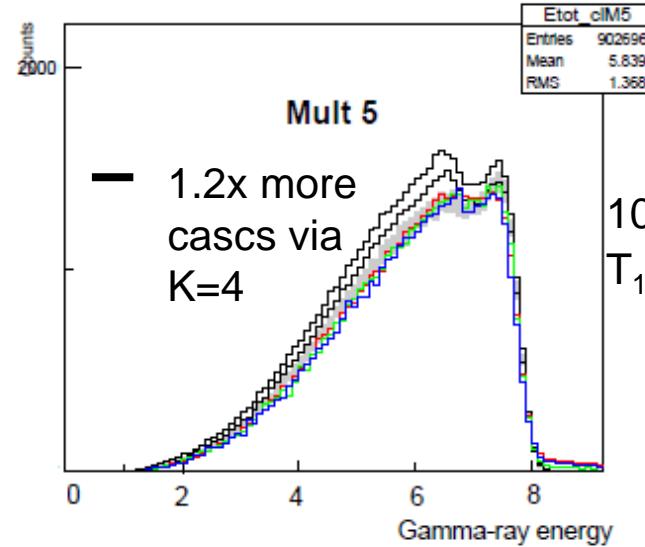
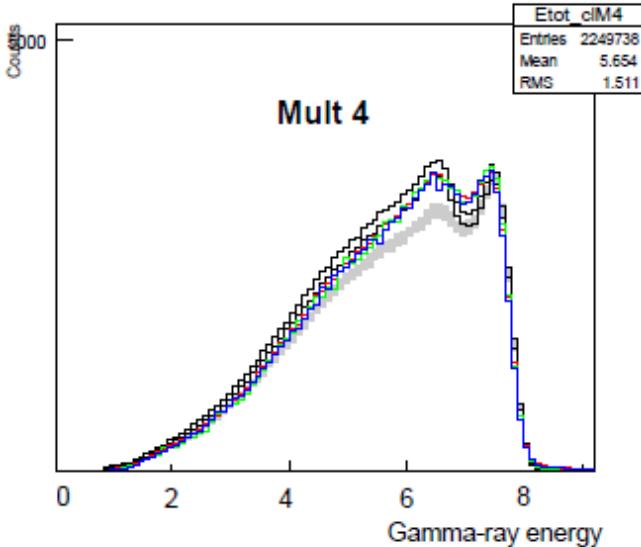
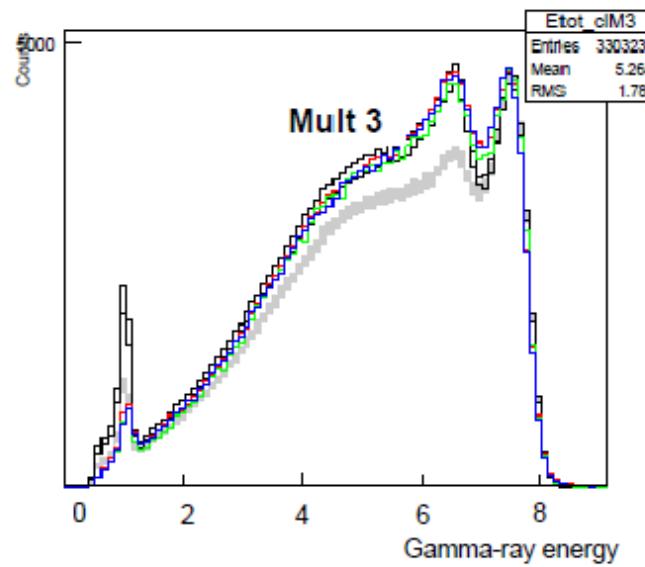
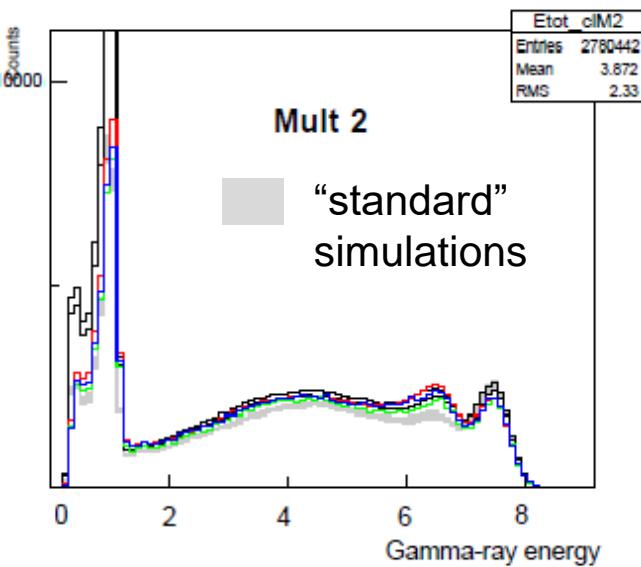
... a surprise



# $^{168}\text{Er}$ results – Sum-energy spectra

spectra for 20 ns coincidence window

... a surprise



# Summary

- Problems with fluctuations in Dy
- Problems with population of the isomeric state in  $^{168}\text{Er}$

problems with populations of isomeric states observed also in other deformed nuclei  $^{177}\text{Lu}$ ,  $^{236}\text{U}$  @ DANCE,  
 $^{180}\text{Hf}$  isotope from measurement in unresolved resonance region at Karlsruhe - K. Wissak et al., PRC73, 045807 (2006)

Possible explanation?

We can only speculate

- influence of level density (spin cut-off)
- influence of quantum number K in these nuclei
- ...

**Thank you very much  
for your attention!**