

# Level densities and $\gamma$ strengths of $^{180,181,182}\text{Ta}$ and $(n,\gamma)$ cross sections

Kgashane Leroy Malatji

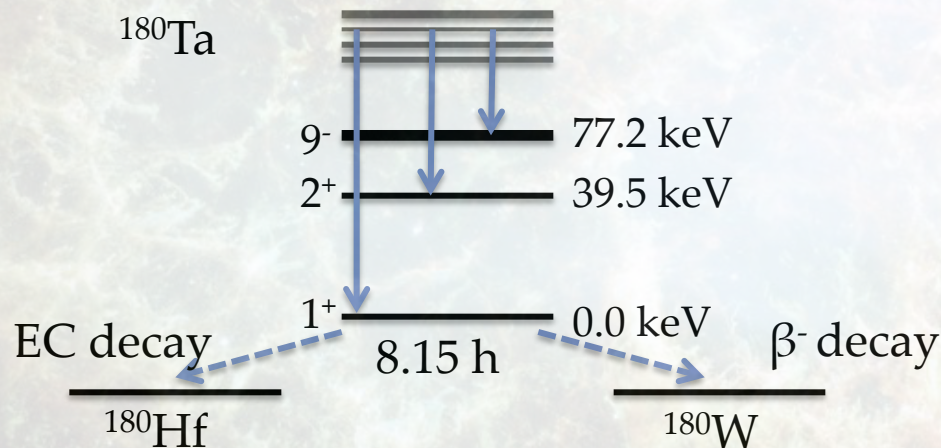
6th Workshop on Nuclear Level Density and Gamma Strength,  
Oslo May 8-12, 2017

# Introduction

## Physics Motivation for $^{180}\text{Ta}$



- Almost all  $A > 110$   $p$ -nuclei are thought to be produced by the photodisintegration of  $s$ - and  $r$ - process pre-existing nuclei
- However, the observed low abundance (0.012%)  $^{180}\text{Ta}$  remains an exception
- The odd-odd  $^{180}\text{Ta}$  exist in a  $9^-$  isomeric state at 77 keV ( $t_{1/2,iso} > 10^{15}$  yrs) in nature

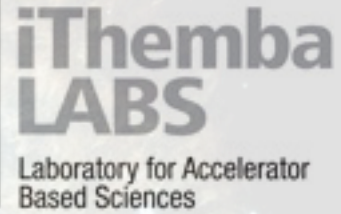


- Several processes are considered

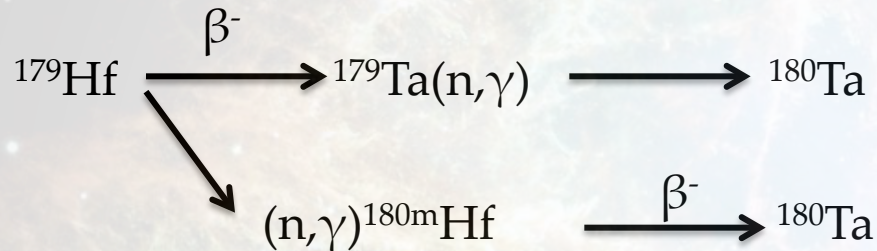


# Introduction

## Physics Motivation for $^{180}\text{Ta}$



- $^{180}\text{Ta}$  could be explained with  $p$ -process [1]
- The  $s$ -process mostly via branching in  $^{179}\text{Hf}$  [2]



- $^{180}\text{Hf}(\nu_e, e)^{180}\text{Ta}$ ,  $^{181}\text{Ta}(\nu, \nu'n)^{180}\text{Ta}$  and  $p$ -process contribute 50, 25 and 25%, respectively [3]
- $^{180}\text{Hf}(\nu_e, e)^{180}\text{Ta}$  50% contribution recently supported by A. Byelikov et al. [4]

[1] M. Arnould and S. Goriely, Phys. Rep. 384, 1 (2003).

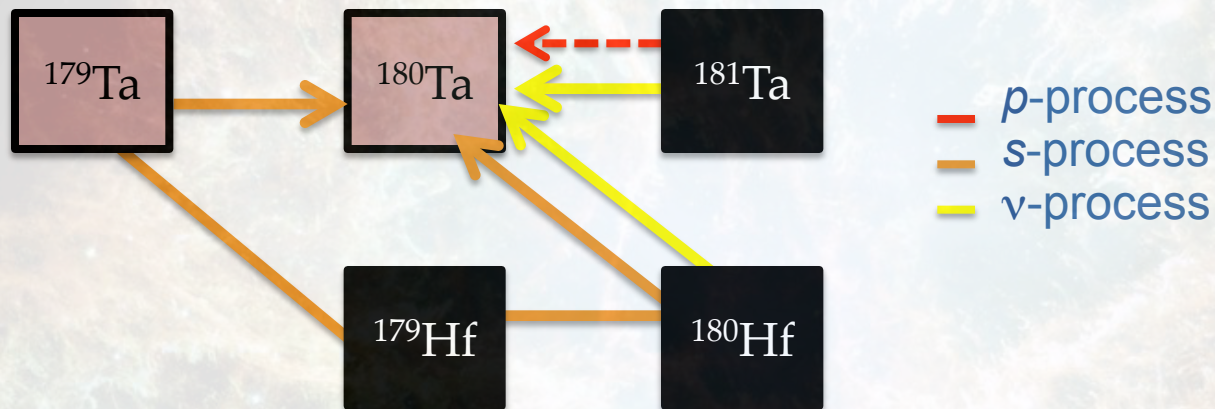
[2] M. Loewe et al. Nucl.Phys. A719 (2003) 275c

[3] A. Heger et al. Phys.Lett. B 606, 258 (2005)

[4] A. Byelikov et al. PRL 98, 082501 (2007)

# Introduction

## Physics Motivation for $^{180}\text{Ta}$

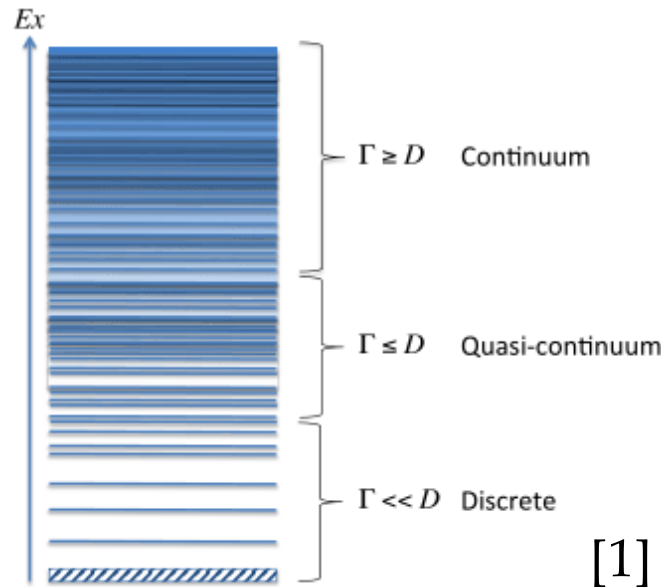


- This is unresolved, hence provoking debates
- Uncertainties in reaction rates rest in nuclear properties
- Therefore production of  $^{180}\text{Ta}$  needs to be reinvestigated with improved nuclear data



# Objectives

- Nuclear Level density (NLD) and  $\gamma$ -ray strength function ( $\gamma$ SF) below  $S_n$  in  $^{180,181,182}\text{Ta}$  isotopes (Oslo Method)



[1]

- Astrophysical Maxwellian averaged (n, $\gamma$ ) cross sections (TALYS [2])
- Investigate production mechanism of  $^{180}\text{Ta}$
- ... additional nuclear structure aspects (C.P. Brits)

[1] Magne Guttormsen et al., Eur. Phys. J. A **51** (12), 170 (2015)

[2] A. J. Koning et al., Nuclear Data for Science and Technology (EDP Sciences; eds O. Bersillon et al.), p. 211 (2008) (see also <http://www.talys.eu>) version 1.6



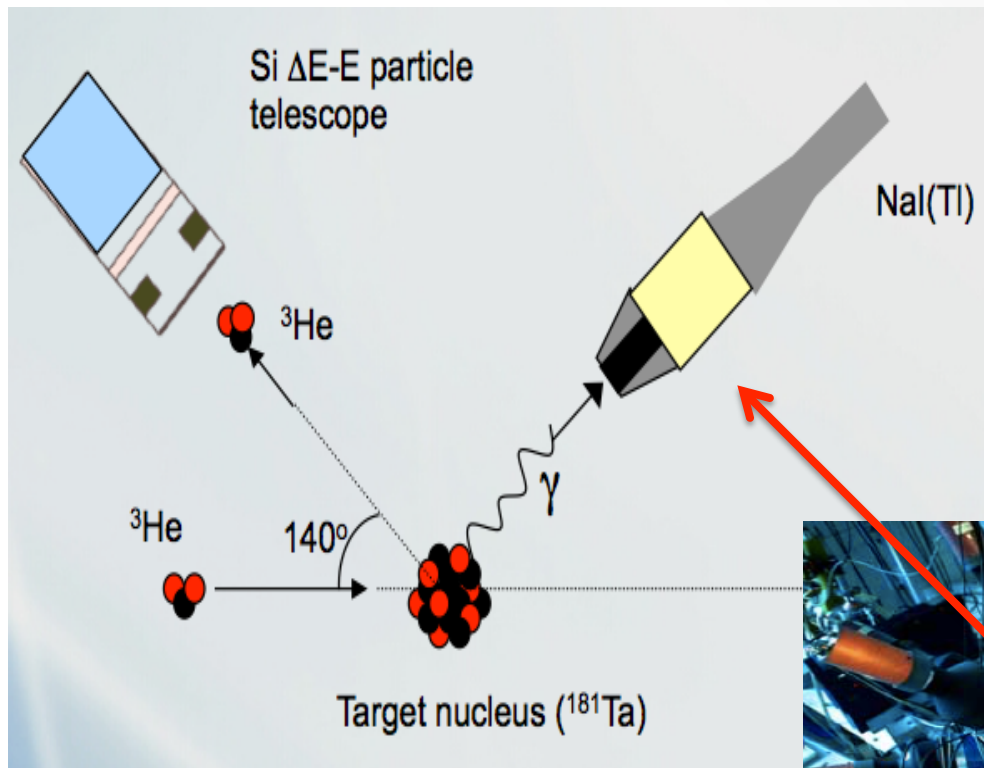
# Experimental Details

## Oslo Cyclotron Laboratory

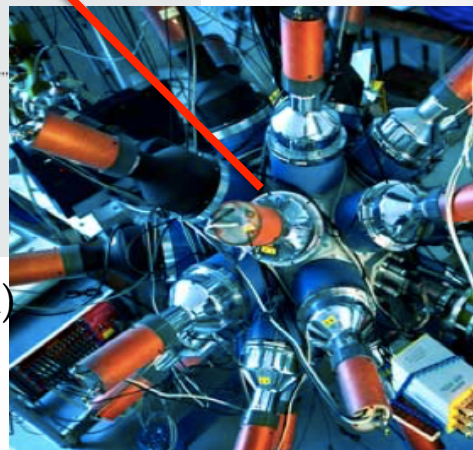


- 0.8 mg/cm<sup>2</sup> thick <sup>181</sup>Ta natural target

- <sup>181</sup>Ta(<sup>3</sup>He,X)<sup>180,181</sup>Ta, 34 MeV
- <sup>181</sup>Ta(d,X)<sup>180,181</sup>Ta, 15 MeV
- <sup>181</sup>Ta(d,X)<sup>181,182</sup>Ta, 12.5 MeV



- CACTUS Array: 26 collimated 5"×5" NaI(Tl) (~22 cm)
- 14.1% eff. at E<sub>γ</sub>= 1332 keV





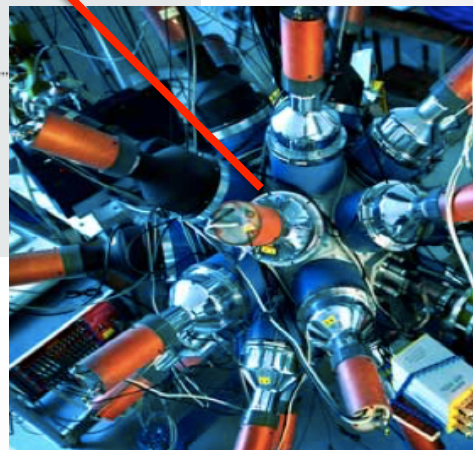
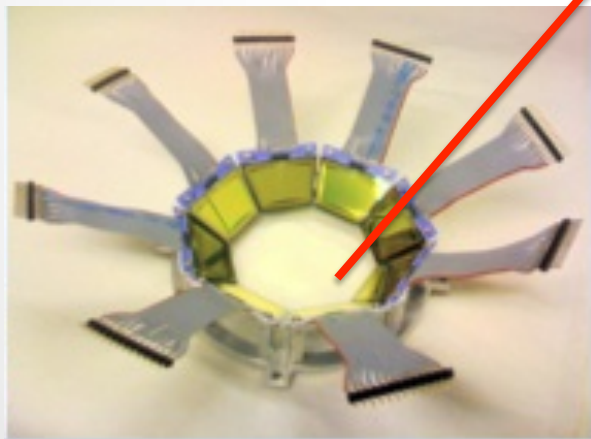
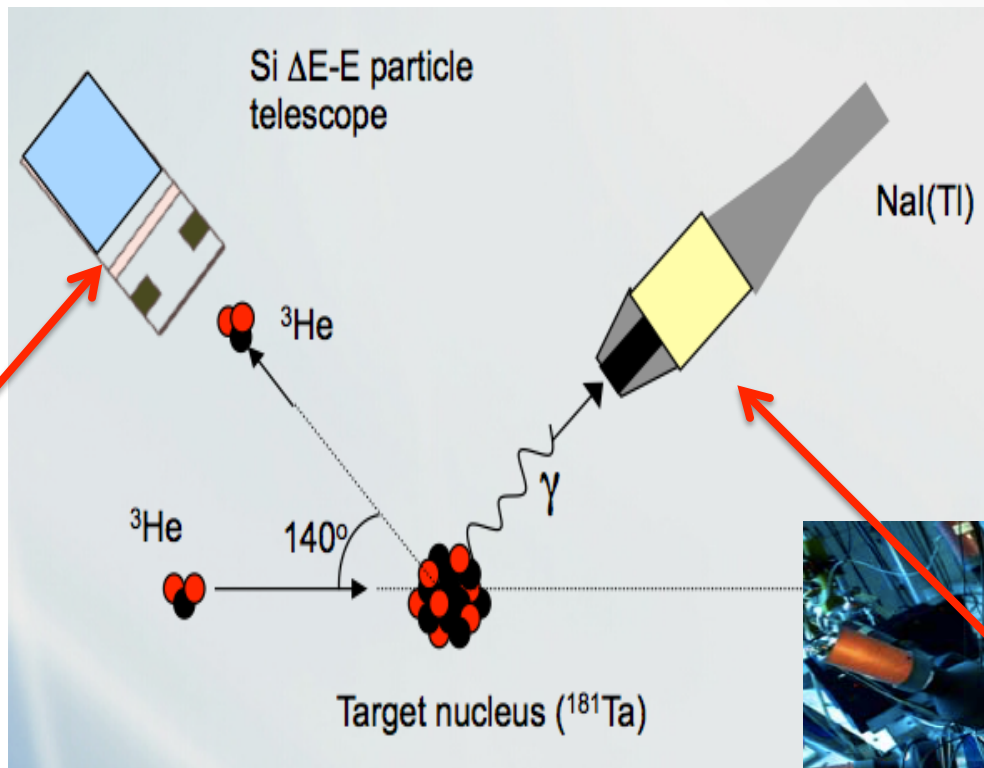
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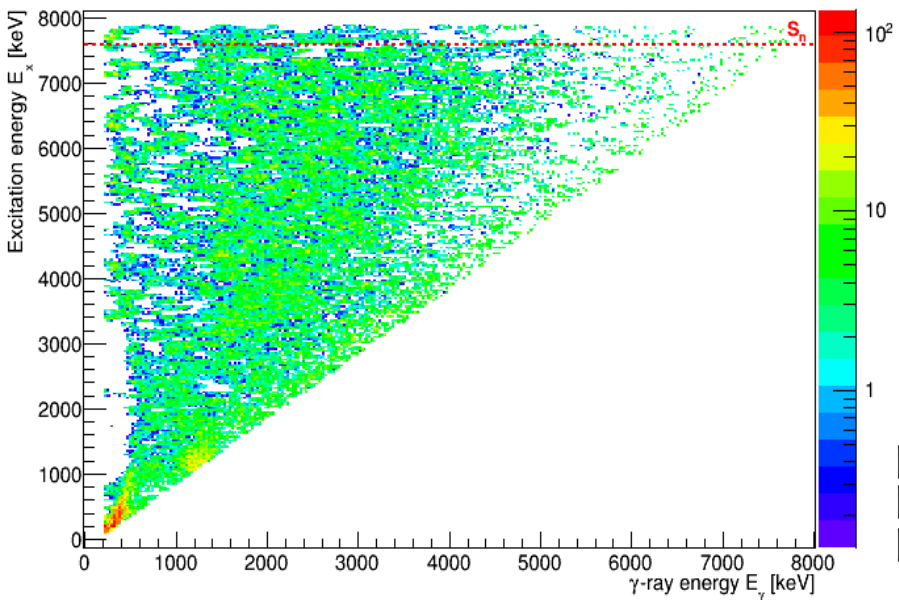
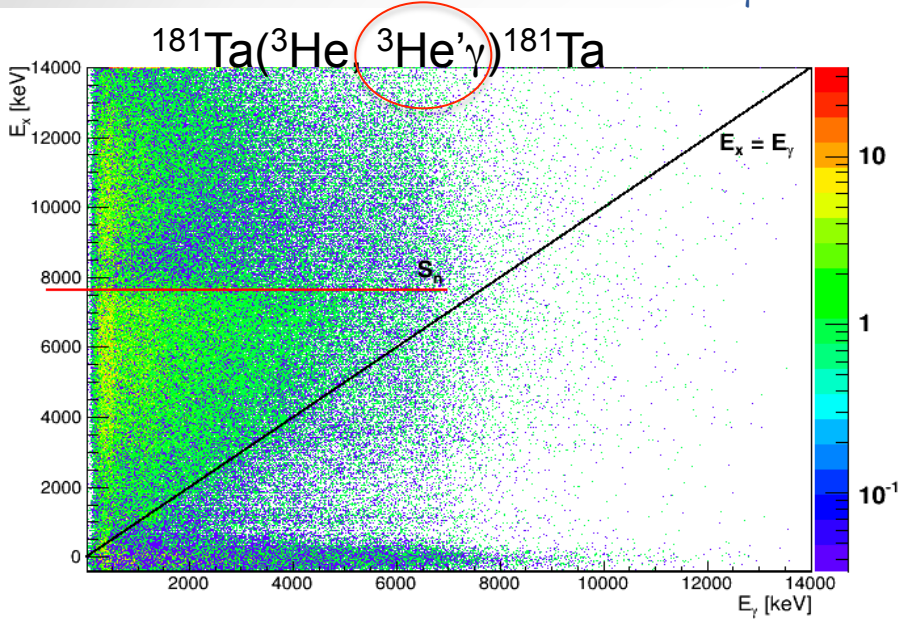
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- SiRi Array, 64  $\Delta E$ -E Si particle telescopes
- $\Delta E$ , E and Al foil thicknesses (130  $\mu\text{m}$ , 1550  $\mu\text{m}$  and 10.5  $\mu\text{m}$ )
- $\theta = 126^\circ$  to  $140^\circ$ ,  $\sim 5$  cm

# Data Analysis

## Particle- $\gamma$ Coincidence Matrices



### The Oslo Method

1. Unfolding  $\gamma$ -ray continuum spectra[1]  
> Unfolding iterative procedure
2. Extraction of primary  $\gamma$ -rays [2]  
> first-generation method
3. Simultaneous extraction of level density and strength function[3]

$$\lambda_{if} = \frac{2\pi}{\hbar} |M_{if}|^2 \cdot \rho(E_f) \quad \text{Fermi's golden rule}$$

$$P(E_i, E_\gamma) \propto \rho(E_f) \cdot \mathcal{T}(E_\gamma) \quad \text{Assumes Brink hypothesis}$$

4. Normalization

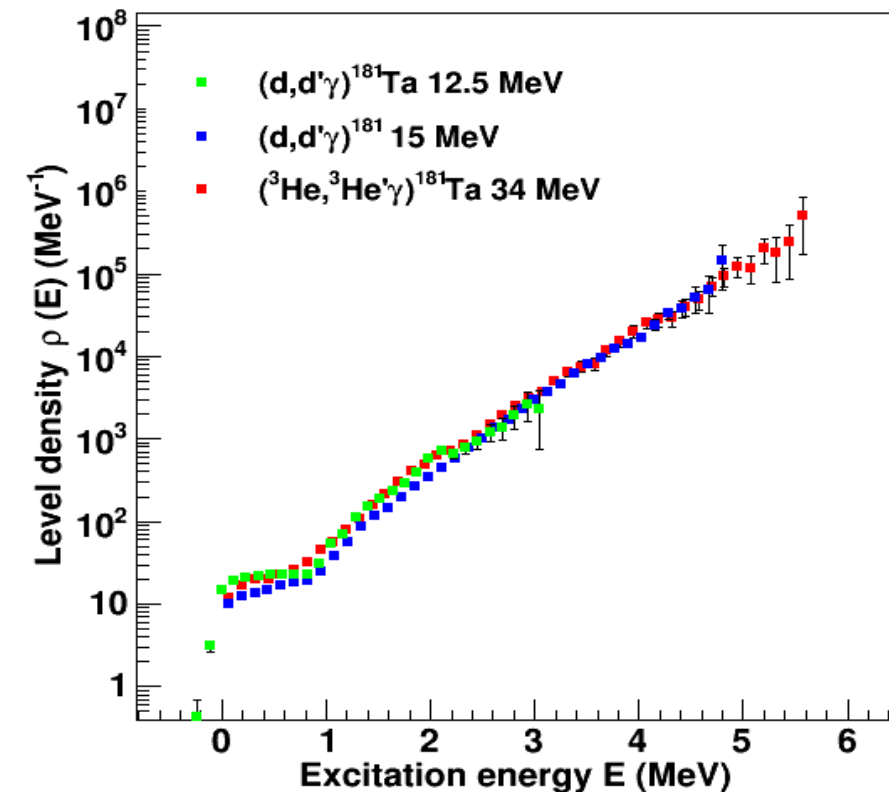
- [1] M. Guttormsen et al., NIM Phys. Res. A 374, 371 (1996)  
 [2] M. Guttormsen et al., NIM Phys. Res. A 255, 518 (1987)  
 [3] A. Schiller et al., NIM Phys. Res. A 447, 498 (2000)



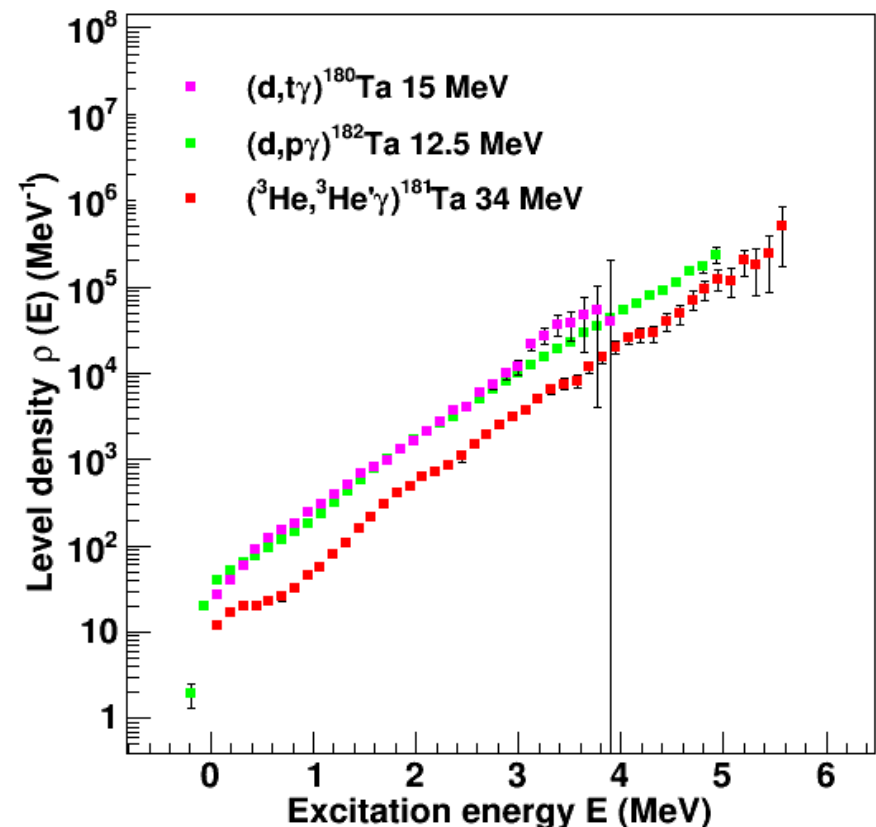
# 180,181,182Ta Results

## Nuclear Level Density

Different reactions yield similar results



NLDs of neighbouring isotopes

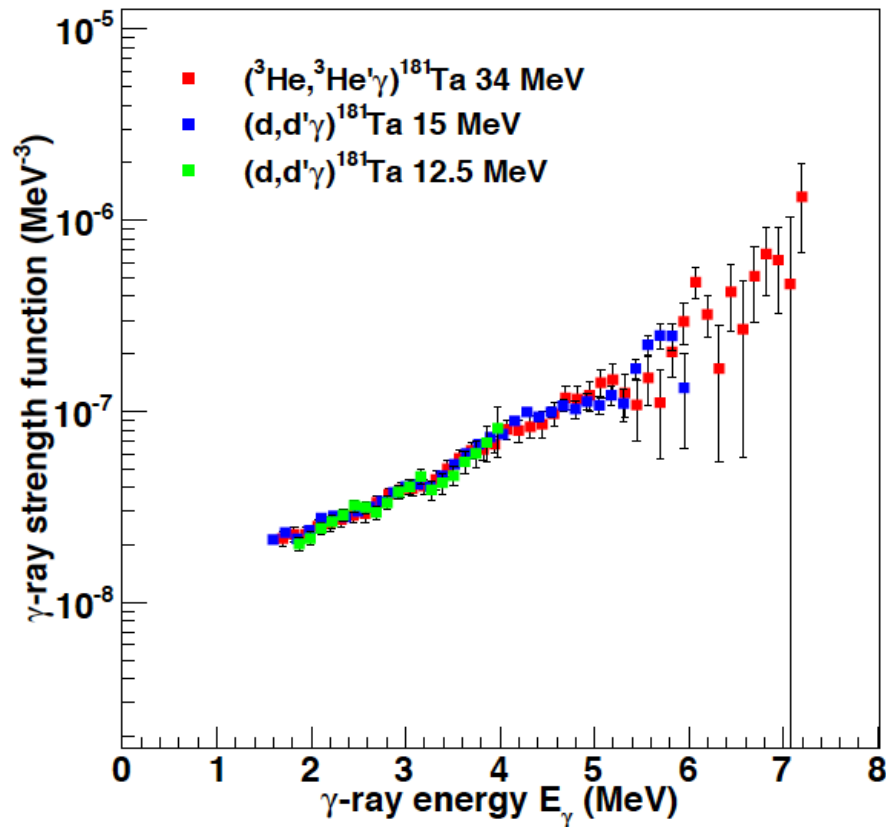


# 180,181,182Ta Results

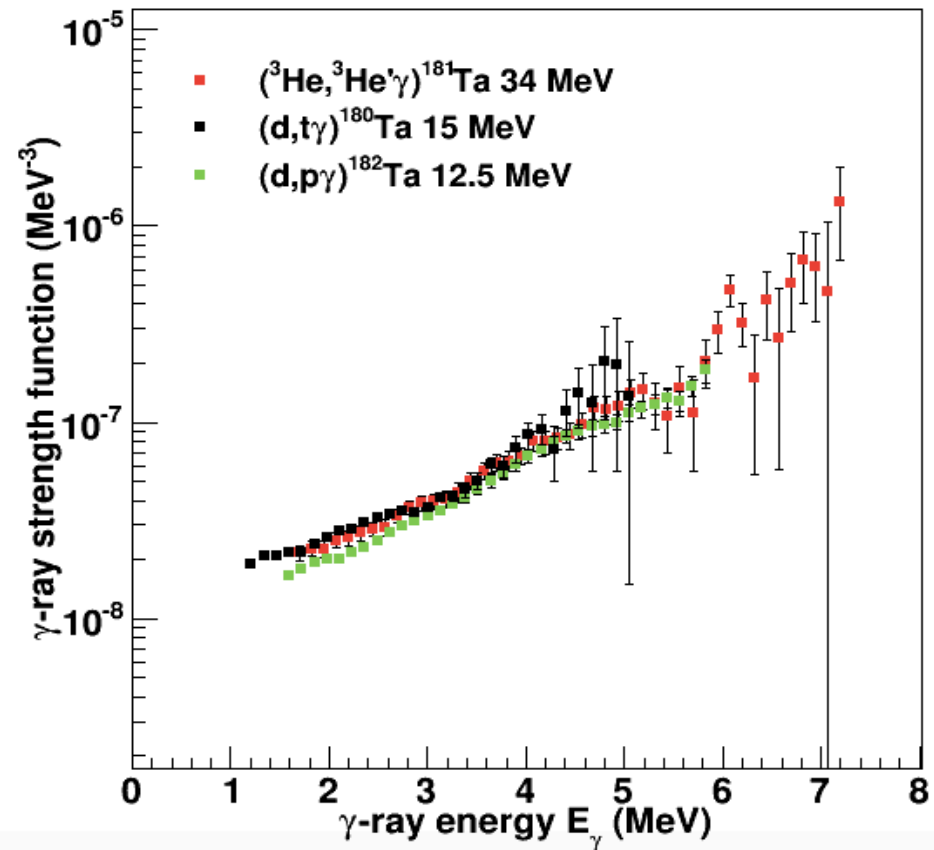
## $\gamma$ -ray Strength Function

$$f(E_\gamma) = \frac{1}{2\pi E_\gamma^3} BT(E_\gamma) \quad [1]$$

Different reactions yield similar results

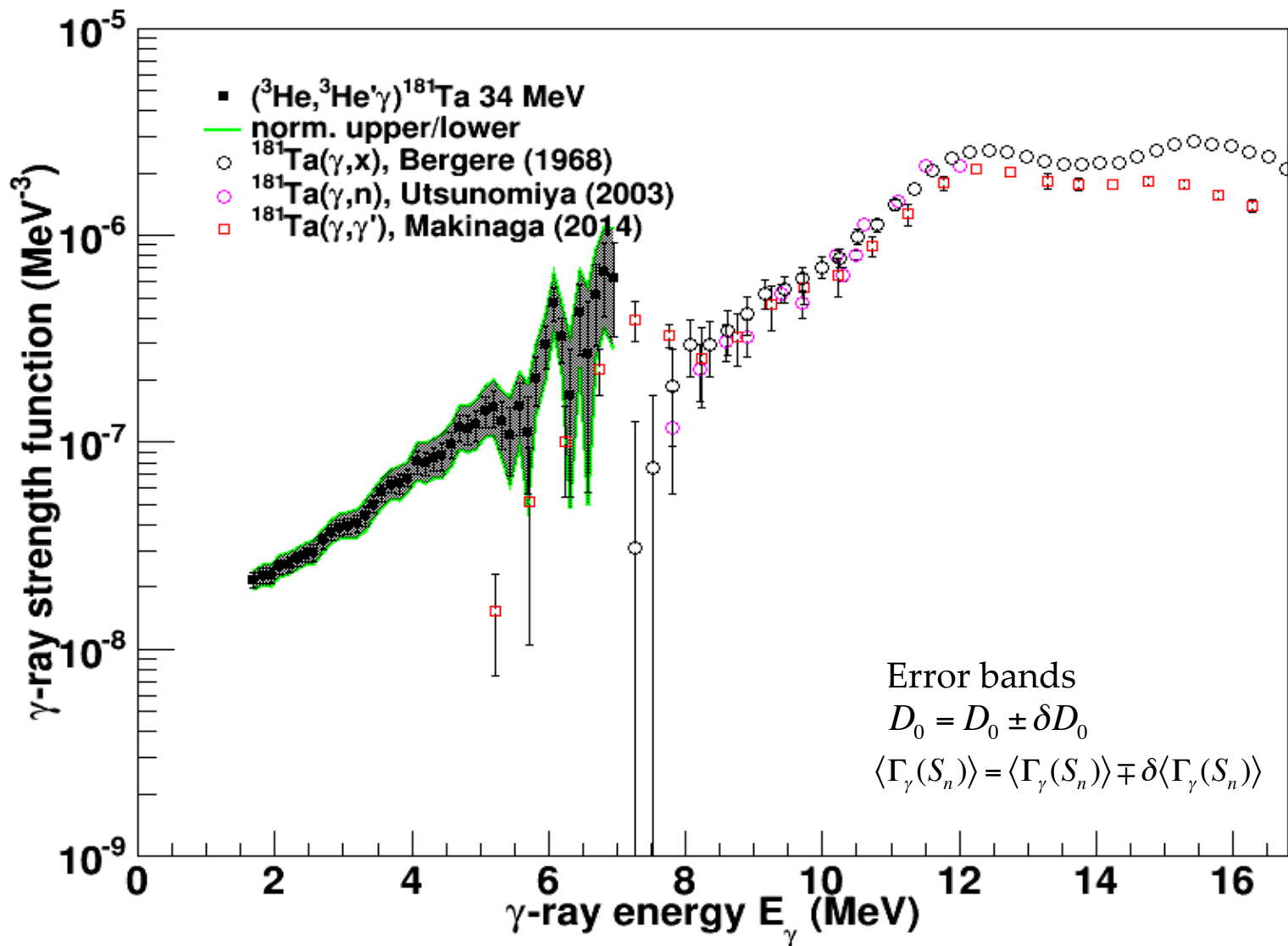


$\gamma$ SFs of neighbouring isotopes



# $^{181}\text{Ta}$ Results

Comparison of  $^{181}\text{Ta}(^3\text{He}, ^3\text{He}'\gamma)$   $\gamma\text{SF}$  with photoabsorption data



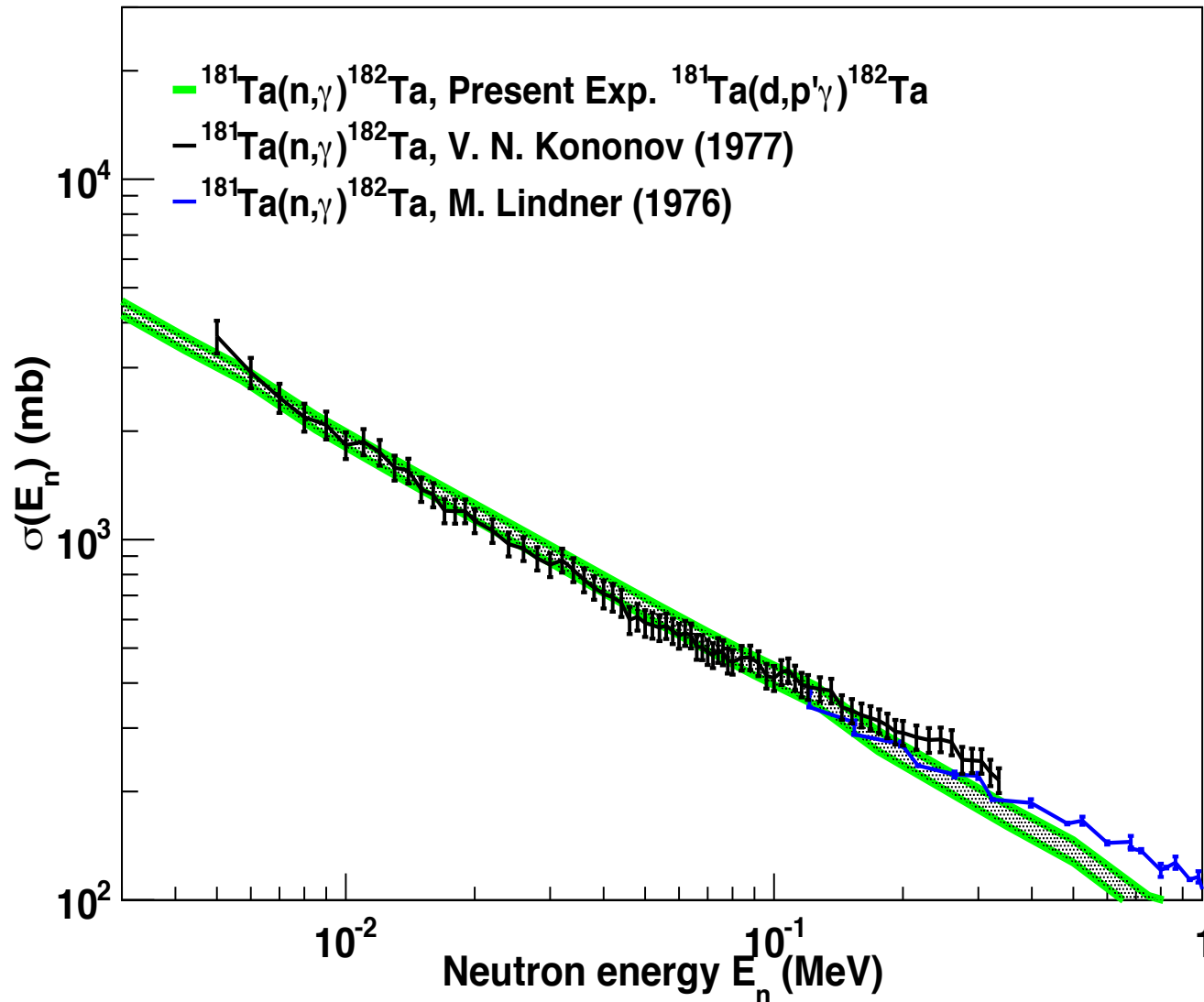


# $^{182}\text{Ta}$ Results

## Neutron Capture Cross Section Calculations



iThemba  
LABS  
Laboratory for Accelerator  
Based Sciences

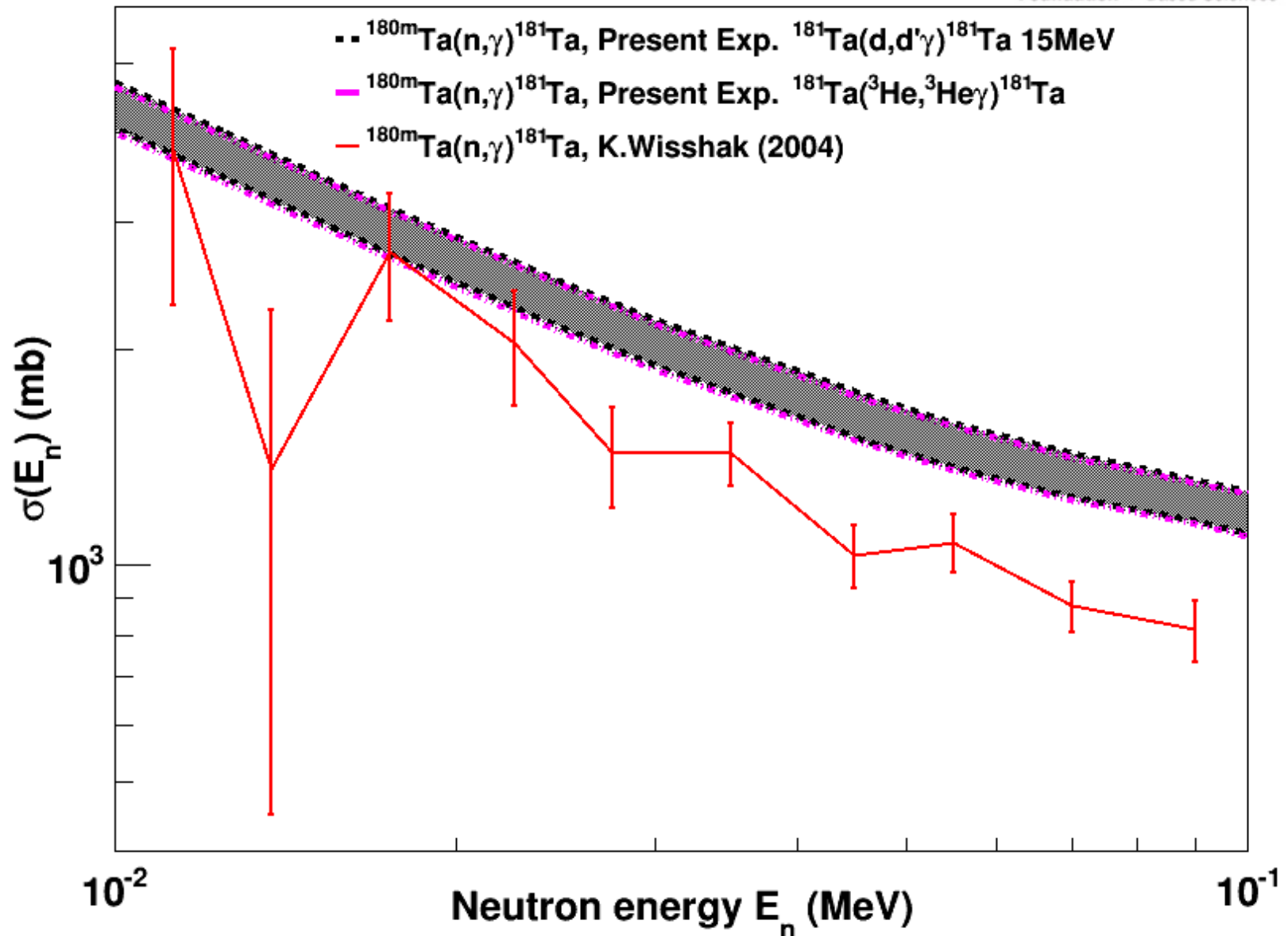


TALYS

Key ingredients  
(HF approach)  
-  $\gamma$ SF, NLD and OMP

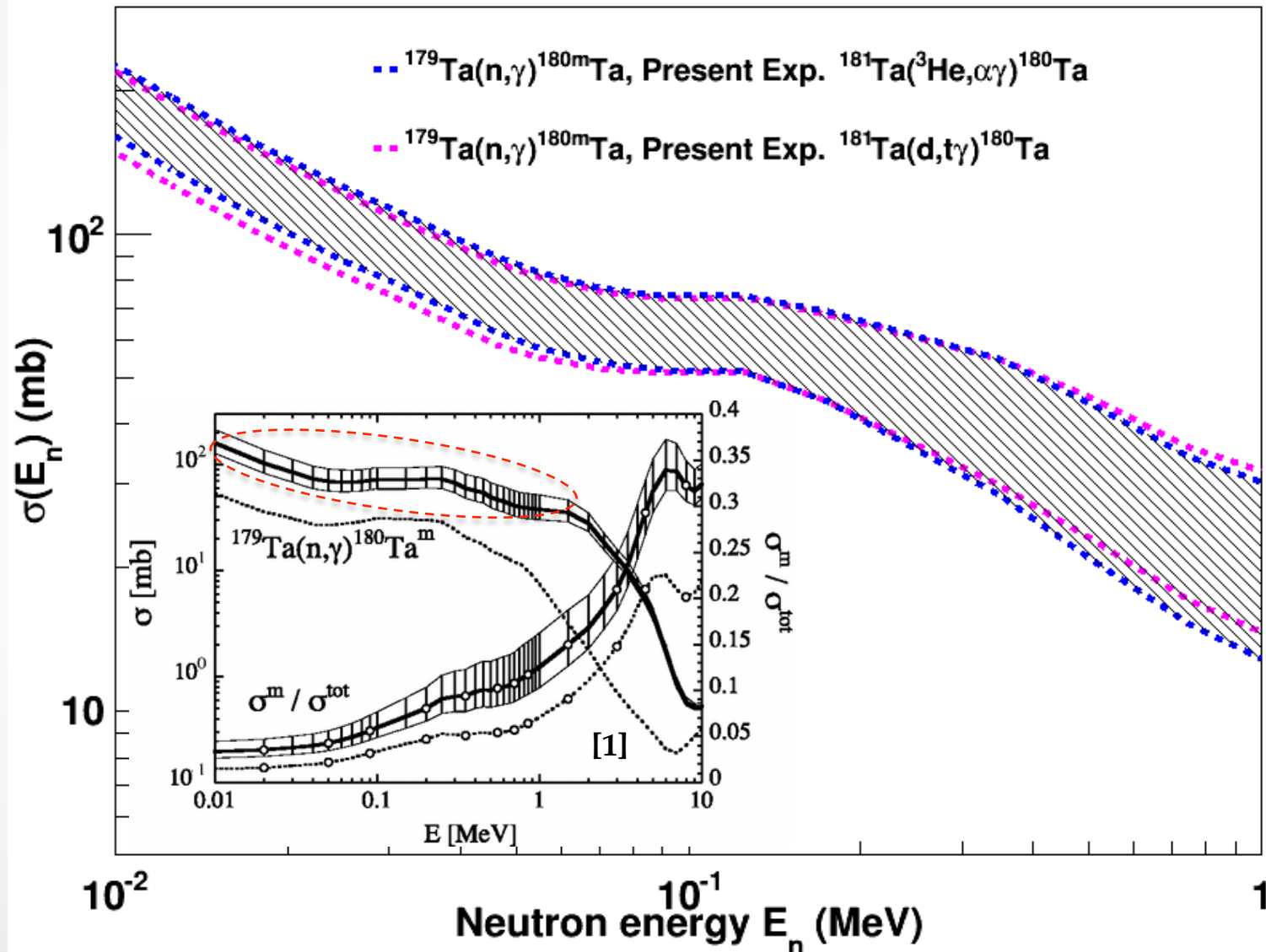
# $^{181}\text{Ta}$ Results

## Neutron Capture Cross Section Calculations



# $^{180}\text{Ta}$ Results

## Neutron capture Cross Section Calculations



[1] S. Goko *et al.*, Phys. Rev. Lett. **96**, 192501 (2006).



# 180,181,182Ta Results

## Maxwellian Averaged (n, $\gamma$ ) Cross Sections



Reaction	$\langle E \rangle$ (keV)	MACS (mb)	KADoNiS. MACS (mb) [1]
$^{179}\text{Ta}(n,\gamma)$	30	$2613 \pm 681$	$1334 \pm 422$
	215	$825 \pm 292$	
$^{180\text{m}}\text{Ta}(n,\gamma)$	30	$2224 \pm 169$	$1465 \pm 100$
	215	$803 \pm 78$	
$^{180\text{gs}}\text{Ta}(n,\gamma)$	30	$2191 \pm 178$	$1640 \pm 260$
	215	$619 \pm 70$	
$^{181}\text{Ta}(n,\gamma)$	30	$936 \pm 52$	$766 \pm 15$
	215	$243 \pm 17$	

- [1] I. Dillmann et al. , AIP Conf. Proc. 819 , 123; online at [http:// www.kadonis.org](http://www.kadonis.org)

# Summary and Outlook



- Experiments successfully performed at the Oslo cyclotron laboratory
- The  $\gamma$ SF and NLD of  $^{180,181,182}\text{Ta}$  extracted with the Oslo Method
- First time, measurements of NLD and  $\gamma$ SF below Sn in  $^{180}\text{Ta}$  and below 5 MeV in  $^{181}\text{Ta}$  experimentally
- The experimental  $\gamma$ SF and NLD used to investigate  $(n,\gamma)$  cross sections
- The newly deduced  $^{179,180,181}\text{Ta}$  MACS will be used in a continued collaboration with S. Goriely
- Evaluate galactic production mechanism of  $^{180}\text{Ta}$  and possibly constrain the astrophysical environments.
- TALYS calculation using theoretical models...

# Acknowledgements

K. L. Malatji<sup>1,2</sup>, B. V. Kheswa<sup>2,3</sup>, M. Wiedeking<sup>2</sup>, F. L. Bello Garrote<sup>3</sup>, D. L. Bleuel<sup>4</sup>, C.P. Brits<sup>1,2</sup>, F. Giacoppo<sup>5,6</sup>, S. Goriely<sup>7</sup>, A. Görgen<sup>3</sup>, M. Guttormsen<sup>3</sup>, K. Hadynska-Klek<sup>3</sup>, T. W. Hagen<sup>3</sup>, V. W. Ingeberg<sup>3</sup>, M. Klintefjord<sup>3</sup>, A. C. Larsen<sup>3</sup>, H. T. Nyhus<sup>3</sup>, T. Renstrøm<sup>3</sup>, S. Rose<sup>3</sup>, E. Sahin<sup>3</sup>, S. Siem<sup>3</sup>, G. M. Tveten<sup>3</sup> and F. Zeiser<sup>3</sup>.

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<sup>4</sup> *Lawrence Livermore National Laboratory, 7000 East Avenue, Livermore, CA, USA*

<sup>5</sup> *Helmholtz Institute Mainz, 55099 Mainz, Germany*

<sup>6</sup> *GSI Helmholtzzentrum für Schwerionenforschung, 64291 Darmstadt, Germany*

<sup>7</sup> *Institut d'Astronomie et d'Astrophysique, Université Libre de Bruxelles, CP 226, B-1050 Brussels, Belgium*

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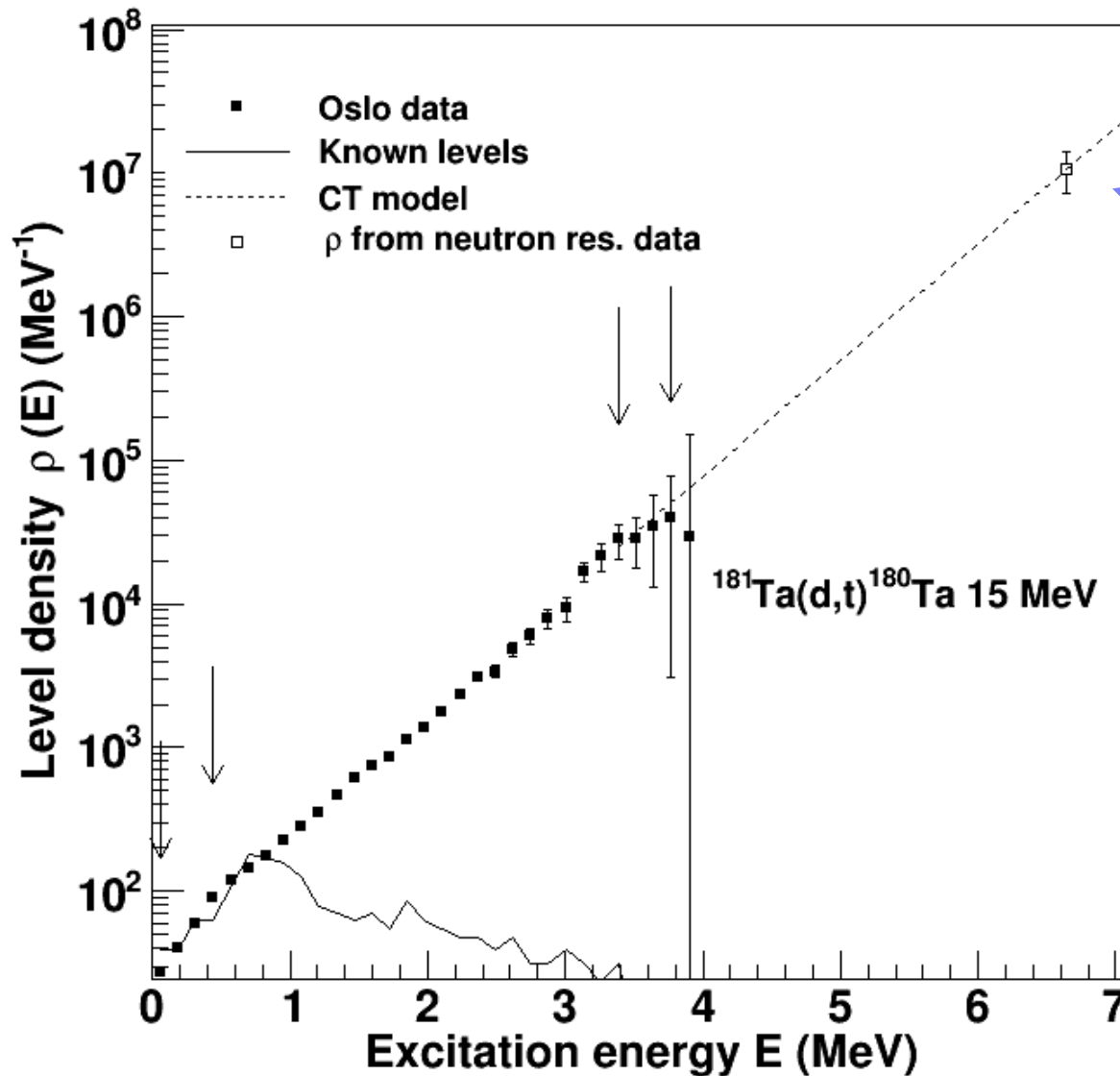
Thank You For Your Attention!!!



# $^{180}\text{Ta}$ Results

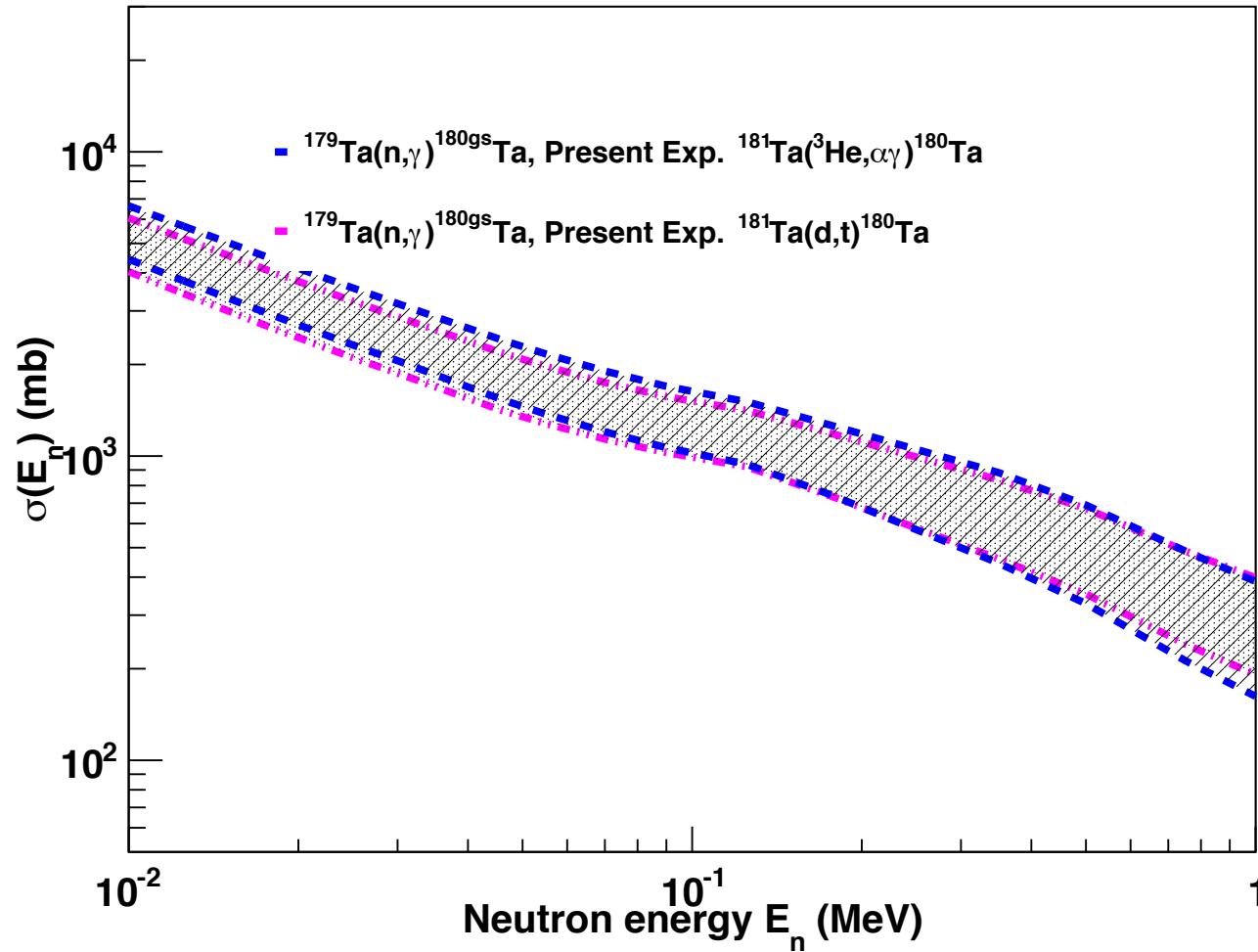
## Normalization of the NLD

$$\rho(S_n) = \frac{2\sigma^2}{D_0(J_T + 1)e^{[-(J_T+1)^2/2\sigma^2]} + e^{(-J_T^2/2\sigma^2)}J_T}$$



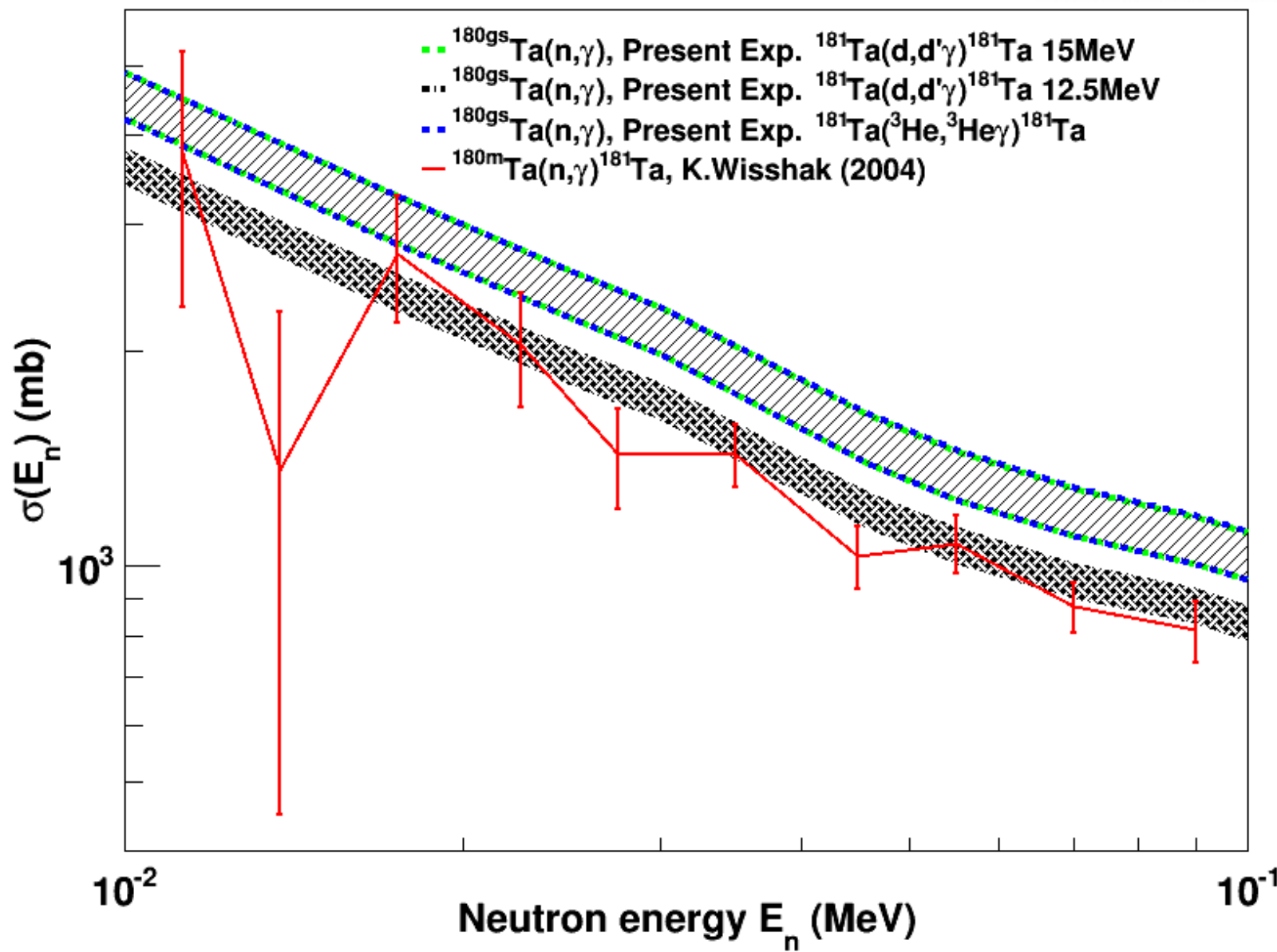
No neutron resonance data available ( $^{180}\text{Ta}$ )

# $^{180\text{gs}}\text{Ta}$ Cross Section

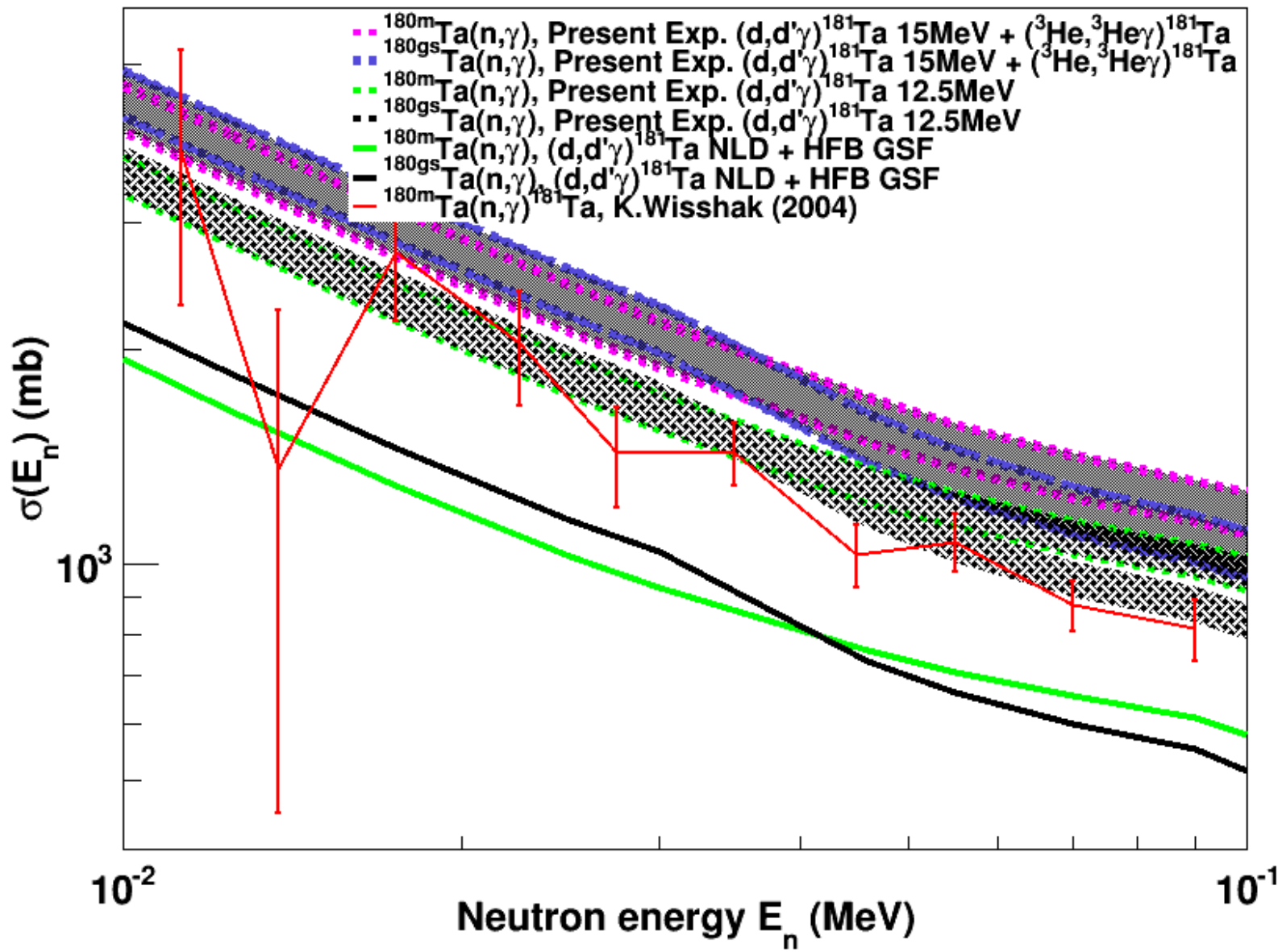




# $^{181}\text{Ta}$ Cross Section

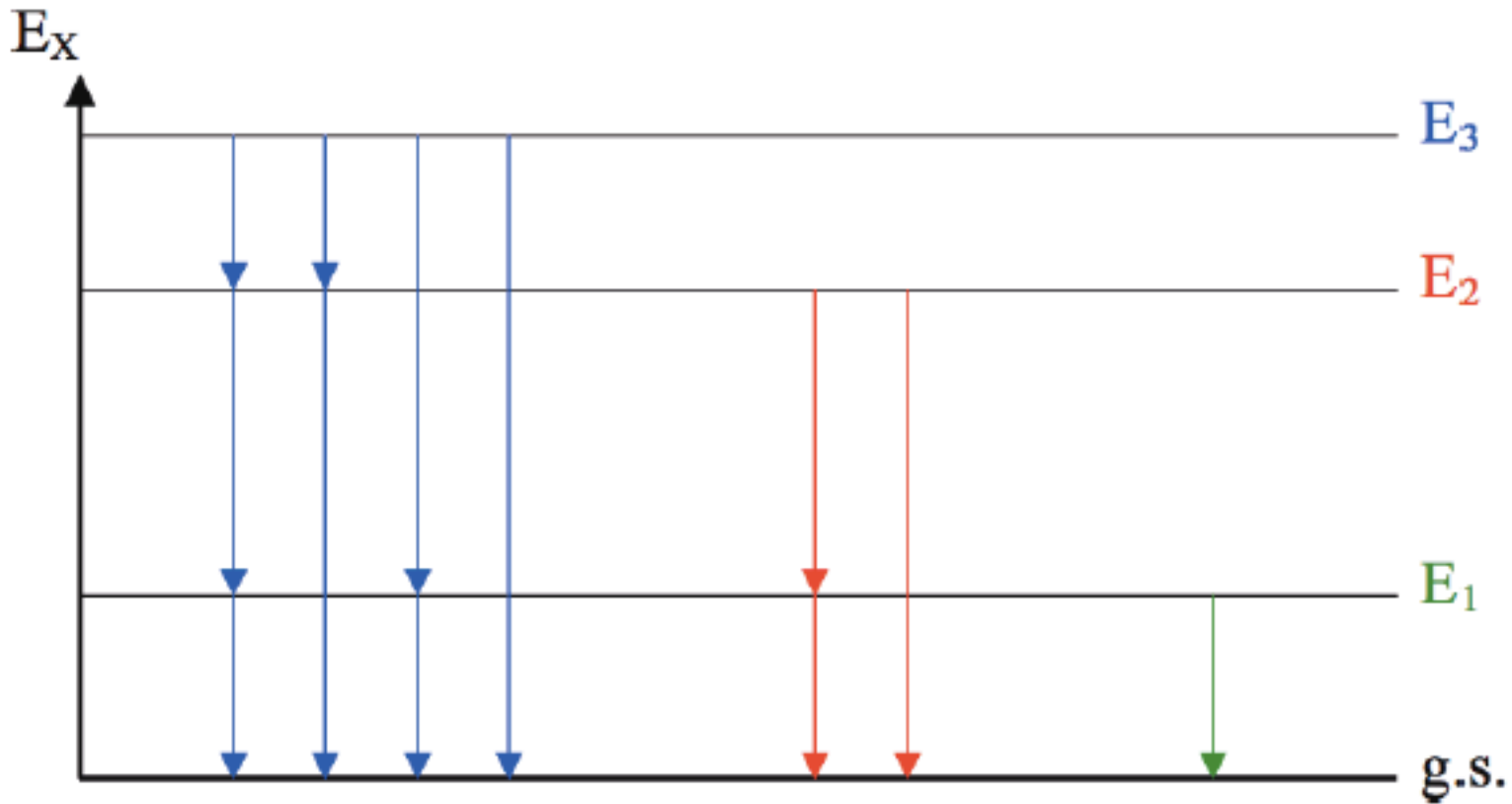


# $^{181}\text{Ta}$ Cross Section



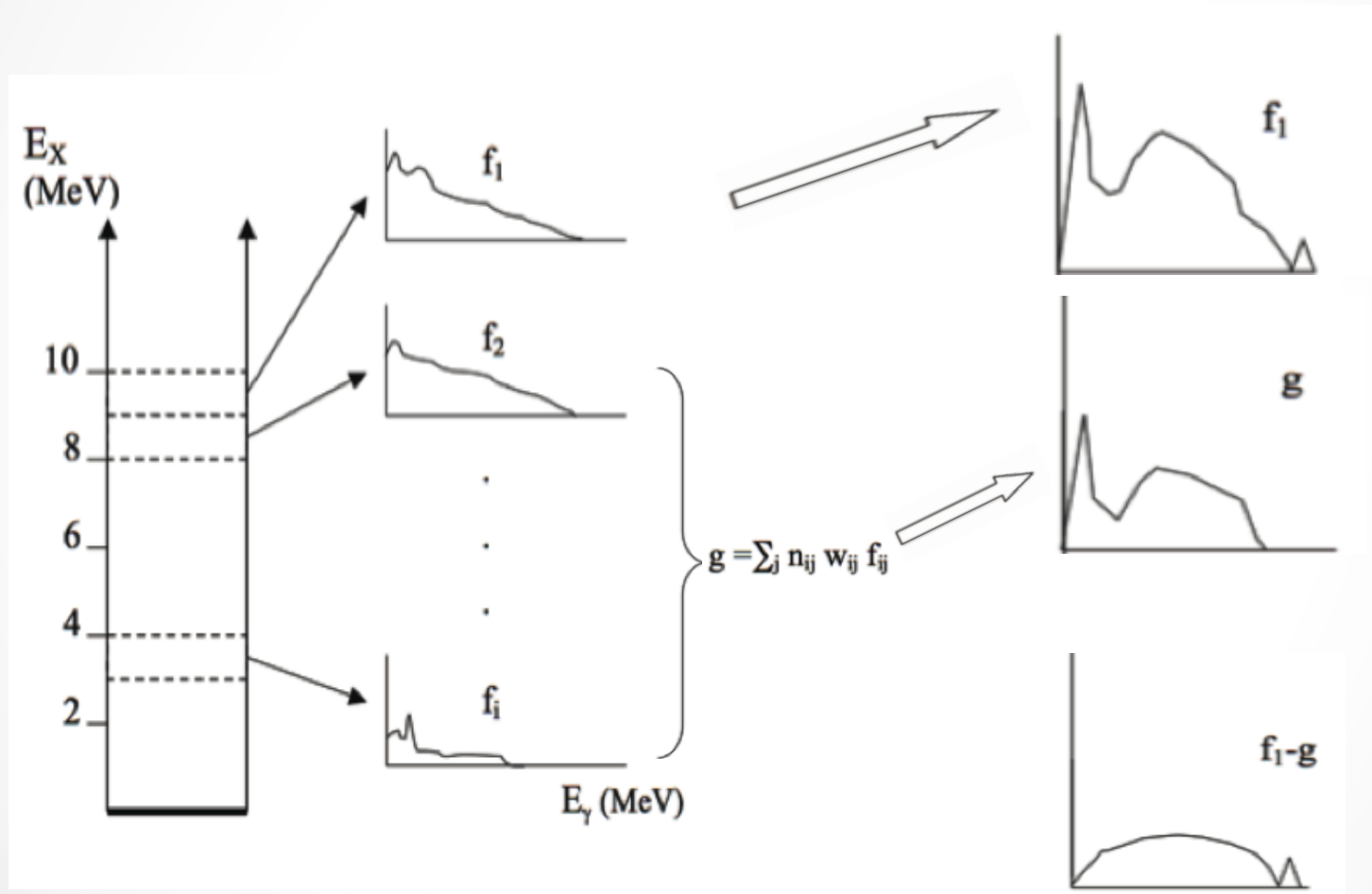
# Oslo Method

## First Generation Method



# Oslo Method

## First Generation Method





# Oslo Method

## Factorization of the First-Generation Matrix

- According Fermi's golden rule:  $\lambda_{if} \propto |\langle f|H'|i\rangle|^2 \rho(E_f)$   
 where  $\rho(E_f)$  is the NLD at a final state  
 is the matrix elements  $|\langle f|H'|i\rangle|$
- Equivalent equation for the FG matrix:  $P(E_i, E) \propto \rho(E_f) \mathcal{T}_{if}$   
 where  $\mathcal{T}_{if}$  is the  $\gamma$  transmission coefficient
- Brink Hypothesis: GEDR can be built on every state, and its properties don't depend on the properties of the initial and final state.
- $\mathcal{T}_{if}$  only depend on the  $\gamma$ -ray energy

# Oslo Method

## Simultaneous Extraction of T and NLD

- The  $\mathcal{T}(E_\gamma)$  and  $\rho(E_f)$  are extracted by fitting  $P_{th}(E_x, E_\gamma)$  to  $P(E_x, E_\gamma)$  and minimizing

$$\chi^2 = \frac{1}{N} \sum_{E_x} \sum_{E_\gamma} \frac{(P_{th}(E_x, E_\gamma) - P(E_x, E_\gamma))^2}{\Delta P(E_x, E_\gamma)}$$

Where 
$$P_{th}(E_x, E_\gamma) = \frac{\rho(E_f) \mathcal{T}(E_\gamma)}{\sum_{E_\gamma} \rho(E_f) \mathcal{T}(E_\gamma)}$$

and  $N, \Delta P(E_x, E_\gamma)$  are degrees of freedom and uncertainty in  $P(E_x, E_\gamma)$

# Oslo Method

## Normalization of T and NLD

- Once  $\rho(E_f)$  and  $\mathcal{T}(E_\gamma)$  are extracted
- Infinitely many solutions can be found of the form

$$\tilde{\rho}(E_f) = A\rho(E_f)e^{\alpha E_f} \dots \dots \dots (1)$$

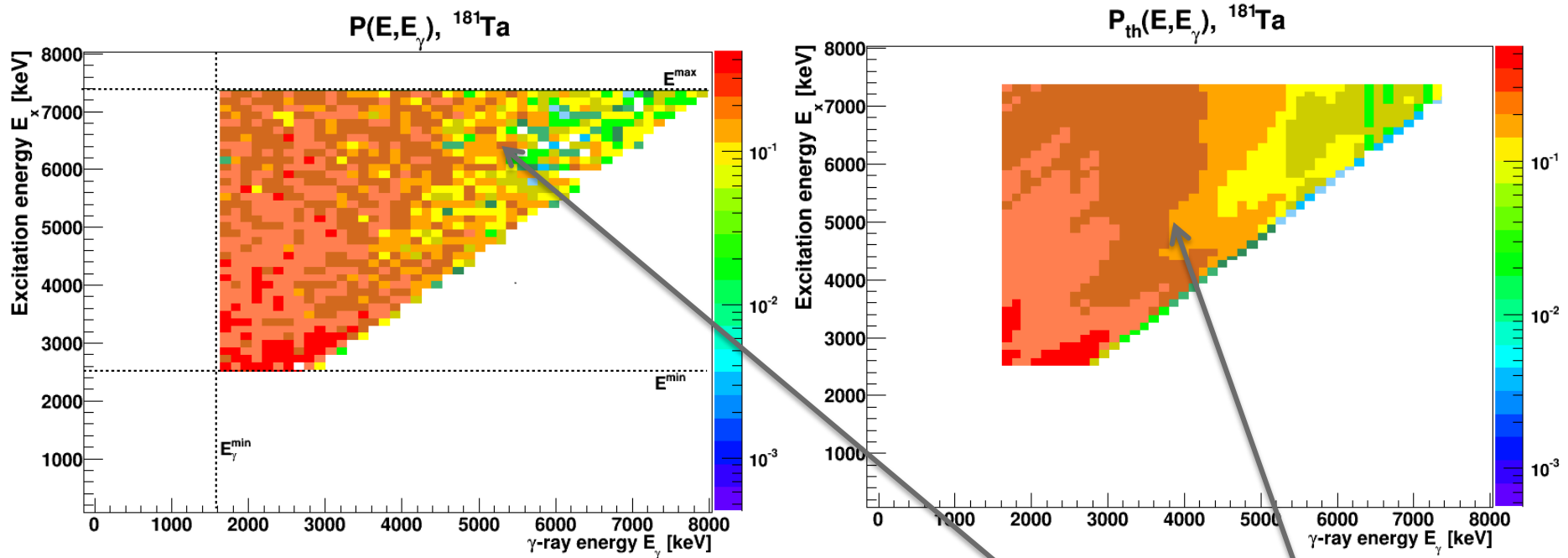
$$\tilde{\mathcal{T}}(E_\gamma) = B\mathcal{T}(E_\gamma)e^{\alpha E_\gamma} \dots \dots \dots (2)$$

Where  $\alpha$  is a common slope between  $\tilde{\rho}(E_f)$  and  $\tilde{\mathcal{T}}(E_\gamma)$   
 $A$  and  $B$  are normalization parameters

- $\alpha$  and  $A$  are obtained by normalizing  $\tilde{\rho}(E_f)$  to  $\rho(S_n)$  and  $\rho$  of known discrete states
- $B$  can be calculated from experimental  $\langle \Gamma_\gamma \rangle$  and  $D_0$  @ neutron threshold

# Data Analysis

## Experimental vs. Fitted FG Matrices



$$P(E, E_\gamma) \propto \rho(E_f) T(E_\gamma).$$

- Assumptions: Brink Hypothesis
- The  $\rho(E_f)$  and  $T(E_\gamma)$  are extracted by fitting to  $P(E_x, E_\gamma)$  and performing  $\chi^2$  minimum.

## The Oslo Method

- Normalization of ( $\gamma$  transmission coefficient)  $T(E_\gamma)$  and  $\rho(E_f)$
- Calculation of  $\gamma$ SF from  $T(E_\gamma)$



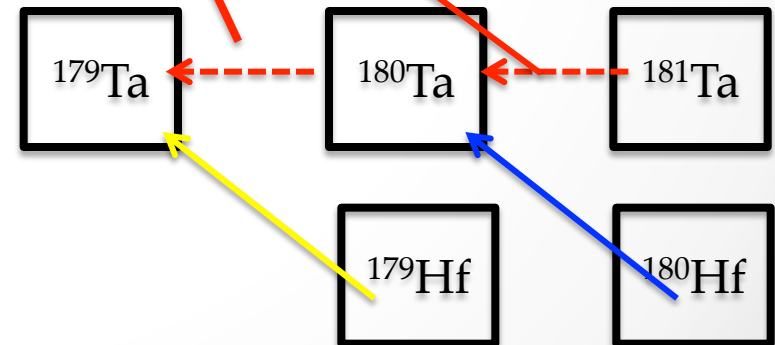
# 180,181,182Ta Preliminary Results

Maxwellian Average Cross Sections (MACS)

Reaction	$\langle E \rangle$ (keV)	MACS (mb)	Rec. MACS (mb)
$^{179}\text{Ta}(n,\gamma)$	30	$2469 \pm 508$	$1334 \pm 422$ [1]
	215	$828 \pm 288$	
$^{180}\text{Ta}(n,\gamma)$	30	$2051 \pm 148$	$1465 \pm 100$ [2,3]
	215	$589 \pm 53$	
$^{181}\text{Ta}(n,\gamma)$	30	$950 \pm 136$	$766 \pm 15$ [4]
	215	$259 \pm 46$	

Assumption: Detailed balance

s-process??



Radiative width and neutron resonance level spacing  $^{180}\text{Ta}$ .

The NLD and TSF were normalized to those of neighbouring isotopes ( $^{182}\text{Ta}$ ) with the requirement of having the same slope. Then obtained level density at the Sn was the used to determine the resonance spacing. This normalization does not give the uncertainties of D0 and Radiative width, so we assume 3 times the percentage of the uncertainties of the neighbouring isotopes ( $^{182}\text{Ta}$ ).

Spin dependence on of the gSF and NLD

So the ultimate question is: is the gamma-decay strength function the same for the high-spin states as the low-spin states?

The Brink-Axel hypothesis says yes, and experimentally it seems to be true too (for example Mathis' [PRL from 2012 on  \$^{95}\text{Mo}\$](#) ), although such extremely narrow spin windows have not been tested. But, depending on the neutron energies, p-wave capture might contribute, and this will make the populated spin range broader.

We did some DICEBOX simulations a long time ago with Milan Krticka from Prague University. For light nuclei ( $^{57}\text{Fe}$ ), a very narrow high-spin window for the initial states produced an artificial “upbend” at low gamma energies due to few available levels ([Larsen et al, PRC 83, 034315 \(2011\)](#)). But for  $^{180}\text{Ta}$  I would not expect such an effect, as it is a heavy, odd-odd nucleus with lots of levels.