

Level densities and γ strengths of $^{180,181,182}\text{Ta}$ and (n,γ) cross sections

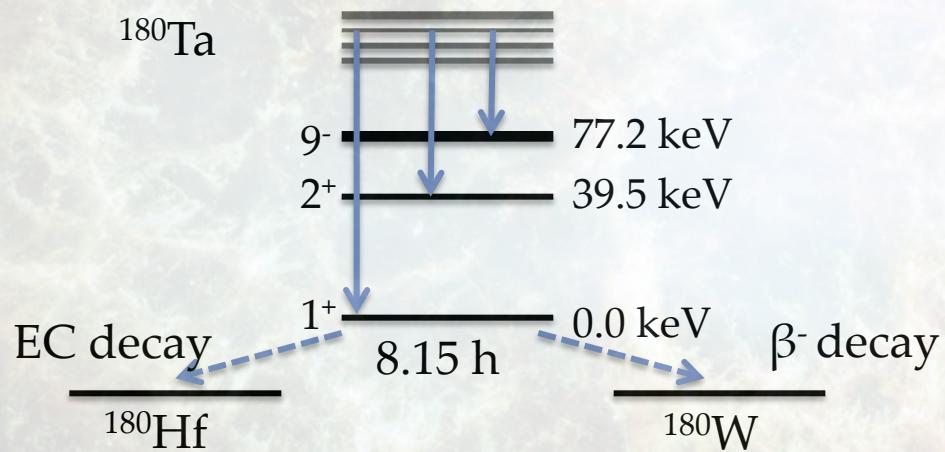
Kgashane Leroy Malatji

6th Workshop on Nuclear Level Density and Gamma Strength,
Oslo May 8-12, 2017

Introduction

Physics Motivation for ^{180}Ta

- Almost all $A > 110$ p -nuclei are thought to be produced by the photodisintegration of s - and r - process pre-existing nuclei
- However, the observed low abundance (0.012%) ^{180}Ta remains an exception
- The odd-odd ^{180}Ta exist in a 9^- isomeric state at 77 keV ($t_{1/2,iso} > 10^{15}$ yrs) in nature



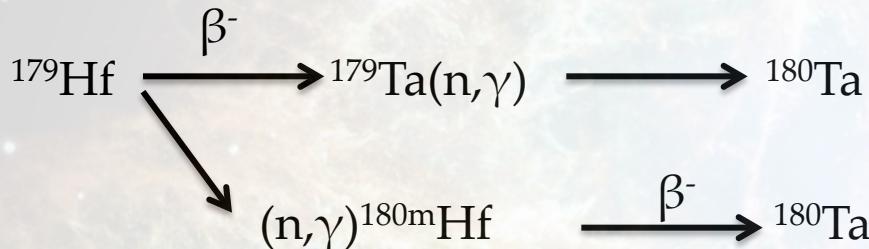
- Several processes are considered

Introduction

Physics Motivation for ^{180}Ta



- ^{180}Ta could be explained with p -process [1]
- The s -process mostly via branching in ^{179}Hf [2]

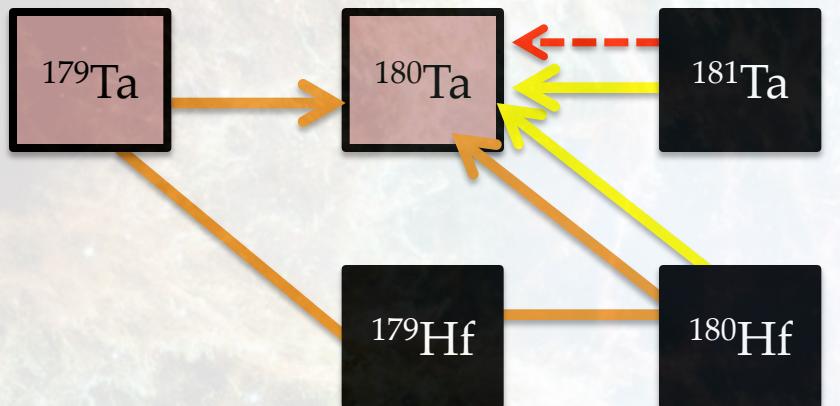


- $^{180}\text{Hf}(\nu_e, e)^{180}\text{Ta}$, $^{181}\text{Ta}(\nu, \nu'n)^{180}\text{Ta}$ and p -process contribute 50, 25 and 25%, respectively [3]
- $^{180}\text{Hf}(\nu_e, e)^{180}\text{Ta}$ 50% contribution recently supported by A. Byelikov et al. [4]

[1] M. Arnould and S. Goriely, Phys. Rep. 384, 1 (2003).
[2] M. Loewe et al. Nucl.Phys. A719 (2003) 275c
[3] A. Heger et al. Phys.Lett. B 606, 258 (2005)
[4] A. Byelikov et al. PRL 98, 082501 (2007)

Introduction

Physics Motivation for ^{180}Ta



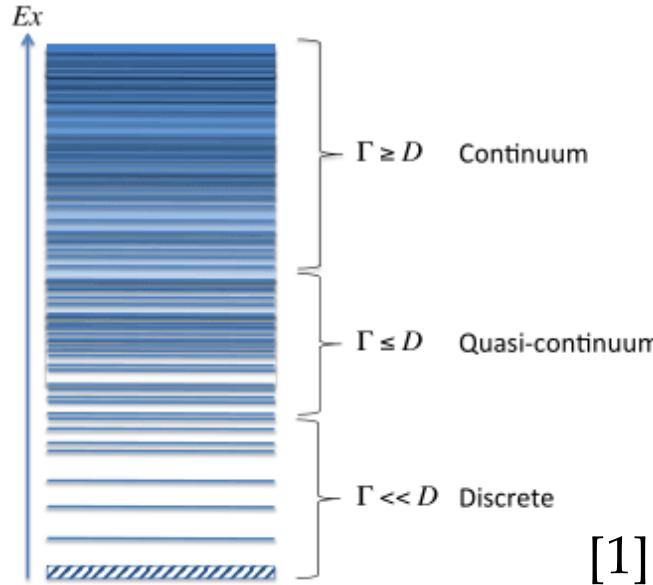
p -process
 s -process
 ν -process



- This is unresolved, hence provoking debates
- Uncertainties in reaction rates rest in nuclear properties
- Therefore production of ^{180}Ta needs to be reinvestigated with improved nuclear data

Objectives

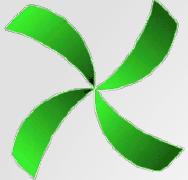
- Nuclear Level density (NLD) and γ -ray strength function (γ SF) below S_n in $^{180,181,182}\text{Ta}$ isotopes (Oslo Method)



- Astrophysical Maxwellian averaged (n, γ) cross sections (TALYS [2])
- Investigate production mechanism of ^{180}Ta
- ... additional nuclear structure aspects (C.P. Brits)

[1] Magne Guttormsen et al., Eur. Phys. J. A **51** (12), 170 (2015)

[2] A. J. Koning et al., Nuclear Data for Science and Technology (EDP Sciences; eds O. Bersillon et al.), p. 211 (2008) (see also <http://www.talys.eu>) version 1.6



Experimental Details

Oslo Cyclotron Laboratory



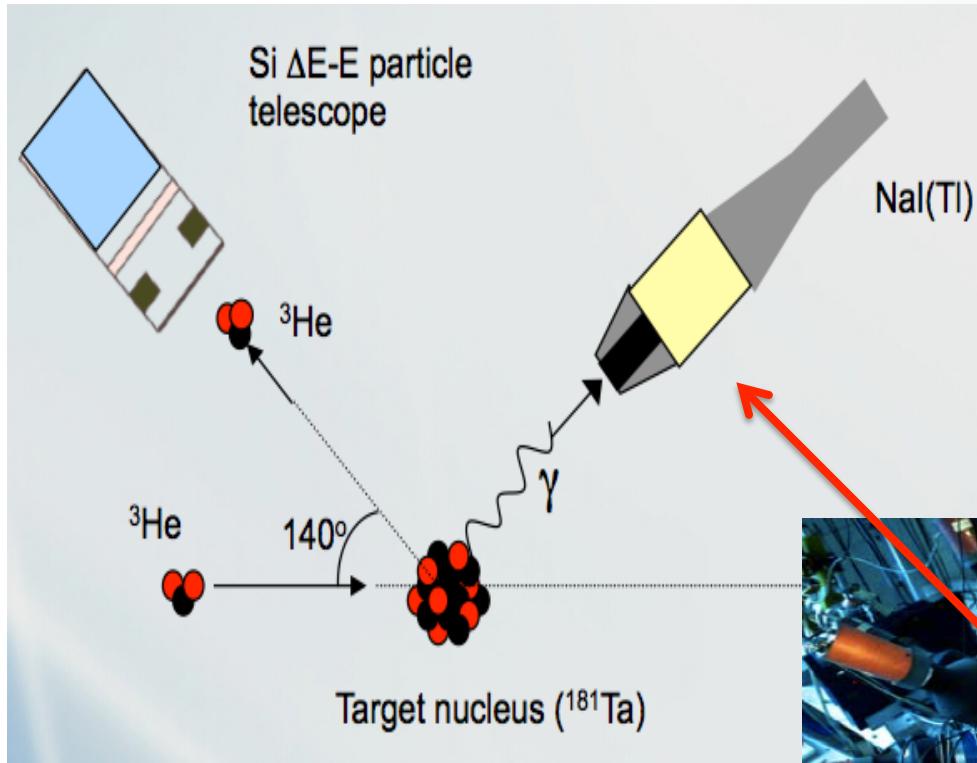
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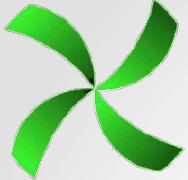
- 0.8 mg/cm² thick ¹⁸¹Ta natural target

- ¹⁸¹Ta(³He, X)^{180,181}Ta, 34 MeV
- ¹⁸¹Ta(d, X)^{180,181}Ta, 15 MeV
- ¹⁸¹Ta(d, X)^{181,182}Ta, 12.5 MeV



- CACTUS Array: 26 collimated 5"×5" NaI(Tl) (~22 cm)
- 14.1% eff. at E_γ = 1332 keV





Experimental Details

Oslo Cyclotron Laboratory



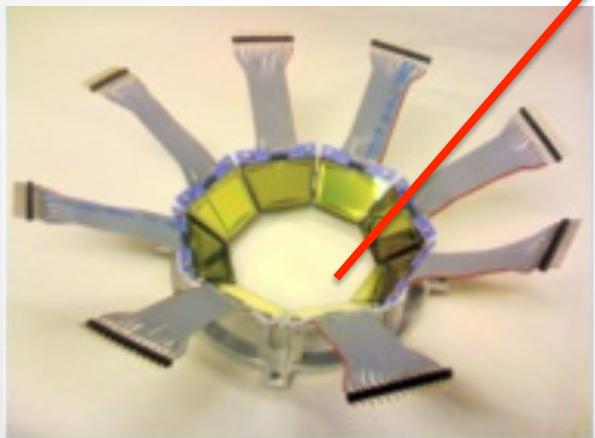
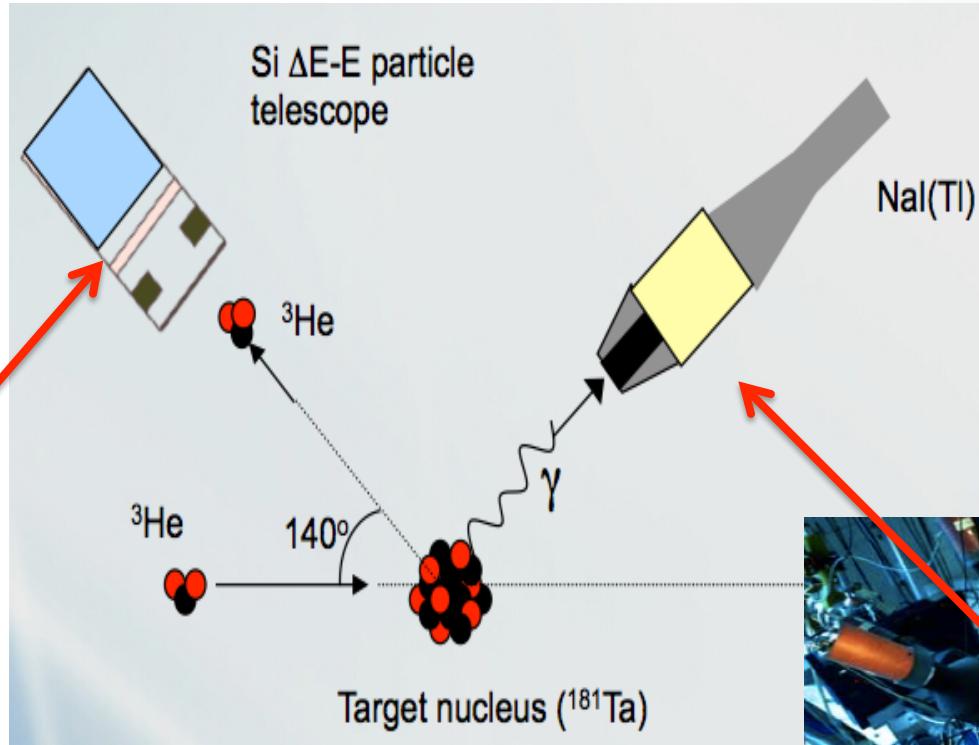
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- 0.8 mg/cm² thick ¹⁸¹Ta natural target

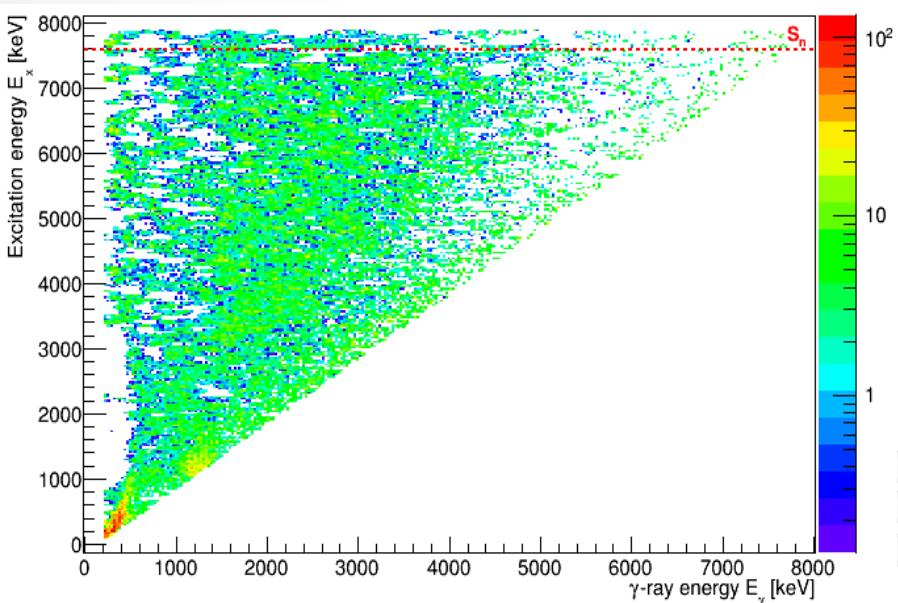
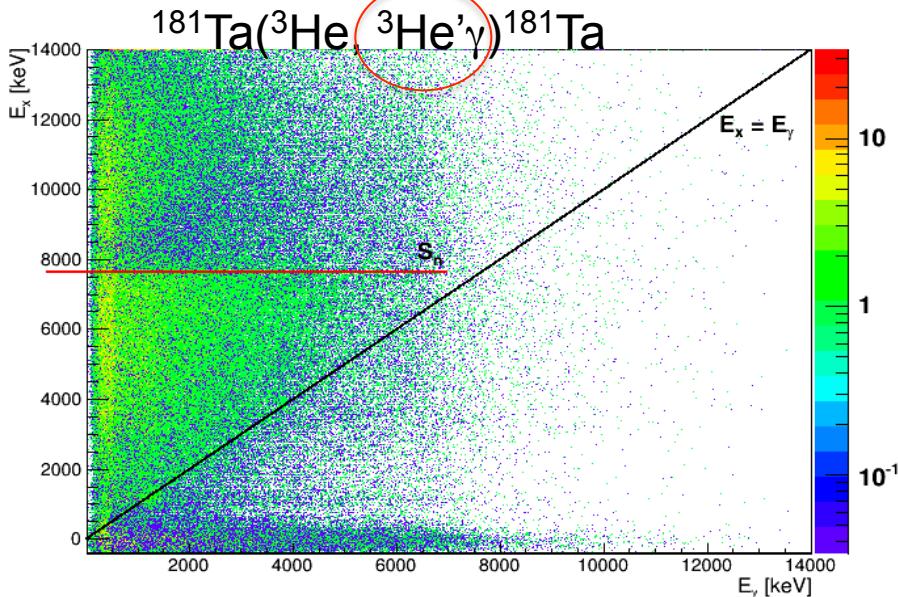
- ¹⁸¹Ta(³He, X)^{180,181}Ta, 34 MeV
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- SiRi Array, 64 ΔE-E Si particle telescopes
- ΔE, E and Al foil thicknesses (130 μm, 1550 μm and 10.5 μm)
- θ = 126° to 140°, ~ 5 cm

Data Analysis

Particle- γ Coincidence Matrices



The Oslo Method

1. Unfolding γ -ray continuum spectra[1]
 - > Unfolding iterative procedure
2. Extraction of primary γ -rays [2]
 - > first-generation method
3. Simultaneous extraction of level density and strength function[3]

$$\lambda_{if} = \frac{2\pi}{\hbar} |M_{if}|^2 \cdot \rho(E_f)$$

Fermi's golden rule

$$P(E_i, E_\gamma) \propto \rho(E_f) \cdot \mathcal{T}(E_\gamma) \quad \text{Assumes Brink hypothesis}$$

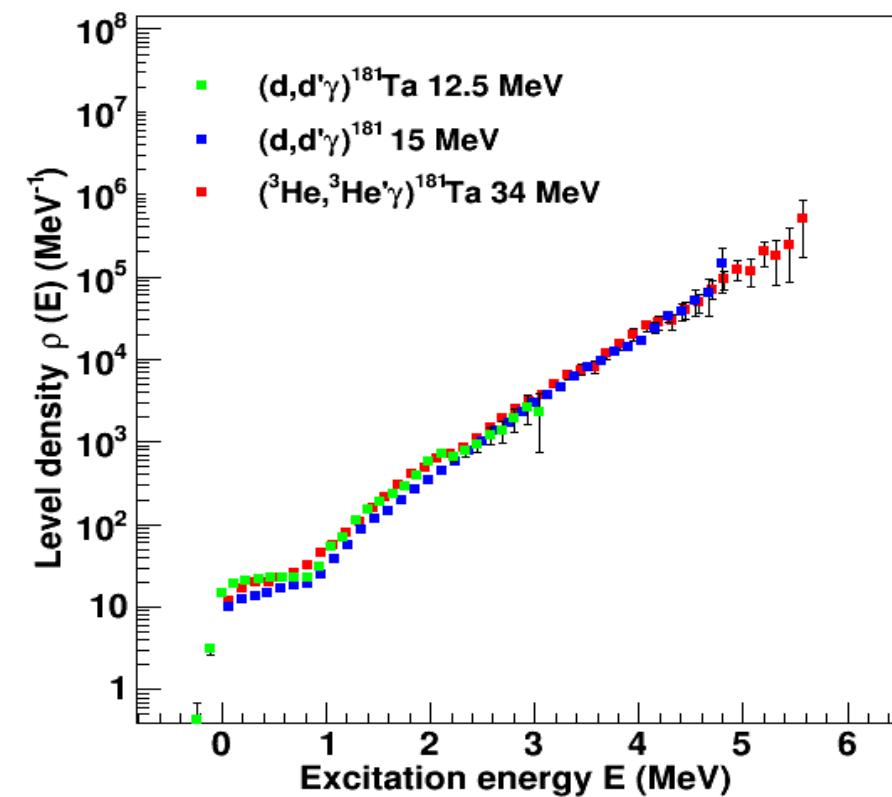
4. Normalization

- [1] M. Guttormsen et al., NIM Phys. Res. A 374, 371 (1996)
- [2] M. Guttormsen et al., NIM Phys. Res. A 255, 518 (1987)
- [3] A. Schiller et al., NIM Phys. Res. A 447, 498 (2000)

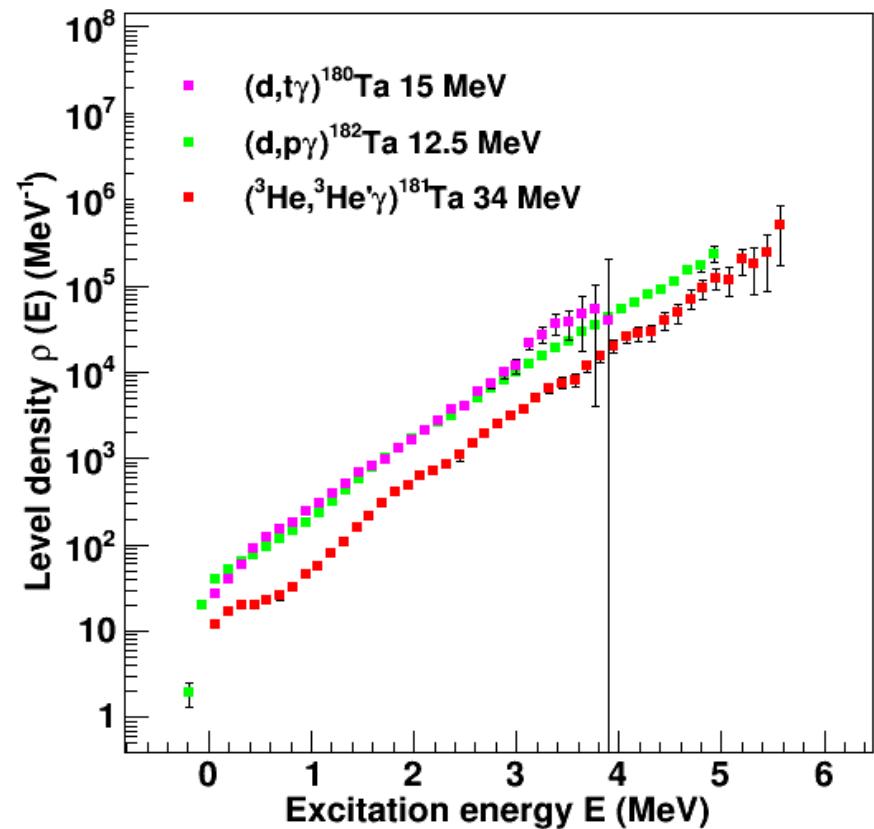
180,181,182Ta Results

Nuclear Level Density

Different reactions yield similar results



NLDs of neighbouring isotopes

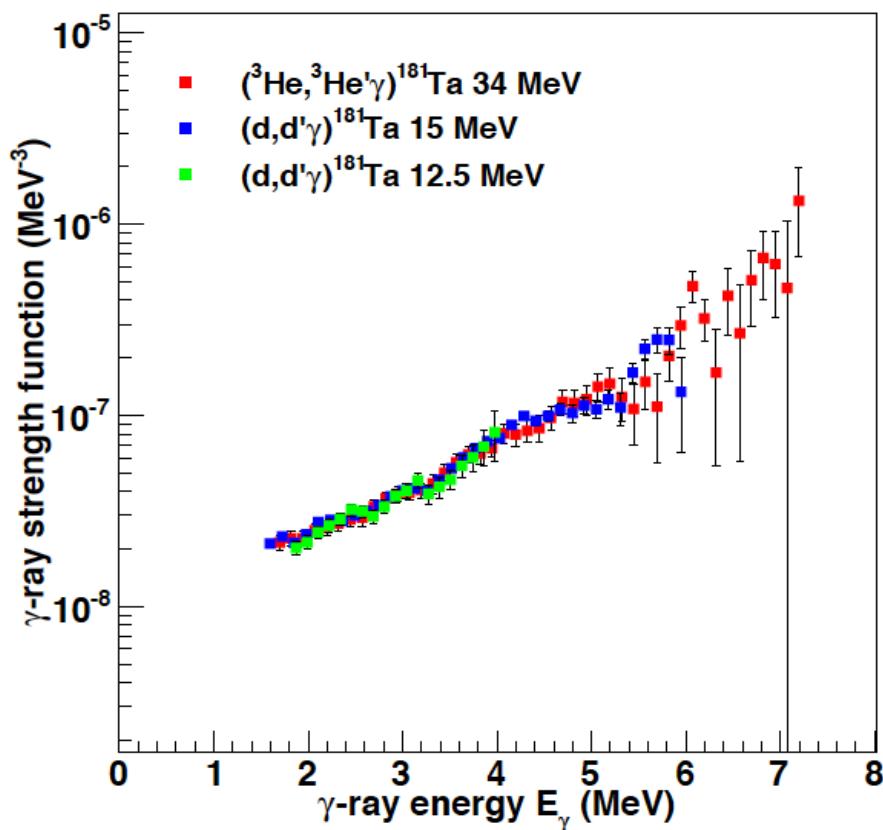


180,181,182Ta Results

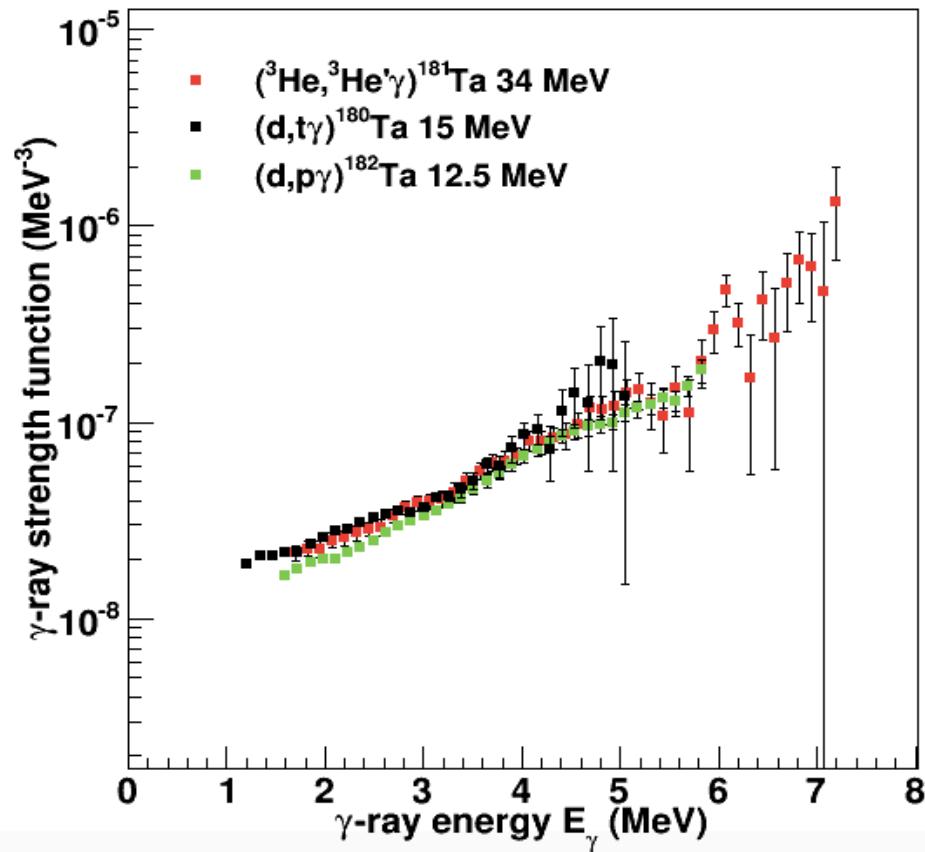
γ -ray Strength Function

$$f(E_\gamma) = \frac{1}{2\pi E_\gamma^3} B\mathcal{T}(E_\gamma) \quad [1]$$

Different reactions yield similar results



γ SFs of neighbouring isotopes



^{181}Ta Results

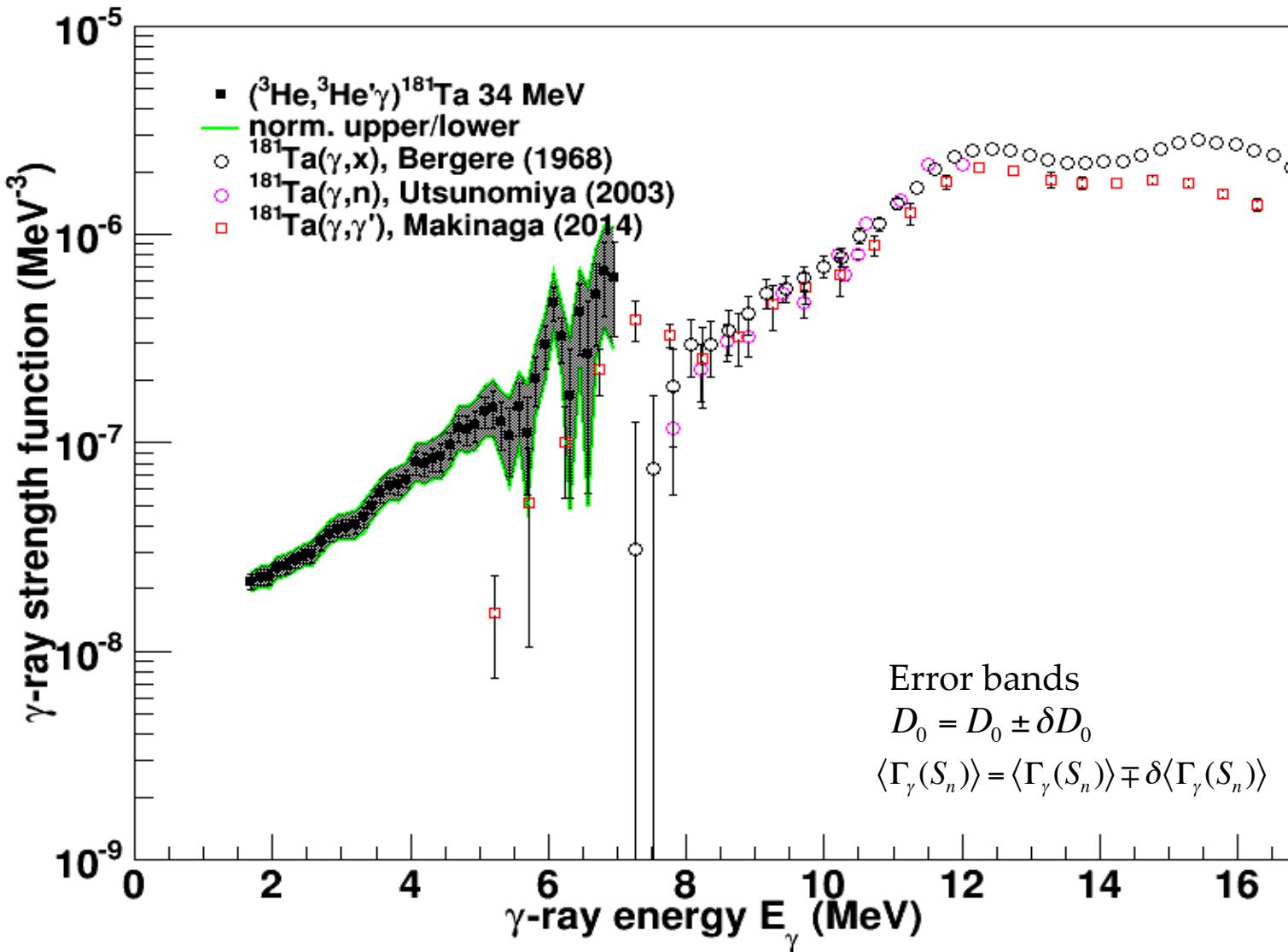
Comparison of $^{181}\text{Ta}(^3\text{He}, ^3\text{He}'\gamma) \gamma\text{SF}$ with photoabsorption data



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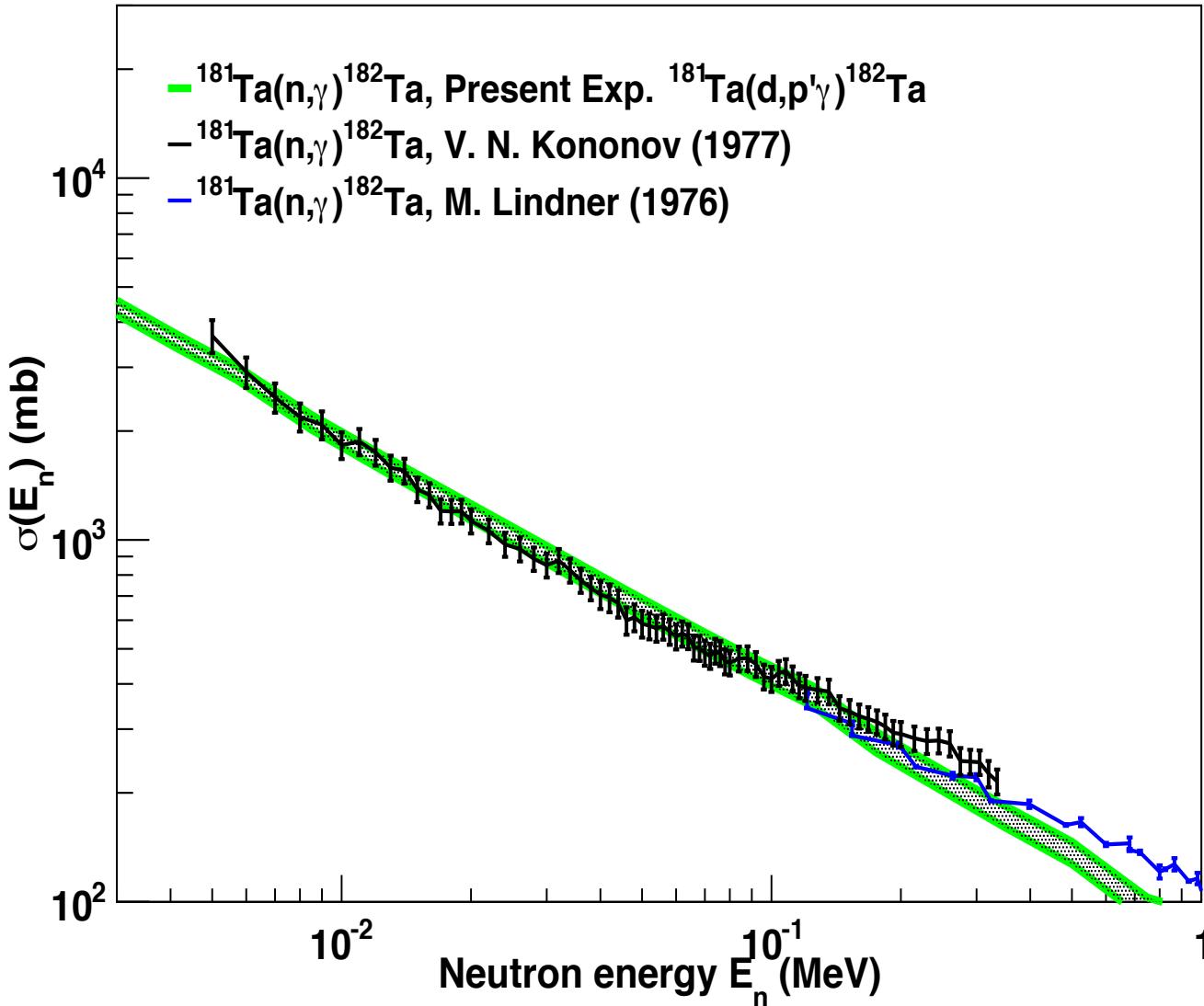


^{182}Ta Results

Neutron Capture Cross Section Calculations



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TALYS

Key ingredients
(HF approach)
- γ SF, NLD and OMP

^{181}Ta Results

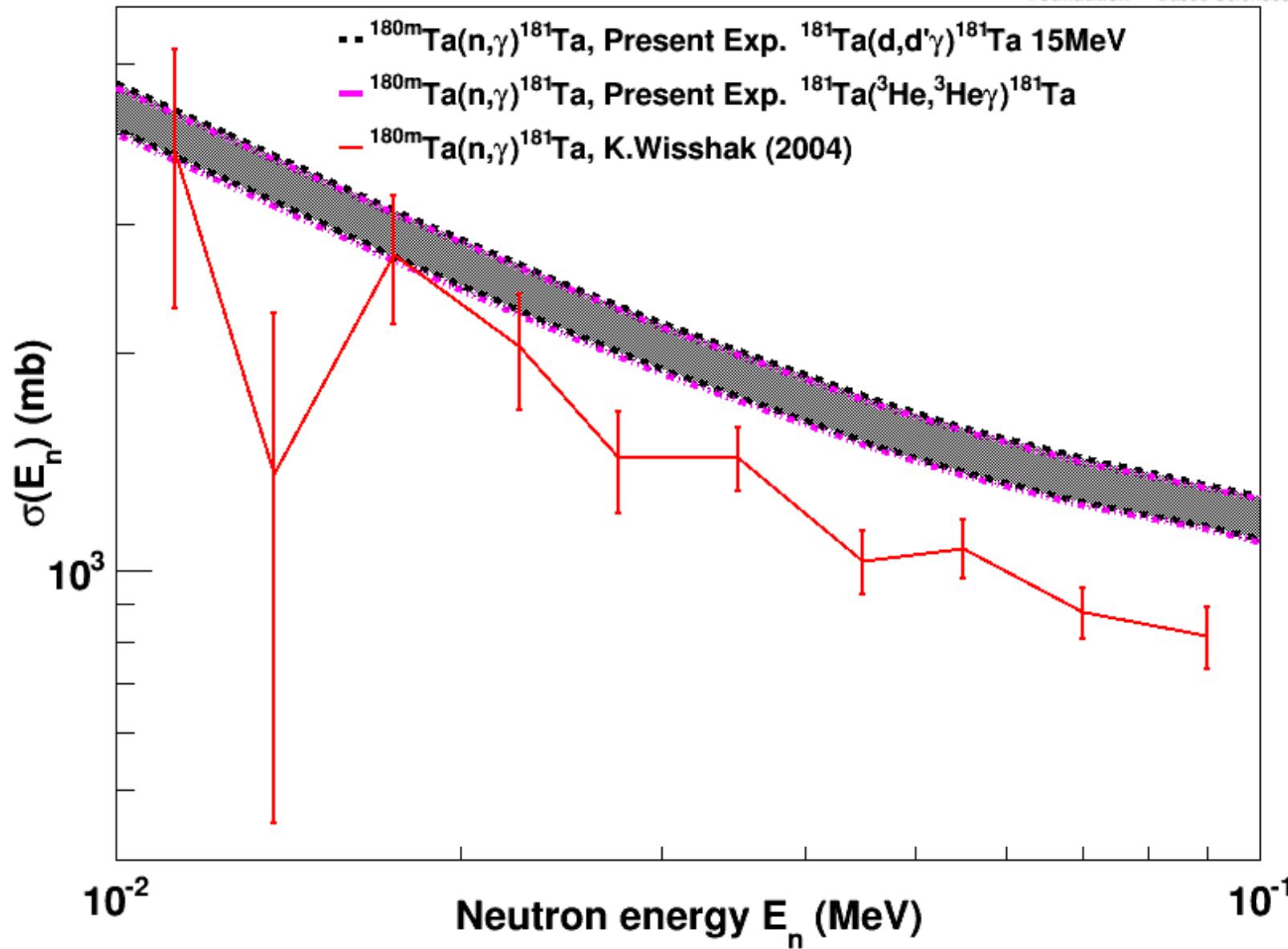
Neutron Capture Cross Section Calculations



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^{180}Ta Results

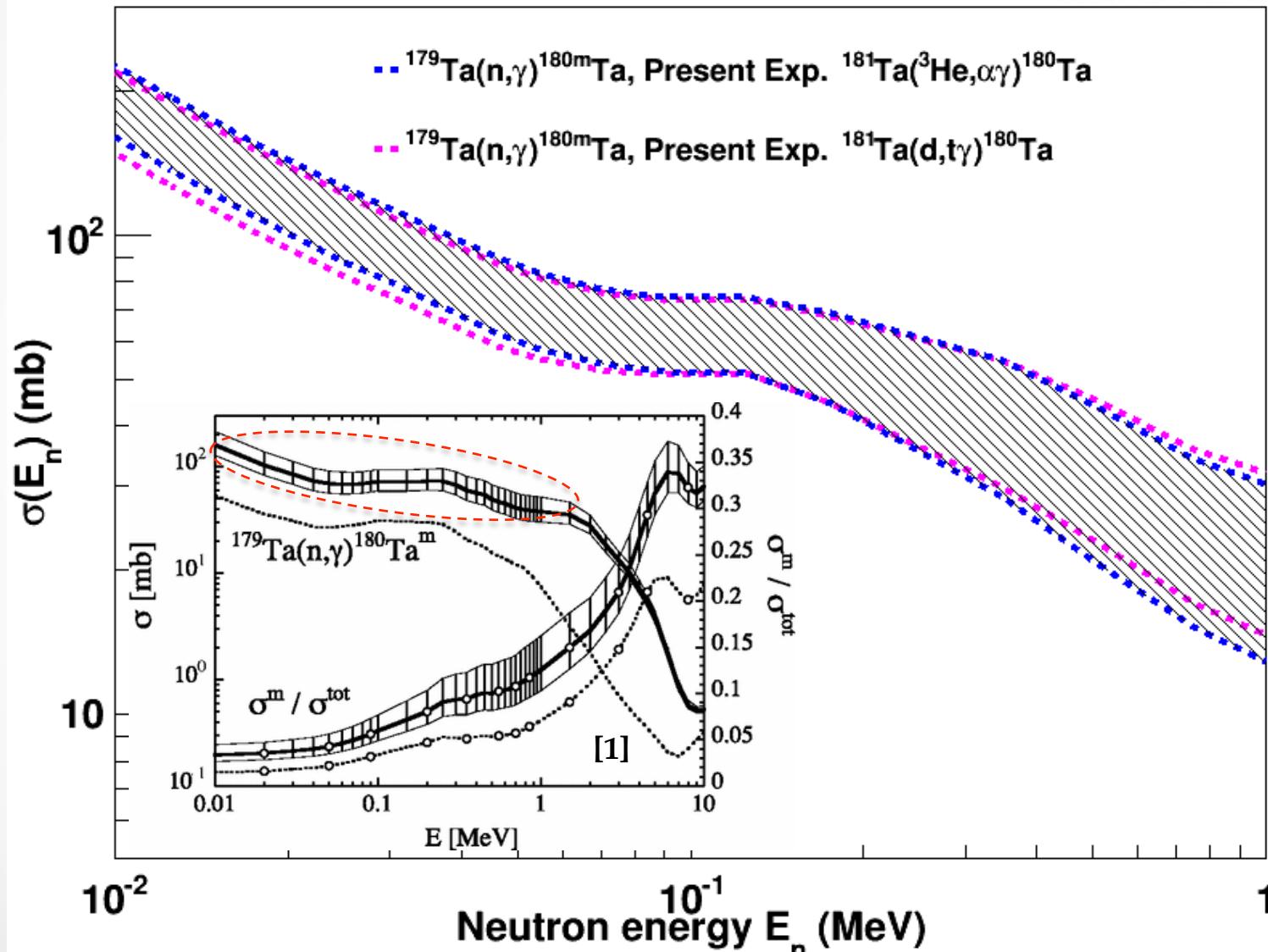
Neutron capture Cross Section Calculations



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$^{180,181,182}\text{Ta}$ Results

Maxwellian Averaged (n,γ) Cross Sections



Reaction	$\langle E \rangle$ (keV)	MACS (mb)	KADoNiS. MACS (mb) [1]
$^{179}\text{Ta}(n,\gamma)$	30	2613 ± 681	1334 ± 422
	215	825 ± 292	
$^{180\text{m}}\text{Ta}(n,\gamma)$	30	2224 ± 169	1465 ± 100
	215	803 ± 78	
$^{180\text{gs}}\text{Ta}(n,\gamma)$	30	2191 ± 178	1640 ± 260
	215	619 ± 70	
$^{181}\text{Ta}(n,\gamma)$	30	936 ± 52	766 ± 15
	215	243 ± 17	

- [1] I. Dillmann et al. , AIP Conf. Proc. 819 , 123; online at <http://www.kadonis.org>

Summary and Outlook

- Experiments successfully performed at the Oslo cyclotron laboratory
- The γ SF and NLD of $^{180,181,182}\text{Ta}$ extracted with the Oslo Method
- First time, measurements of NLD and γ SF below Sn in ^{180}Ta and below 5 MeV in ^{181}Ta experimentally
- The experimental γ SF and NLD used to investigate (n,γ) cross sections
- The newly deduced $^{179,180,181}\text{Ta}$ MACS will be used in a continued collaboration with S. Goriely
- Evaluate galactic production mechanism of ^{180}Ta and possibly constrain the astrophysical environments.
- TALYS calculation using theoretical models...

Acknowledgements

K. L. Malatji^{1,2}, B. V. Kheswa^{2,3}, M. Wiedeking², F. L. Bello Garrote³, D. L. Bleuel⁴, C.P Brits^{1,2}, F. Giacoppo^{5,6}, S. Goriely⁷, A. Görgen³, M. Guttormsen³, K. Hadynska-Klek³, T. W. Hagen³, V. W. Ingeberg³, M. Klintefjord³, A. C. Larsen³, H. T. Nyhus³, T. Renstrøm³, S. Rose³, E. Sahin³, S. Siem³, G. M. Tveten³ and F. Zeiser³.

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⁷ Institut d'Astronomie et d'Astrophysique, Université Libre de Bruxelles, CP 226, B-1050 Brussels, Belgium

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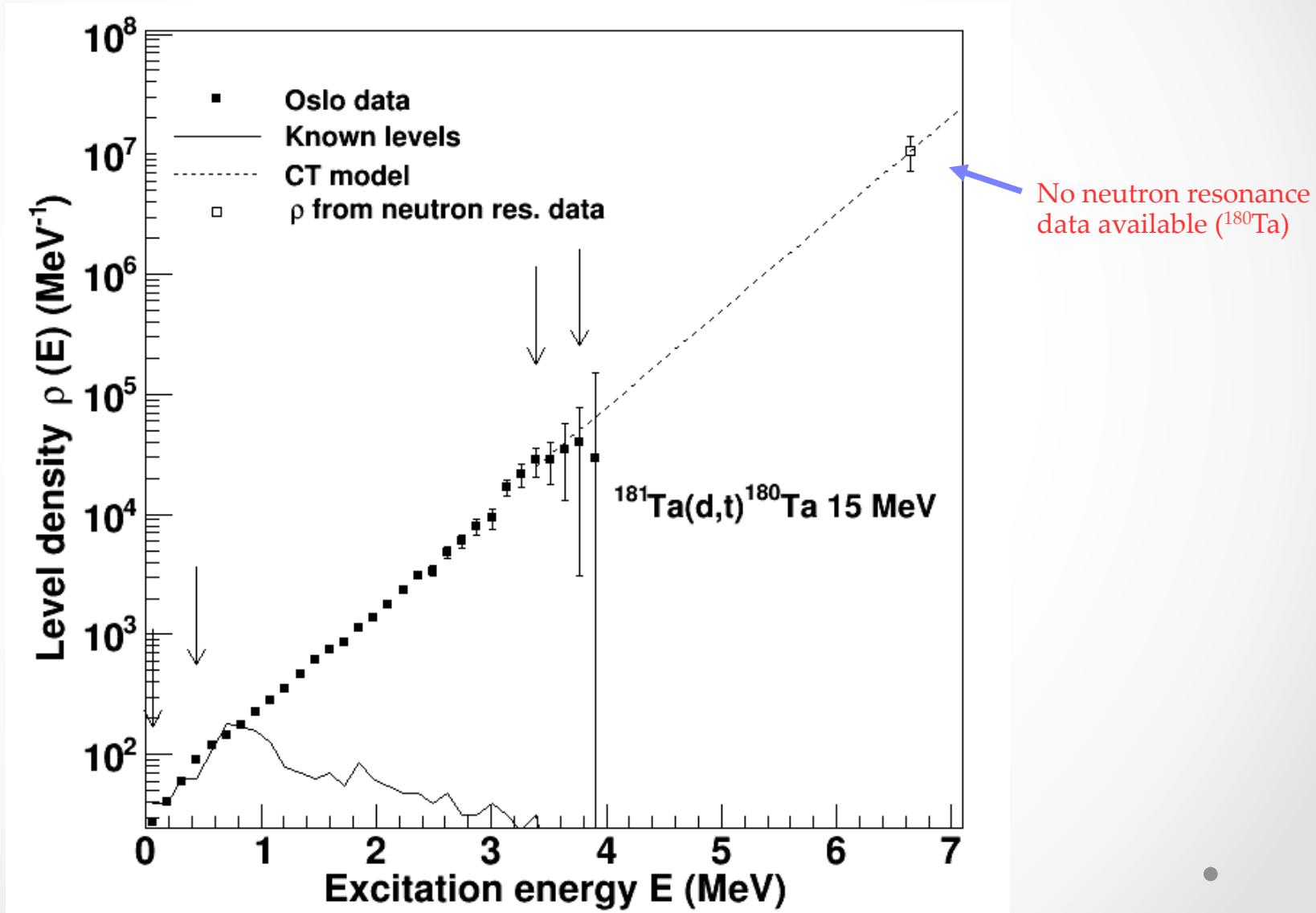
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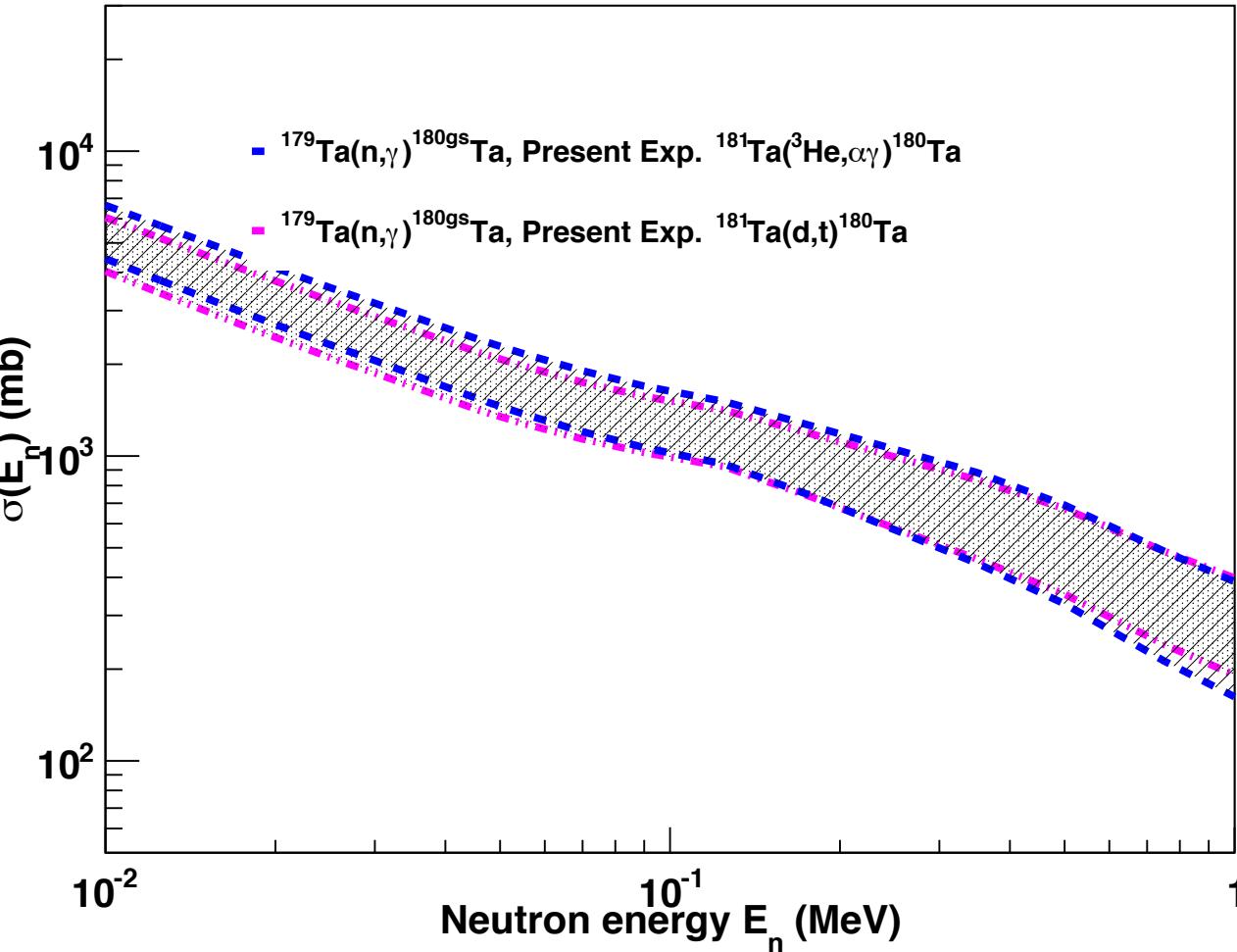
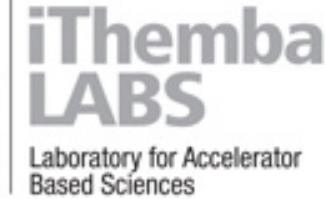
^{180}Ta Results

Normalization of the NLD

$$\rho(S_n) = \frac{2\sigma^2}{D_0(J_T + 1)e^{[-(J_T+1)^2/2\sigma^2]} + e^{(-J_T^2/2\sigma^2)}J_T}$$



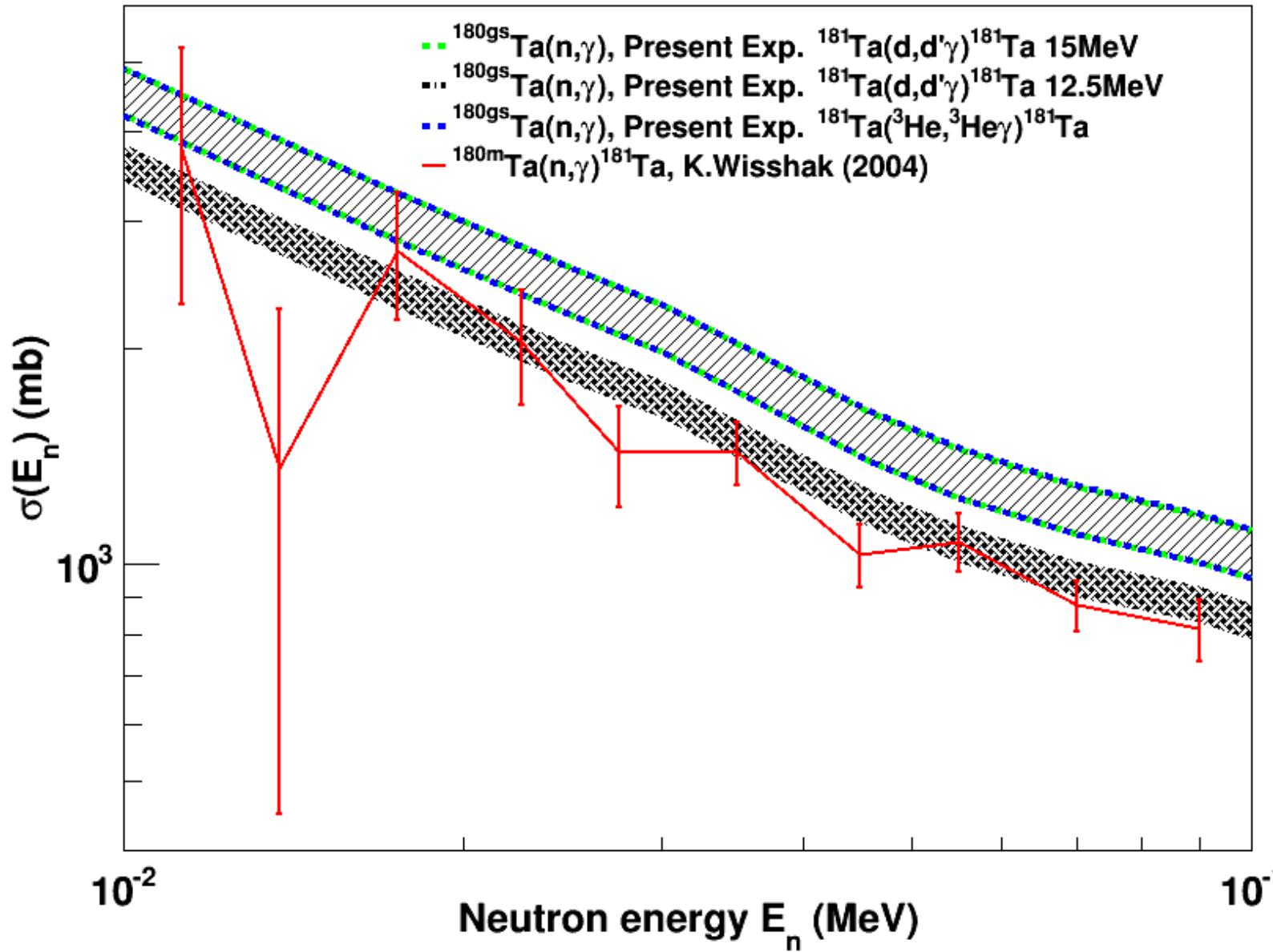
$^{180}\text{gsTa}$ Cross Section



^{181}Ta Cross Section



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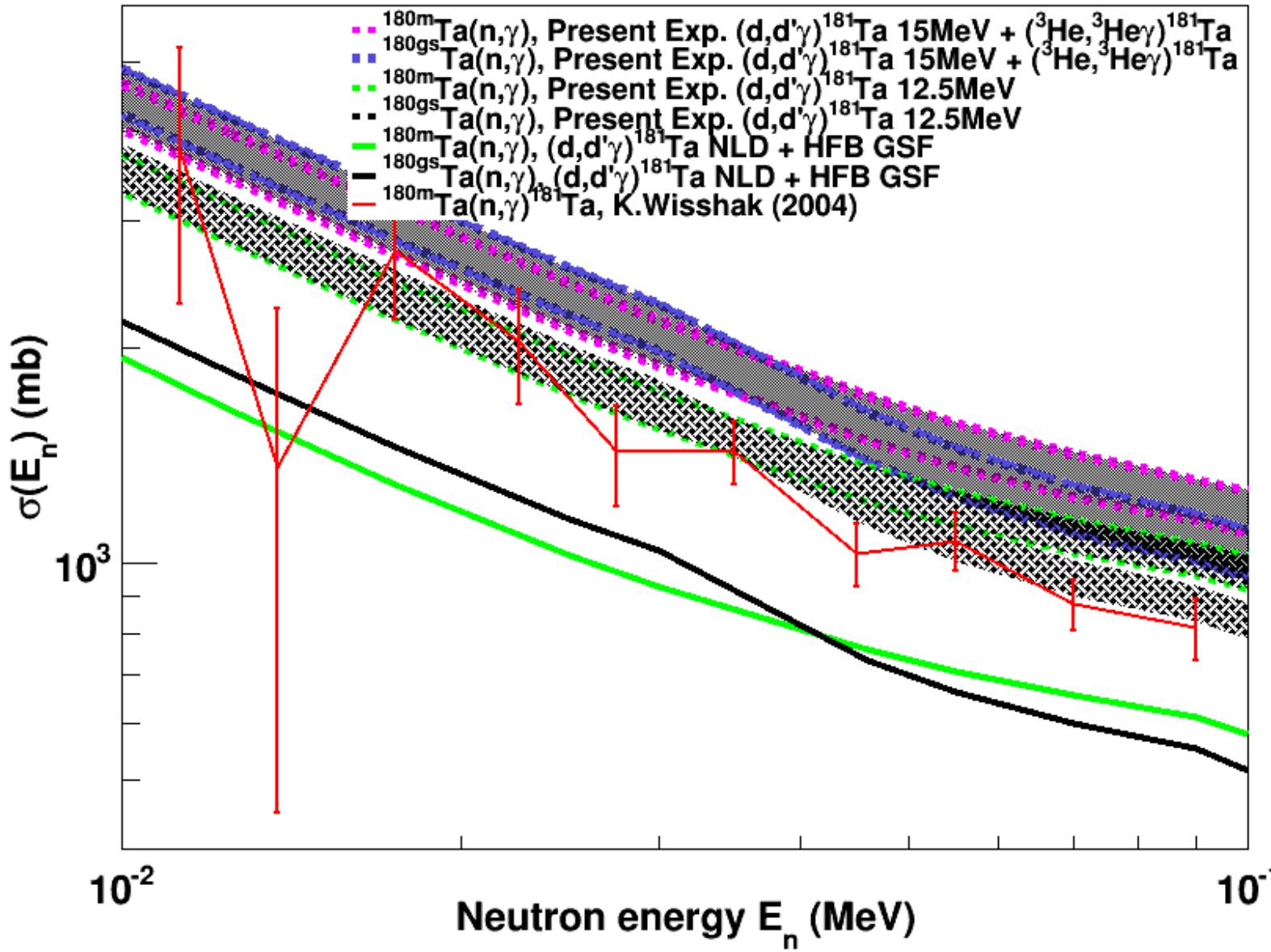
^{181}Ta Cross Section



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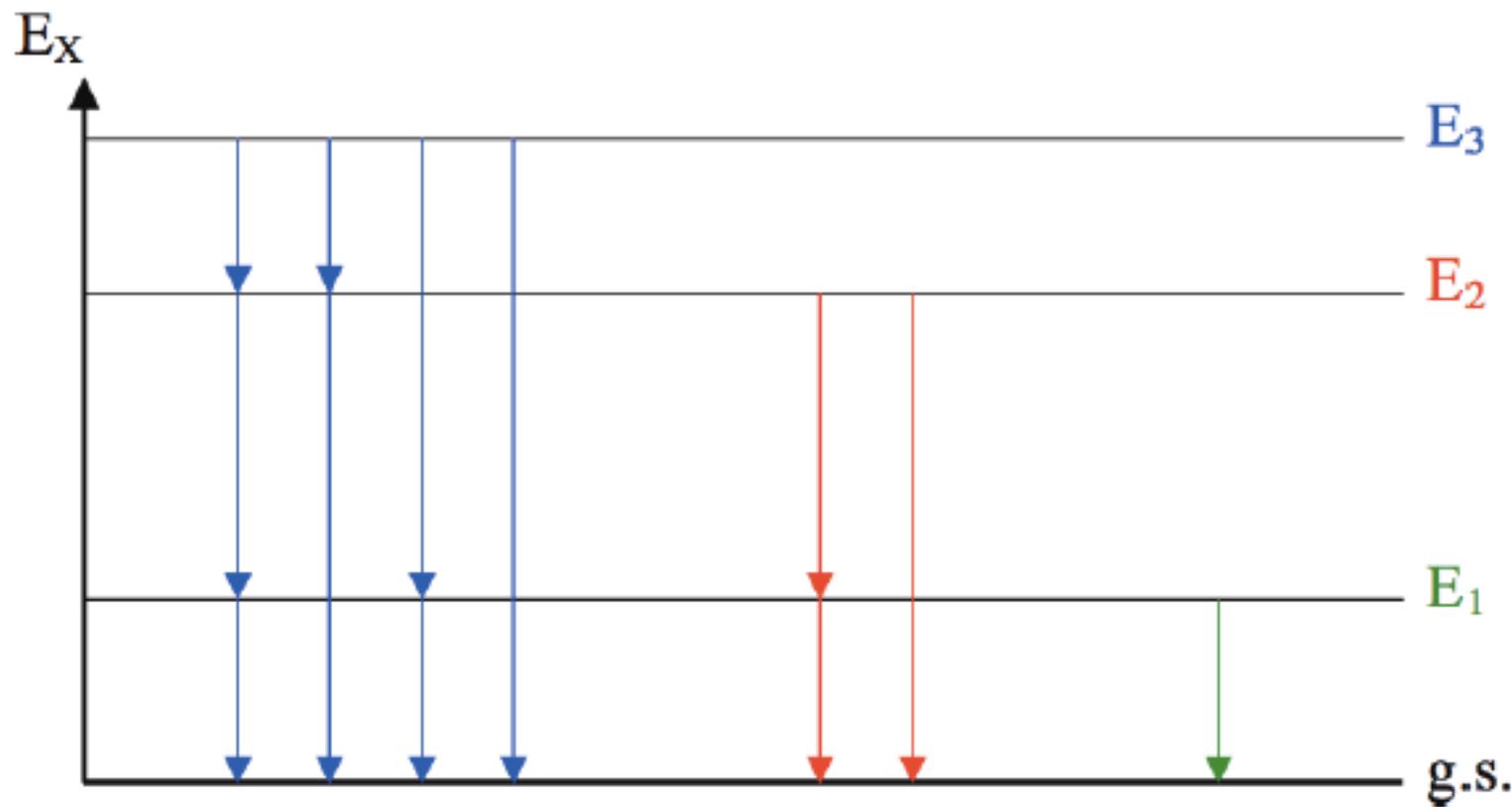
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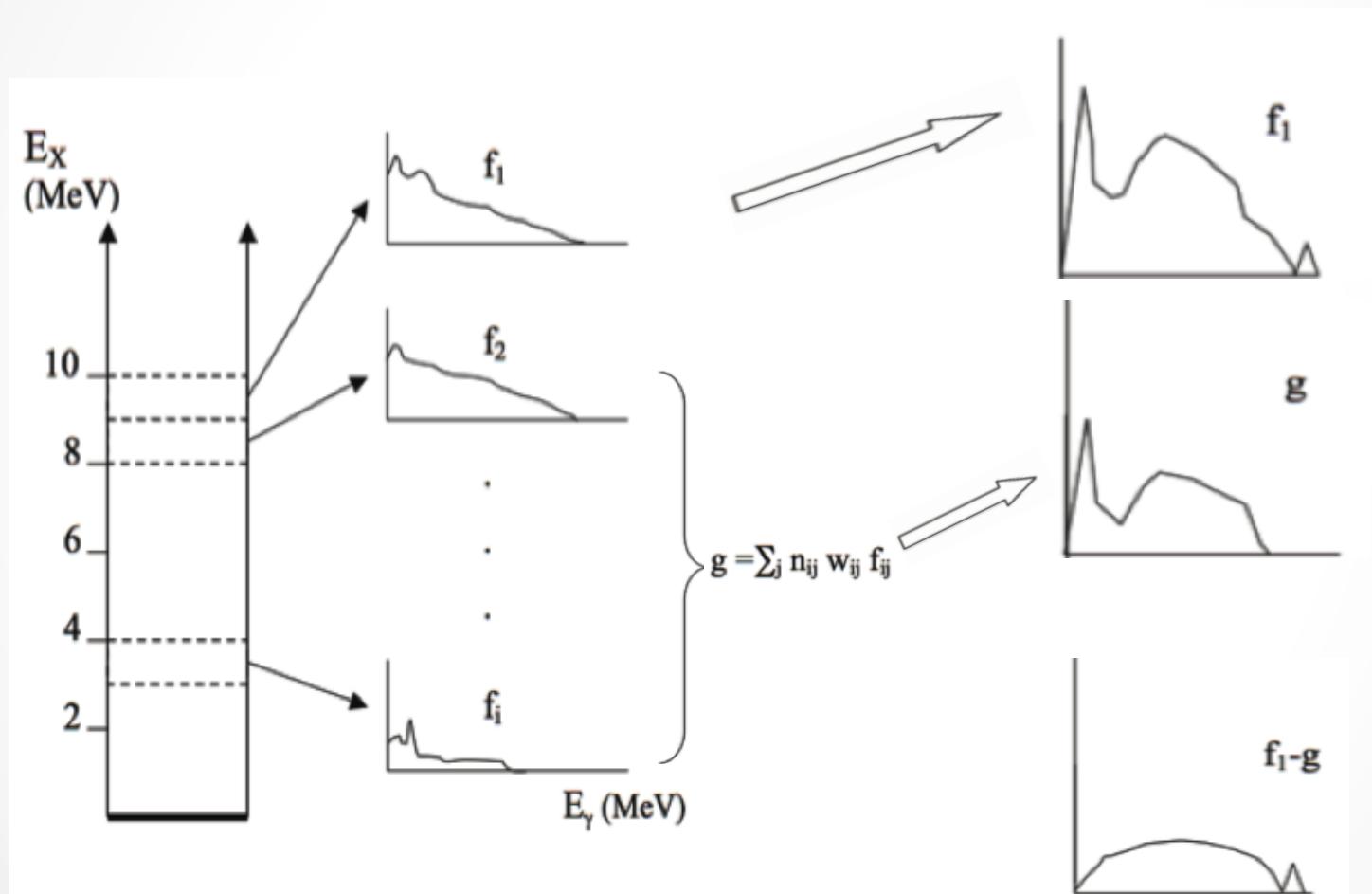
Oslo Method

First Generation Method



Oslo Method

First Generation Method



Oslo Method

Factorization of the First-Generation Matrix

- According Fermi's golden rule: $\lambda_{if} \propto |\langle f|H'|i\rangle|^2 \rho(E_f)$
where $\rho(E_f)$ is the NLD at a final state
is the matrix elements $|\langle f|H'|i\rangle|$
- Equivalent equation for the FG matrix: $P(E_i, E_f) \propto \rho(E_f) T_{if}$
where T_{if} is the γ transmission coefficient
- Brink Hypothesis: GEDR can be built on every state, and its properties don't depend on the properties of the initial and final state.
- T_{if} only depend on the γ -ray energy

Oslo Method

Simultaneous Extraction of T and NLD

- The $\mathcal{T}(E_\gamma)$ and $\rho(E_f)$ are extracted by fitting $P_{th}(E_x, E_\gamma)$ to $P(E_x, E_\gamma)$ and minimizing

$$\chi^2 = \frac{1}{N} \sum_{E_x} \sum_{E_\gamma} \frac{(P_{th}(E_x, E_\gamma) - P(E_x, E_\gamma))}{\Delta P(E_x, E_\gamma)}$$

Where $P_{th}(E_x, E_\gamma) = \frac{\rho(E_f)\mathcal{T}(E_\gamma)}{\sum_{E_\gamma} \rho(E_f)\mathcal{T}(E_\gamma)}$

and $N, \Delta P(E_x, E_\gamma)$ are degrees of freedom and uncertainty in $P(E_x, E_\gamma)$

Oslo Method

Normalization of T and NLD

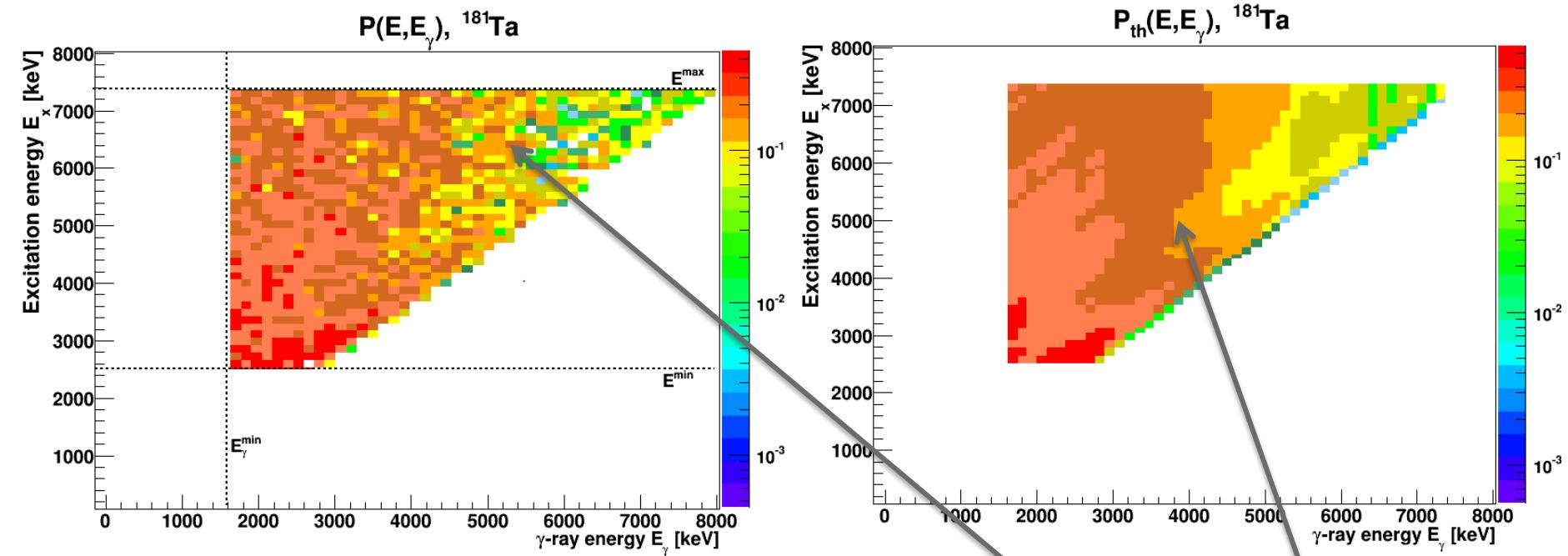
- Once $\rho(E_f)$ and $\mathcal{T}(E_\gamma)$ are extracted
- Infinitely many solutions can be found of the form

Where α is a common slope between $\tilde{\rho}(E_f)$ and $\tilde{\mathcal{T}}(E_\gamma)$
 And B are normalization parameters

- α and A are obtained by normalizing $\tilde{\rho}(E_f)$ to $\rho(S_n)$ and ρ of known discrete states
- B can be calculated from experimental $\langle \Gamma_\gamma \rangle$ and D_0 @ neutron threshold

Data Analysis

Experimental vs. Fitted FG Matrices



- Assumptions: Brink Hypothesis
- The $\rho(E_f)$ and $\mathcal{T}(E_\gamma)$ are extracted by fitting to $P(E_x, E_\gamma)$ and performing χ^2 minimum.

$$P(E, E_\gamma) \propto \rho(E_f) \mathcal{T}(E_\gamma).$$

The Oslo Method

- Normalization of (γ transmission coefficient) $\mathcal{T}(E_\gamma)$ and $\rho(E_f)$
- Calculation of γ SF from $\mathcal{T}(E_\gamma)$

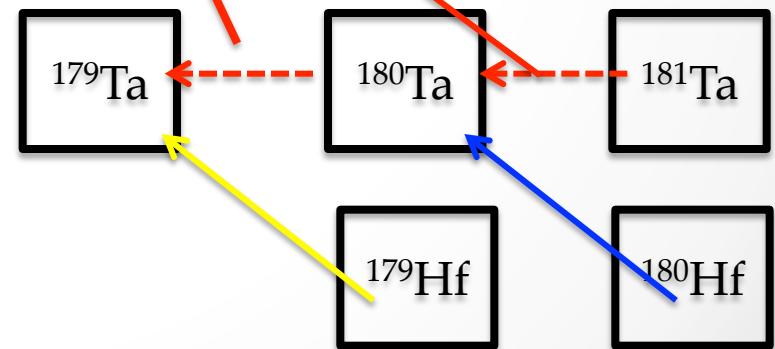
$^{180,181,182}\text{Ta}$ Preliminary Results

Maxwellian Average Cross Sections (MACS)

Reaction	$\langle E \rangle$ (keV)	MACS (mb)	Rec. MACS (mb)
$^{179}\text{Ta}(n,\gamma)$	30	2469 ± 508	1334 ± 422 [1]
	215	828 ± 288	
$^{180}\text{Ta}(n,\gamma)$	30	2051 ± 148	1465 ± 100 [2,3]
	215	589 ± 53	
$^{181}\text{Ta}(n,\gamma)$	30	950 ± 136	766 ± 15 [4]
	215	259 ± 46	

Assumption: Detailed balance

s-process??



Radiative width and neutron resonance level spacing 180Ta.

The NLD and TSF were normalized to those of neighbouring isotopes (182Ta) with the requirement of having the same slope. Then obtained level density at the Sn was used to determine the resonance spacing. This normalization does not give the uncertainties of D0 and Radiative width, so we assume 3 times the percentage of the uncertainties of the neighbouring isotopes (182Ta).

Spin dependence on of the gSF and NLD

So the ultimate question is: is the gamma-decay strength function the same for the high-spin states as the low-spin states?

The Brink-Axel hypothesis says yes, and experimentally it seems to be true too (for example Mathis' [PRL from 2012 on 95Mo](#)), although such extremely narrow spin windows have not been tested. But, depending on the neutron energies, p-wave capture might contribute, and this will make the populated spin range broader.

We did some DICEBOX simulations a long time ago with Milan Krticka from Prague University. For light nuclei ([57Fe](#)), a very narrow high-spin window for the initial states produced an artificial "upbend" at low gamma energies due to few available levels ([Larsen et al, PRC 83, 034315 \(2011\)](#)). But for 180Ta I would not expect such an effect, as it is a heavy, odd-odd nucleus with lots of levels.